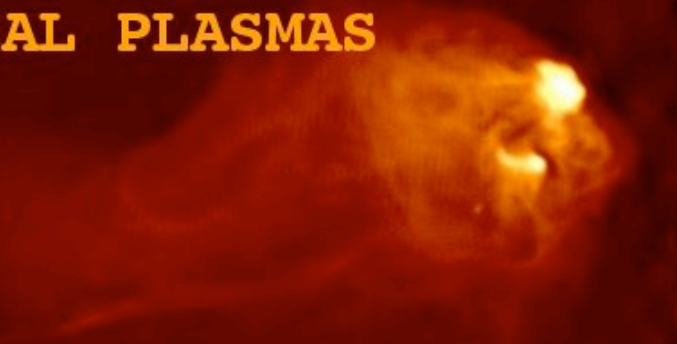


**KINETIC MODELING OF ASTROPHYSICAL PLASMAS**

October 5-9, 2008  
Krakow, Poland



# Relativistic Current Sheets in Electron-Positron Plasmas

Seiji Zenitani

NASA Goddard Space Flight Center

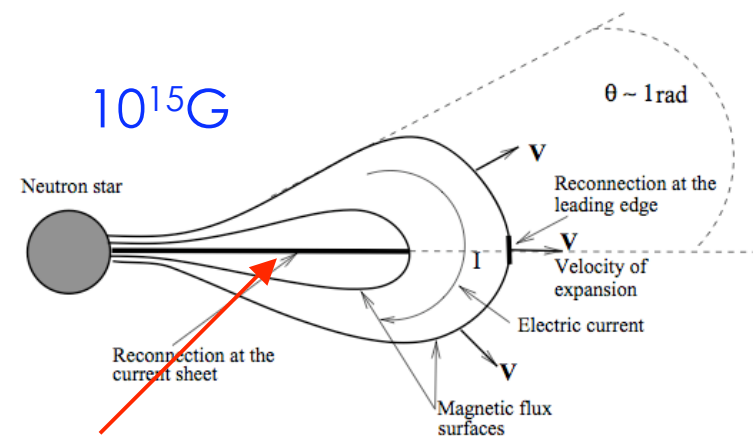
Collaborators: M. Hoshino (U. Tokyo), M. Hesse, A.  
Klimas (NASA/GSFC)

# Outline

- Introduction
- Basic processes in a relativistic current sheet
  - 2D Reconnection
  - 2D Drift Kink Instability
  - 3D Evolution
  - 3D Guide field effect
  - Weibel instability
- Discussions
- Large-scale MHD problem (option)
- Summary + Open questions

# Sites of relativistic current sheets

- Pulsar winds
  - Magnetic dissipation in relativistic outflow of electron positron plasma winds
- Magnetars
  - giant flare models for SGR
- Various potential sites
  - Active galactic nuclei
  - Gamma ray bursts

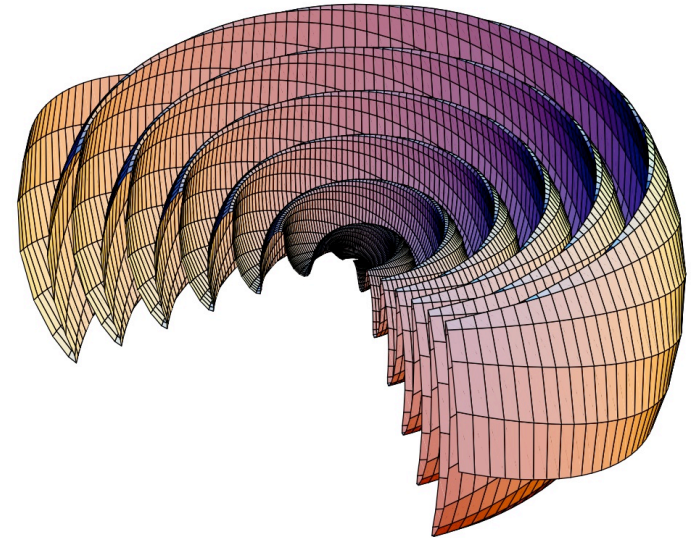


Reconnection  
in the current sheet

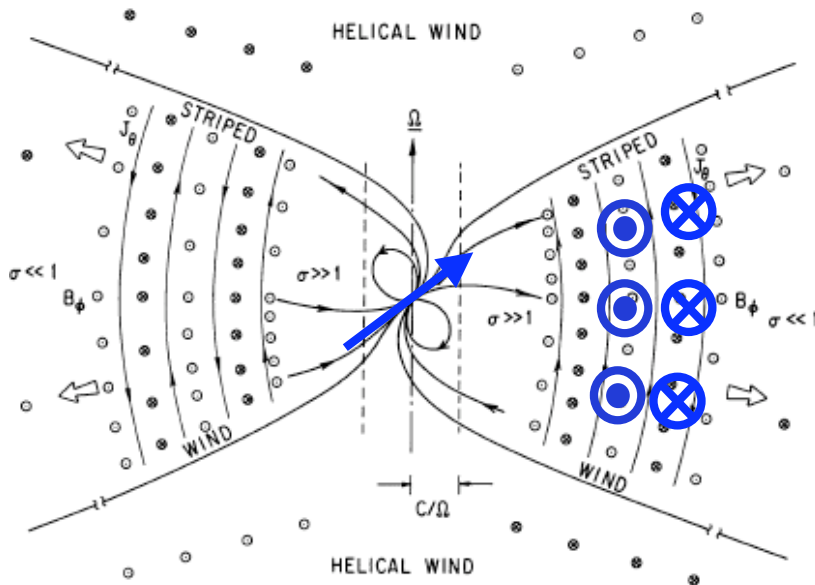
Lyutikov 2006 MNRAS

# Striped pulsar wind

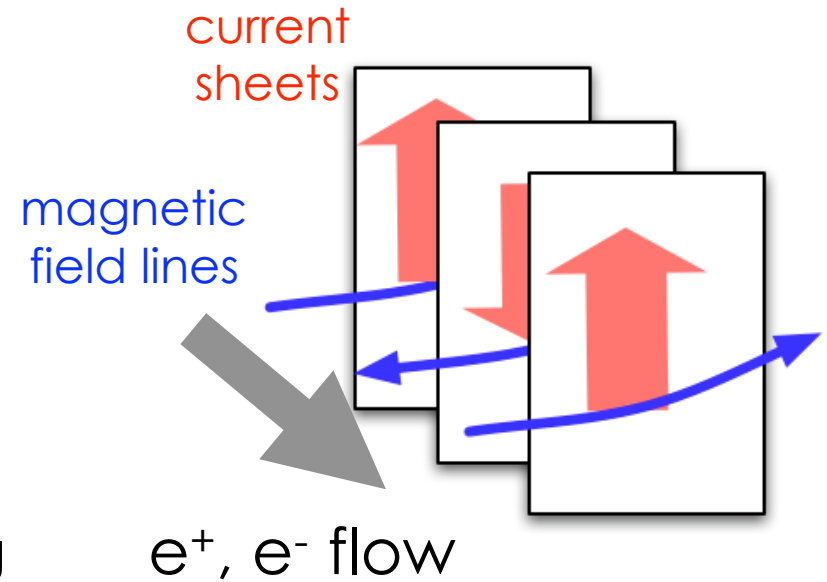
- Magnetic dissipation process is highly demanded in the striped current sheets (Coroniti 1990 ApJ, Lyubarsky & Kirk 2001 ApJ, Kirk & Skjaeraasen 2003 ApJ)



Kirk et al. 2007 [astroph/0703116](#)



Coroniti 1990 ApJ



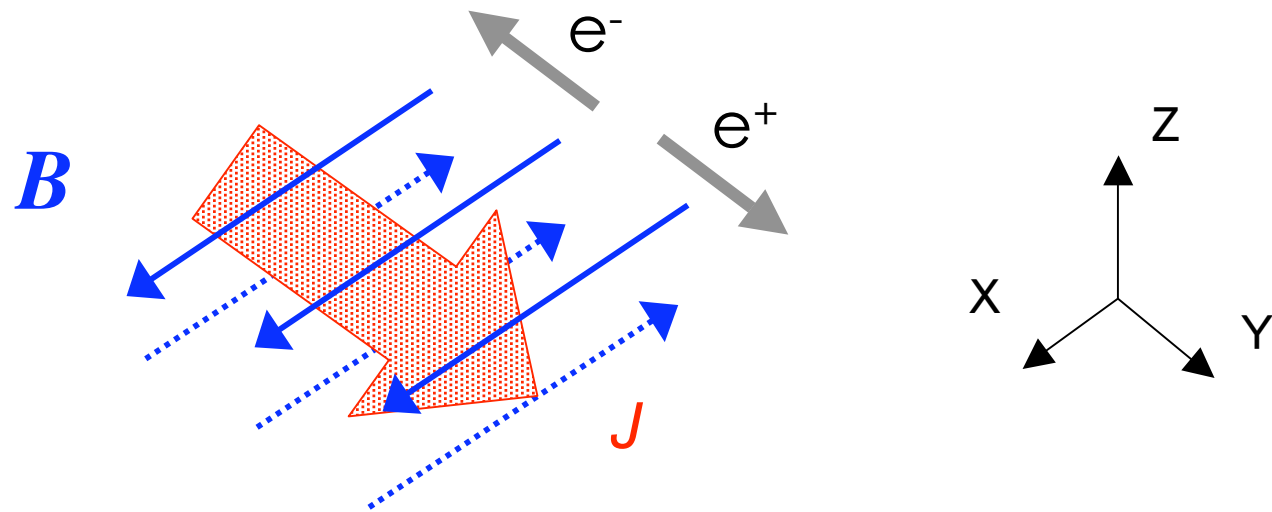
current sheets

magnetic field lines

e<sup>+</sup>, e<sup>-</sup> flow

# Basic processes in a relativistic current sheet

# Relativistic Current Sheet (RCS)

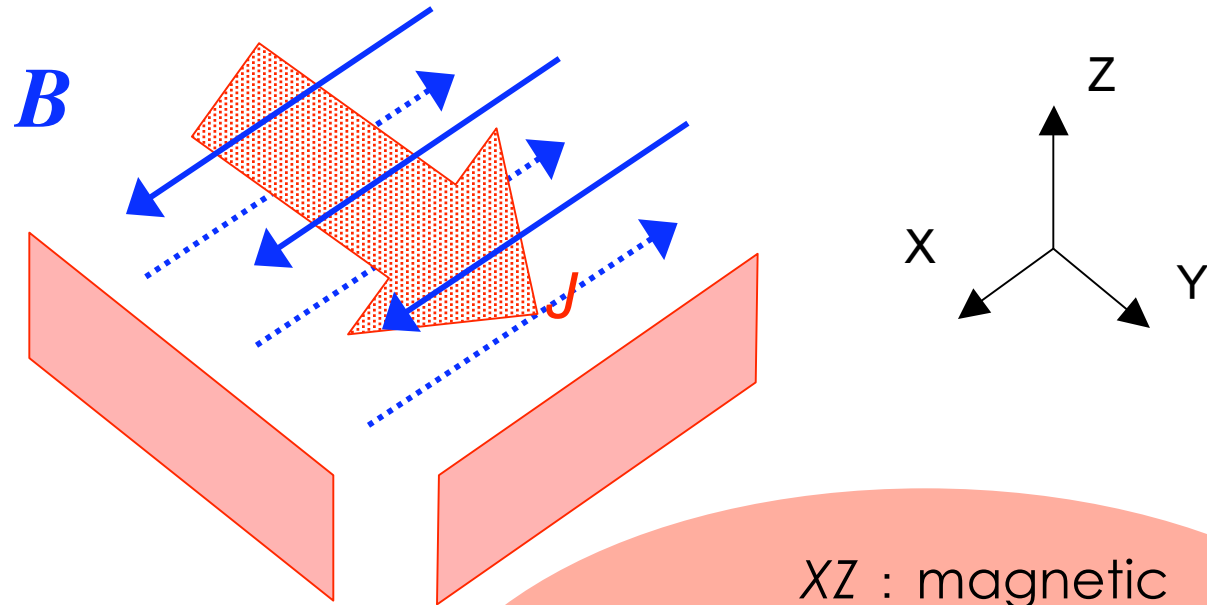


- Antiparallel magnetic field lines
- Dense plasma current sheet at the center
- Current : the counter-streaming of electrons and positrons
- Relativity :  $T \sim mc^2$ ,  $c_A \sim c$
- Relativistic Harris model (Hoh 1966, Kirk & Skjaeraasen 2003)

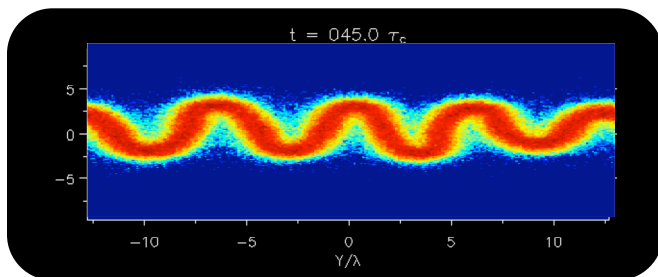
$$B = B_0 \tanh(z/\lambda) \hat{x}$$

$$f_s = \frac{n_0}{4\pi m^2 c T K_2(mc^2/T)} \cosh^{-2}(z/\lambda) \exp \left[ - \frac{\gamma_s (\varepsilon - \beta_s m c u_y)}{T} \right]$$

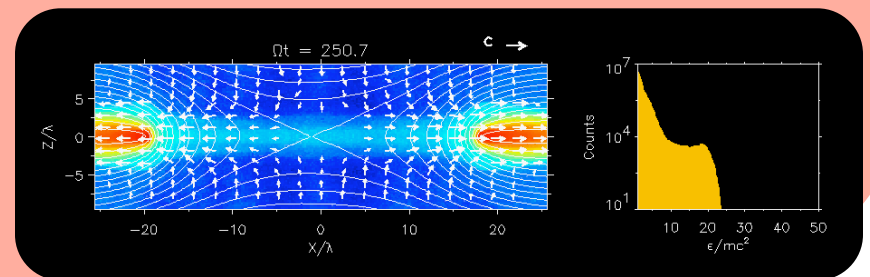
# Magnetic Reconnection (RX)



YZ : drift kink instability (DKI)

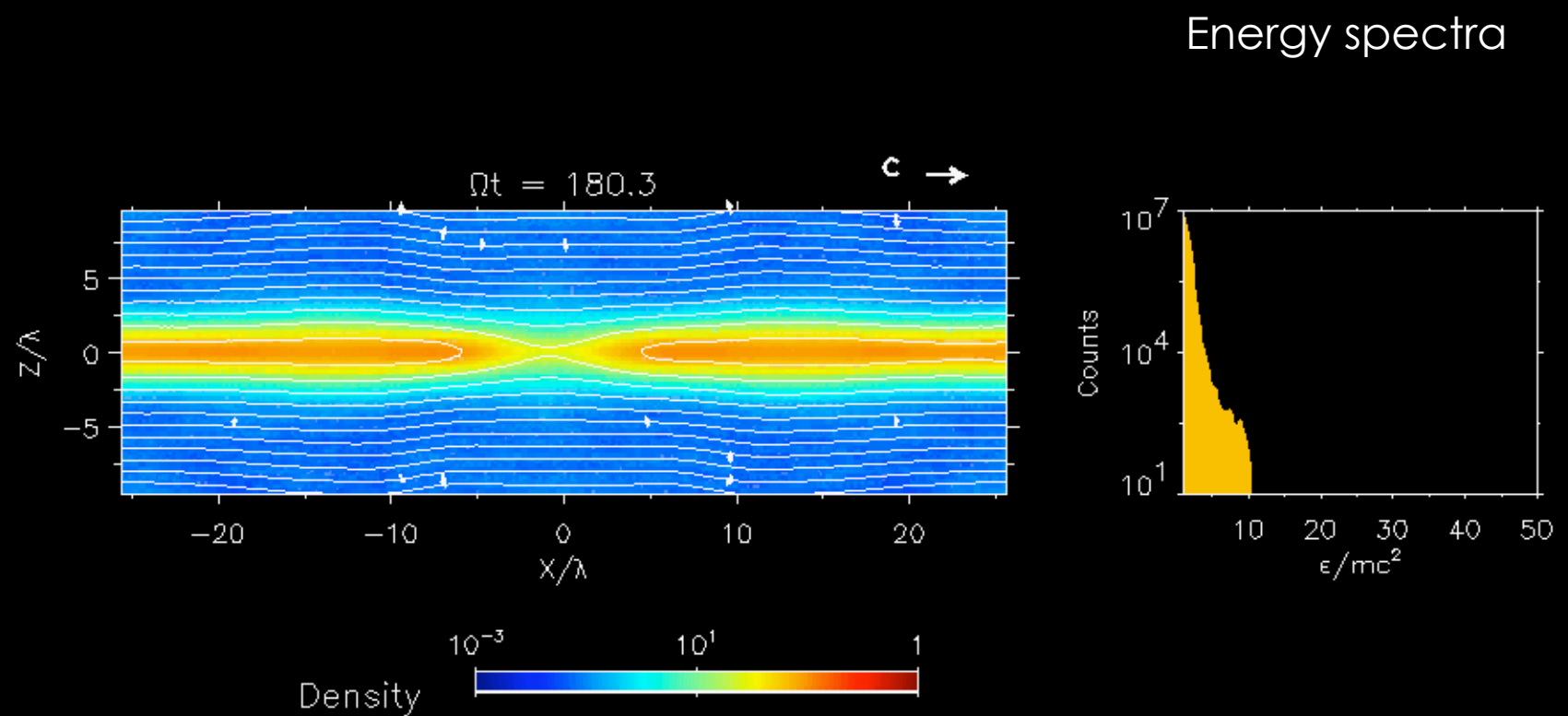


XZ : magnetic reconnection (RX)



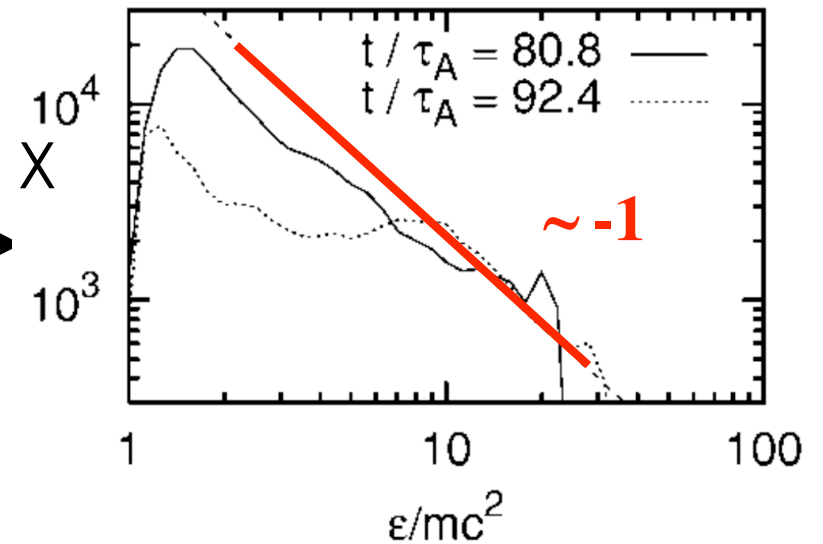
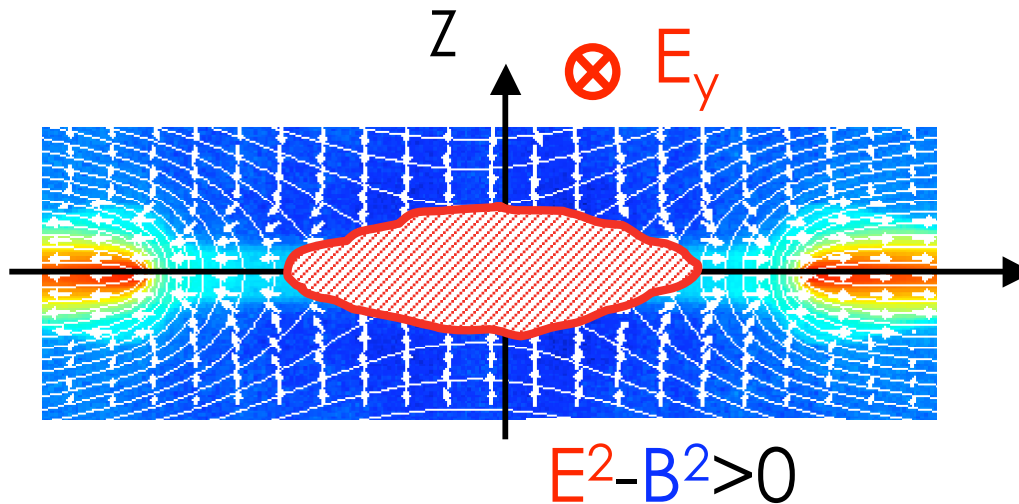
# 2D PIC simulation

- Fast reconnection occurs
- Particle acceleration around the X-region

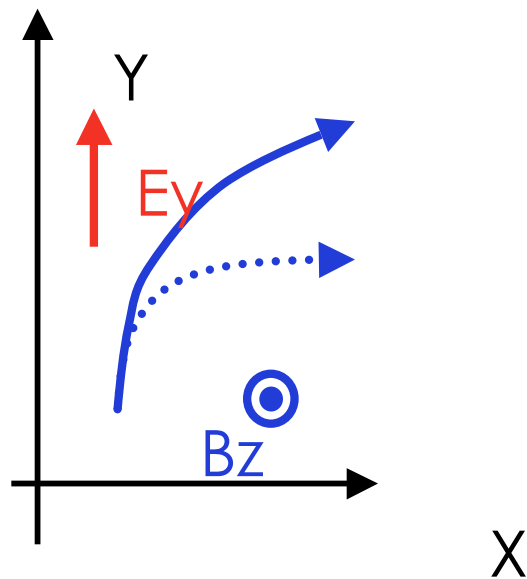




# DC particle acceleration



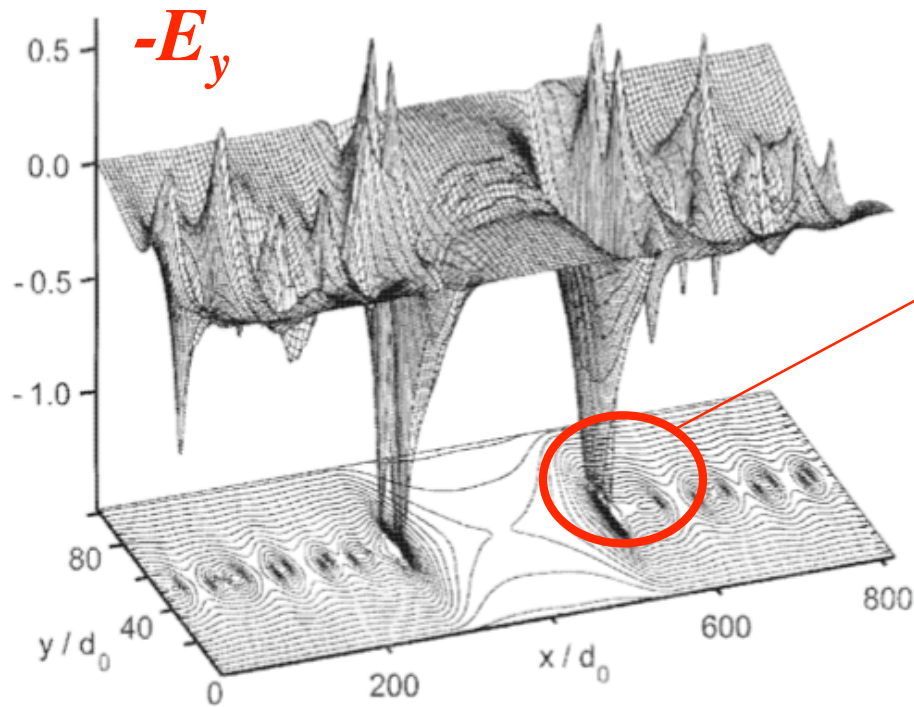
Zenitani & Hoshino 2001 ApJ



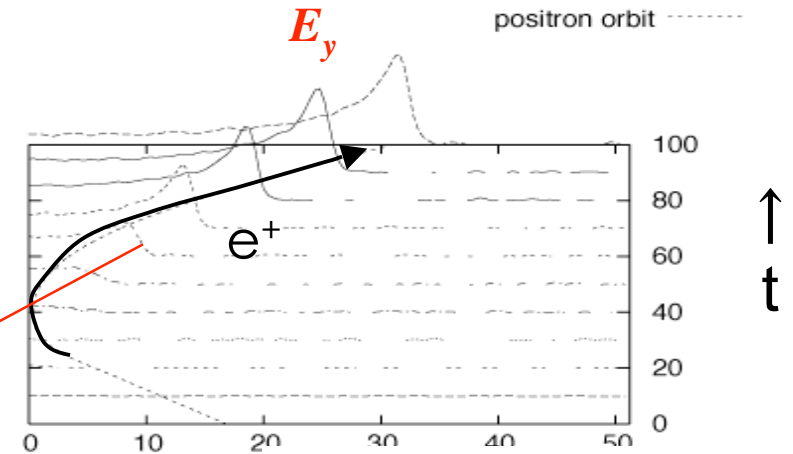
Trapping condition  
 ~ Gyro motion by  $B_z$  (Speiser orbit)  
 ==> extended in the  $Y$  direction

$$r_L \approx \frac{c}{\omega_C} = \frac{\gamma m_0 c^2}{e B_Z} \propto \varepsilon$$

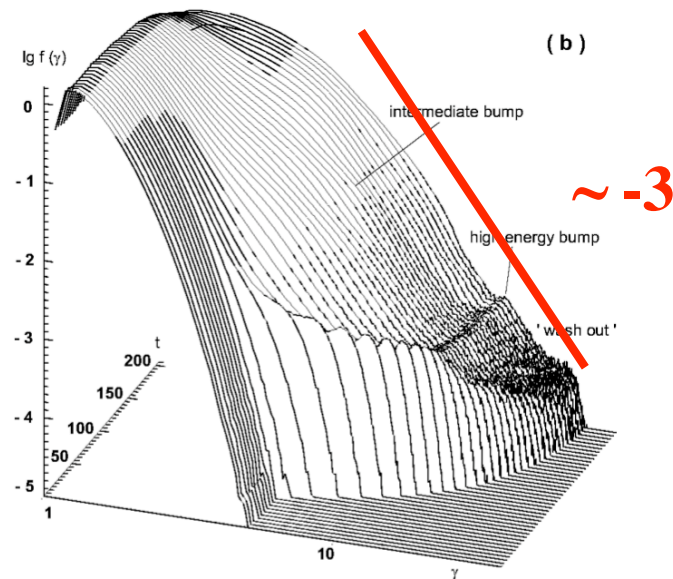
# Large-scale dynamic evolution



Jaroschek et al. 2004 ApJ



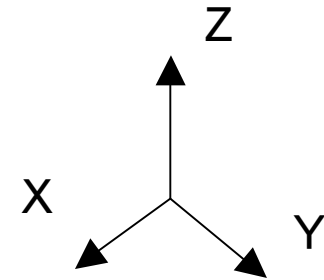
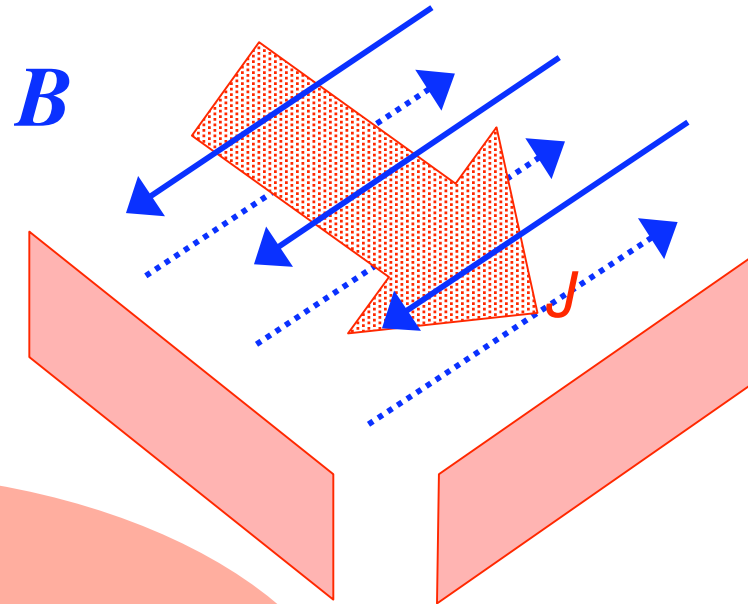
Zenitani & Hoshino 2007 ApJ



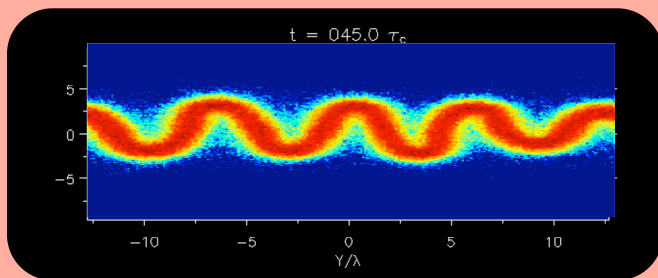
Jaroschek et al. 2004 Phys. Plasmas

- Powerful motional electric fields at multiple magnetic islands
- Entire acceleration mechanism: not yet well understood

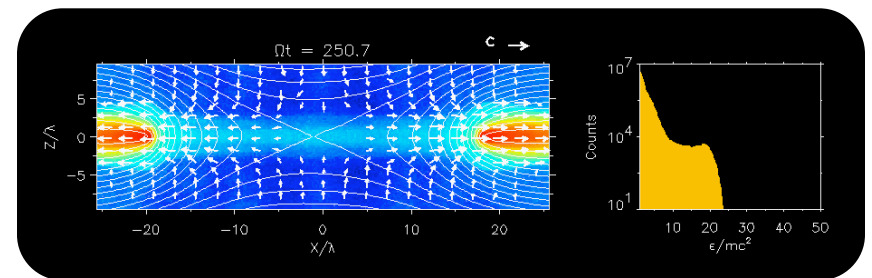
# Drift Kink Instability (DKI)



YZ : drift kink instability (DKI)

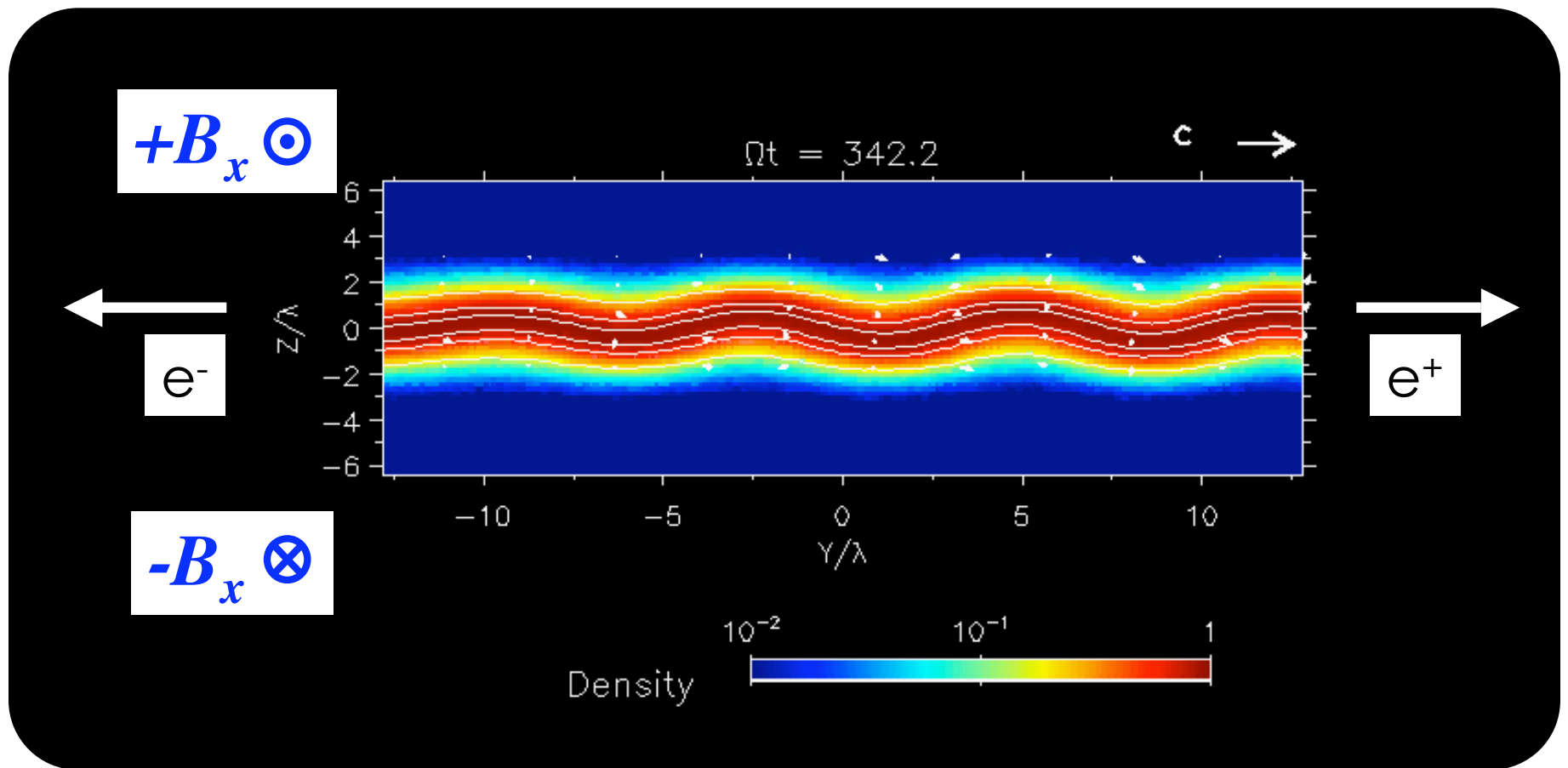


XZ : magnetic reconnection (RX)



# 2D PIC simulation

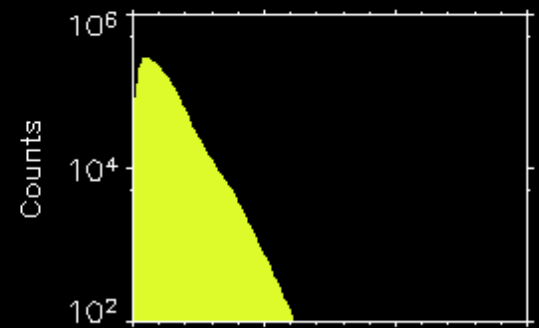
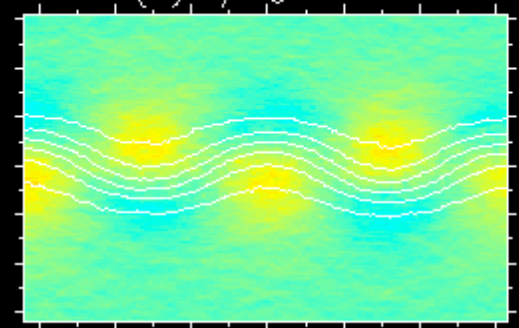
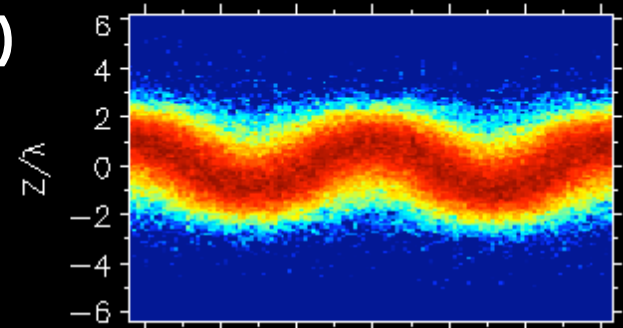
- A kink-type instability, driven by the electron-positron counter-streaming (Zhu & Winglee 1996 JGR, Ozaki et al. 1996 Phys. Plasmas, Pritchett et al 1996 JGR, Daughton 1999 Phys. Plasmas)



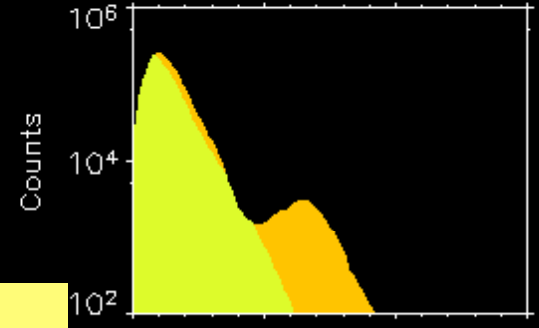
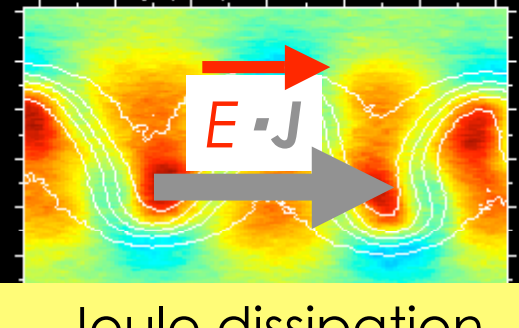
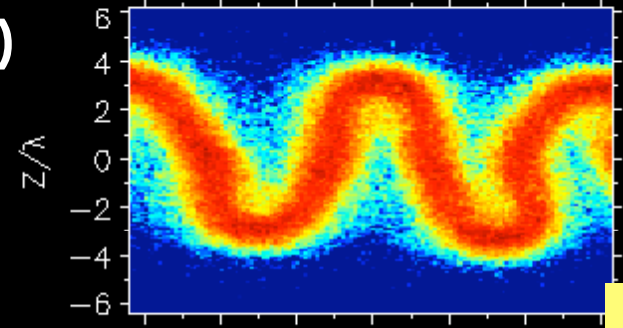
Electric field

Energy spectra

(1)

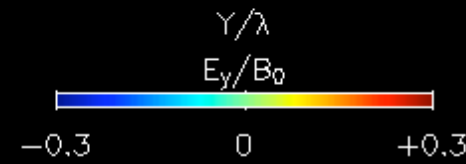
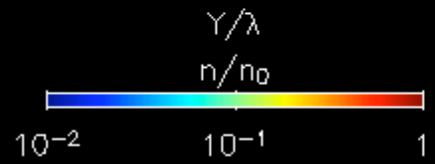
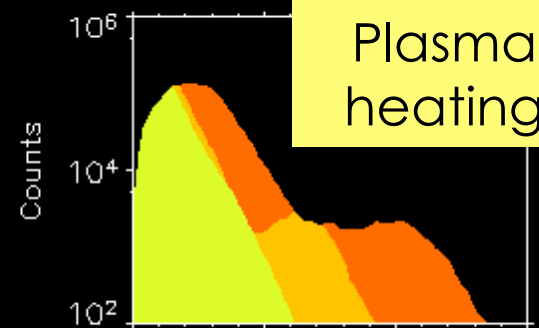
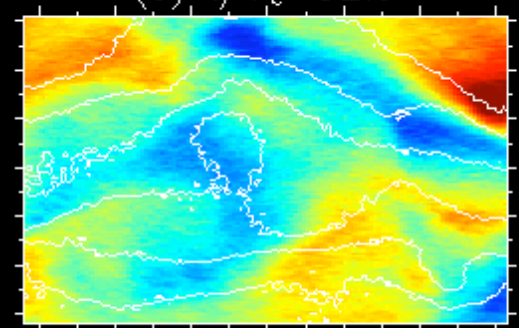
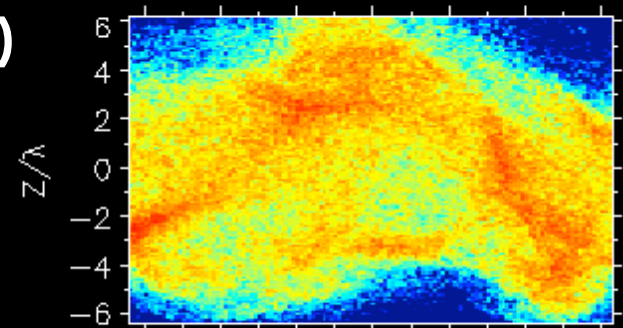


(2)



Joule dissipation

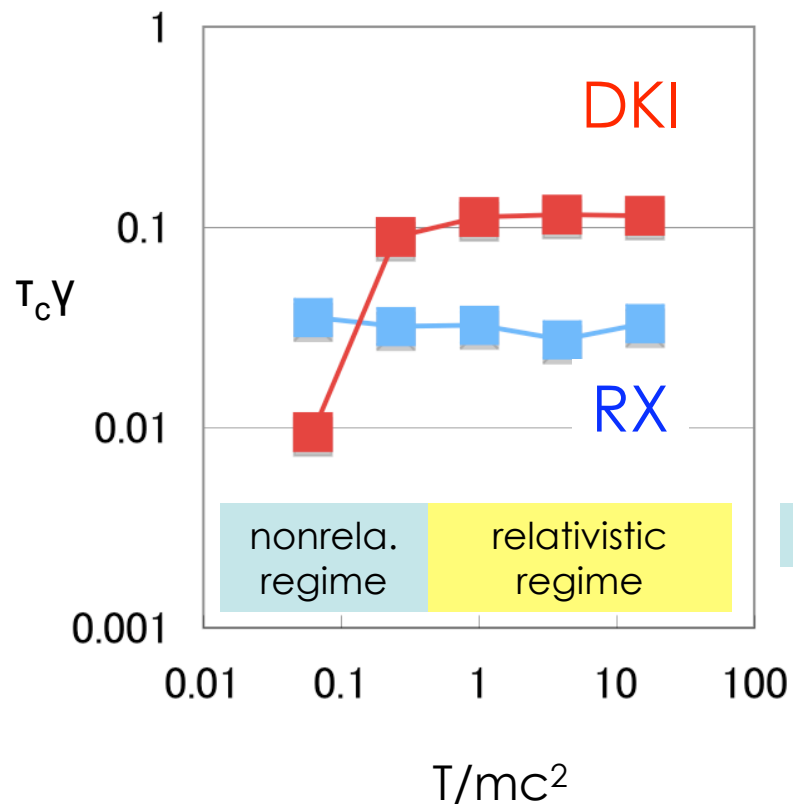
(3)



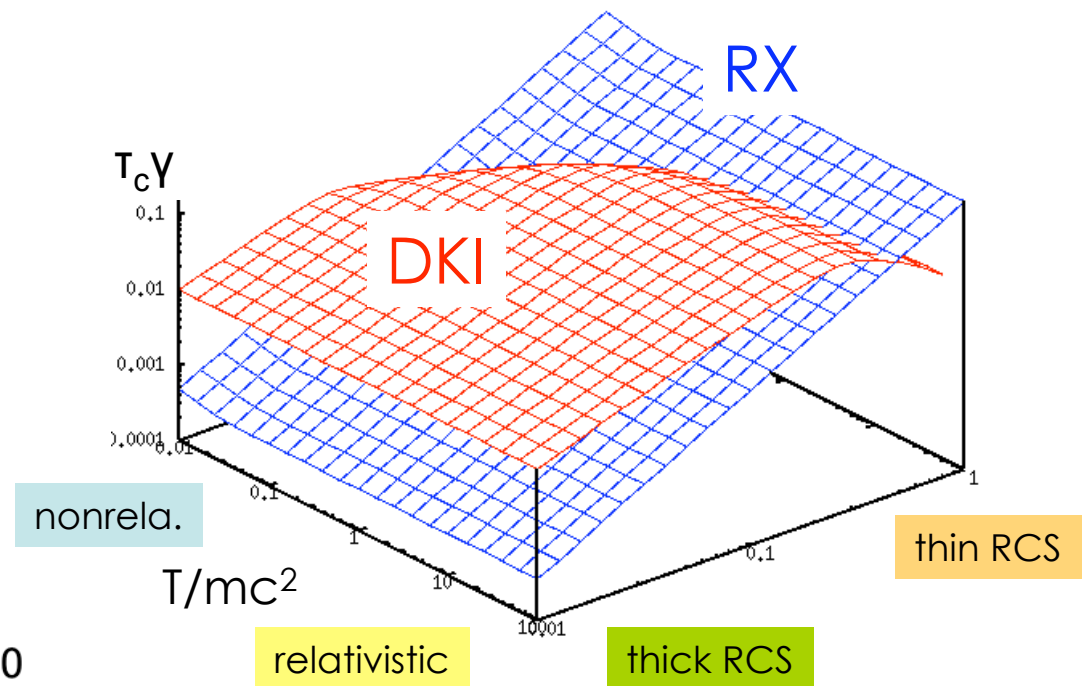
# Two competing modes

**RX** (nonthermal acceleration) vs **DKI** (plasma heating).  
In the relativistic regime, **DKI** grows faster.

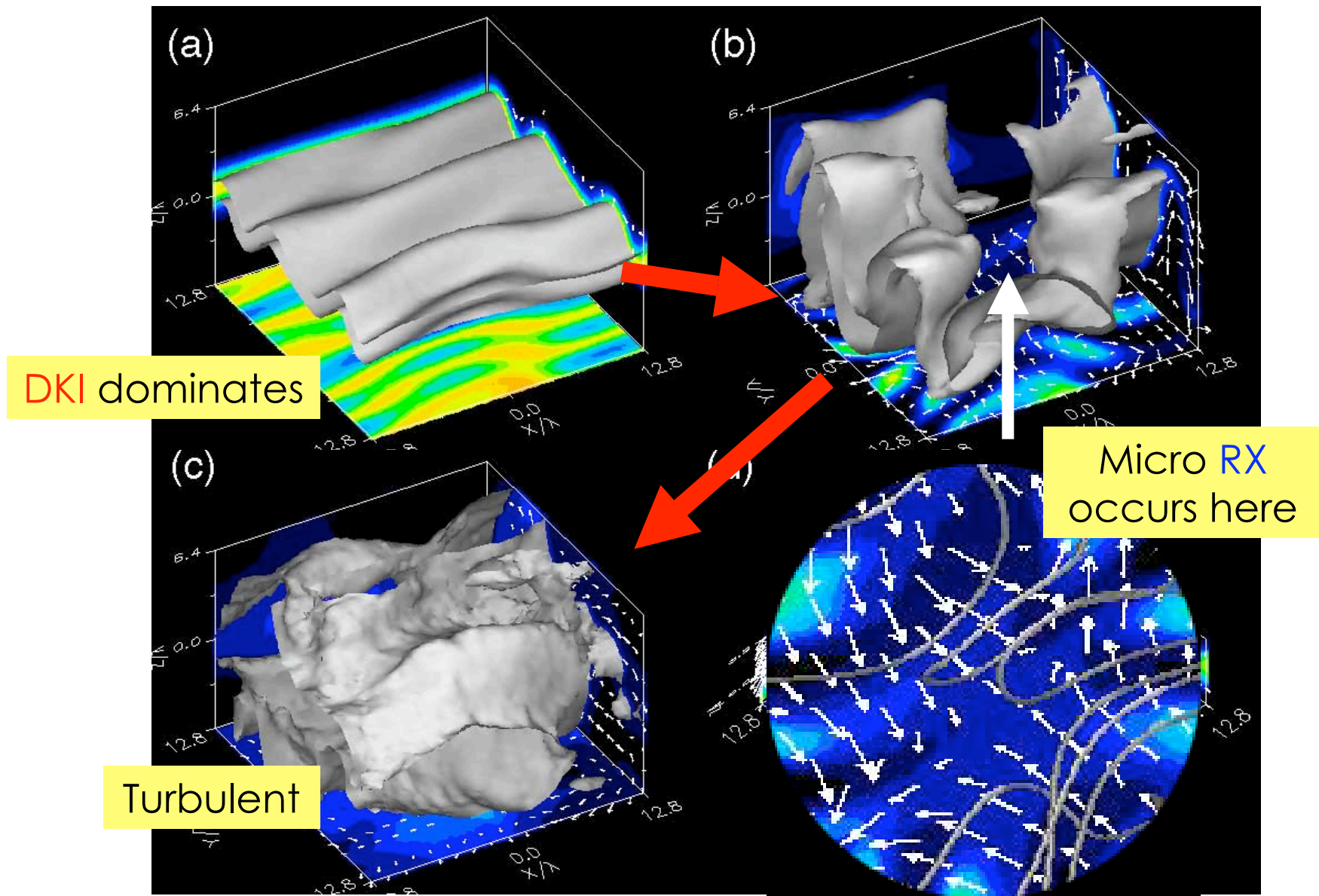
- PIC simulation



- Analytical estimate



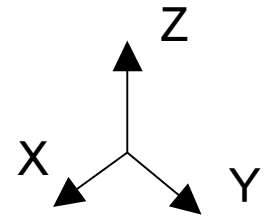
# 3D evolution



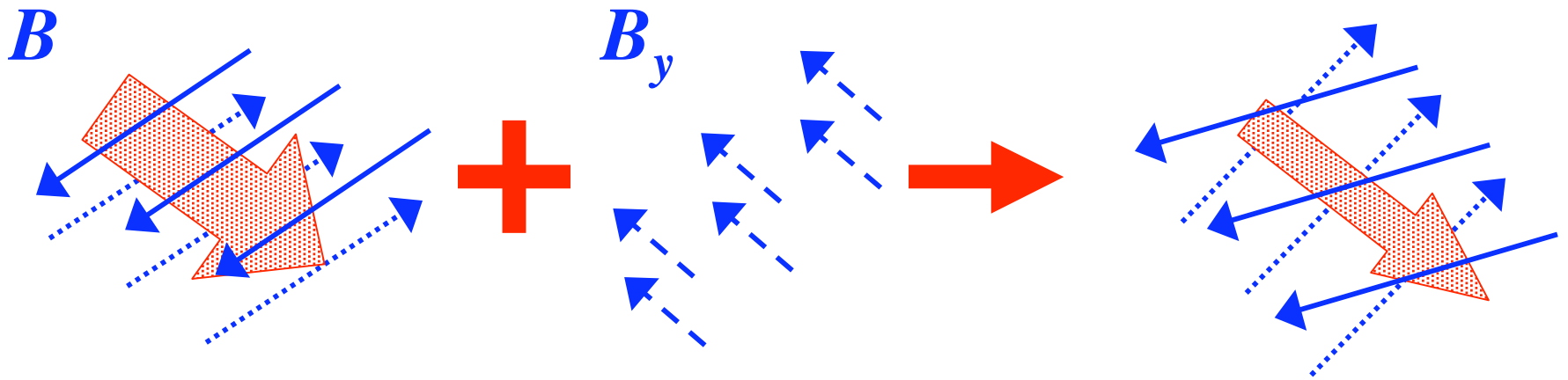
Guide field case



# The Guide field ( $B_y$ )

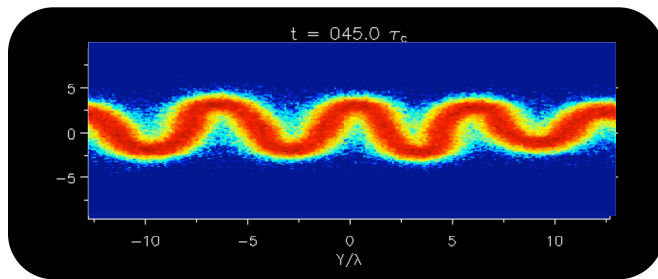


- Harris field + Uniform  $B_y$  = Twisted equilibrium

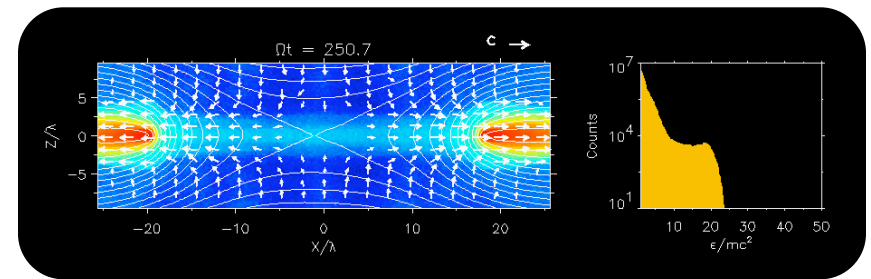


YZ : drift kink instability (DKI)

XZ : magnetic reconnection (RX)



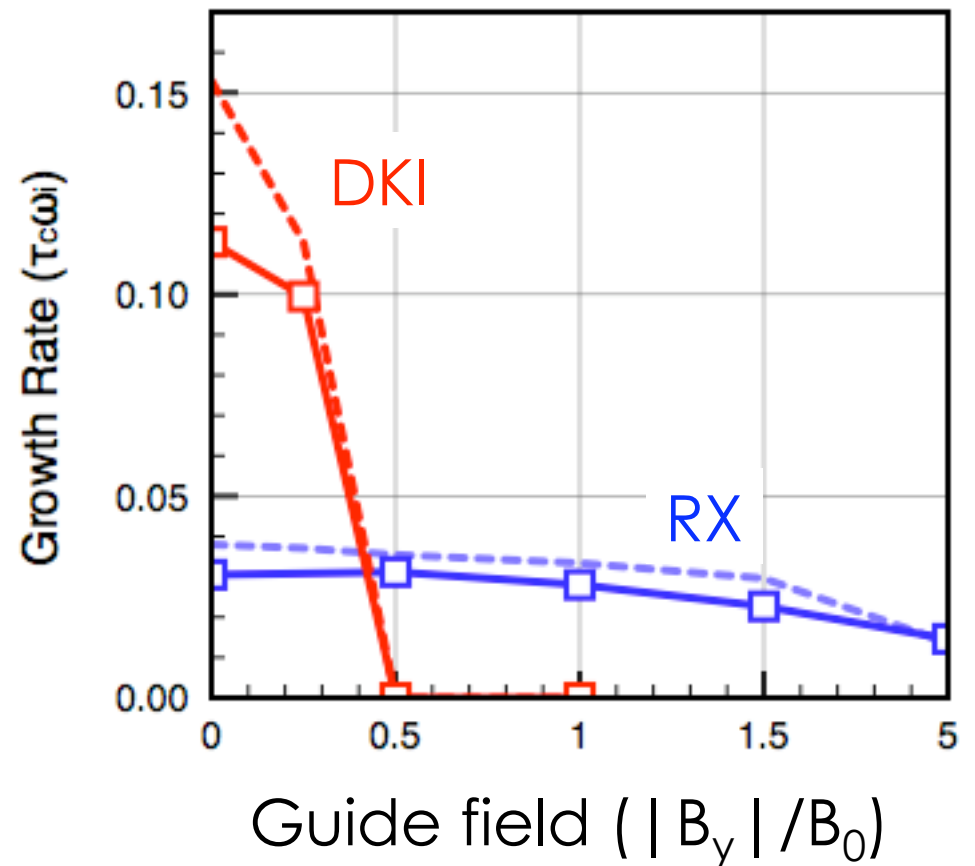
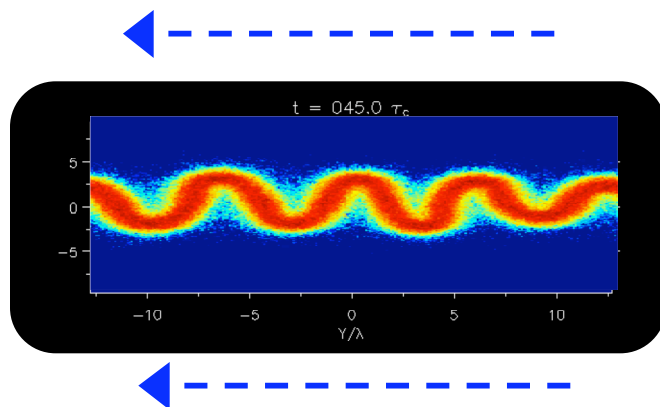
←  $B$



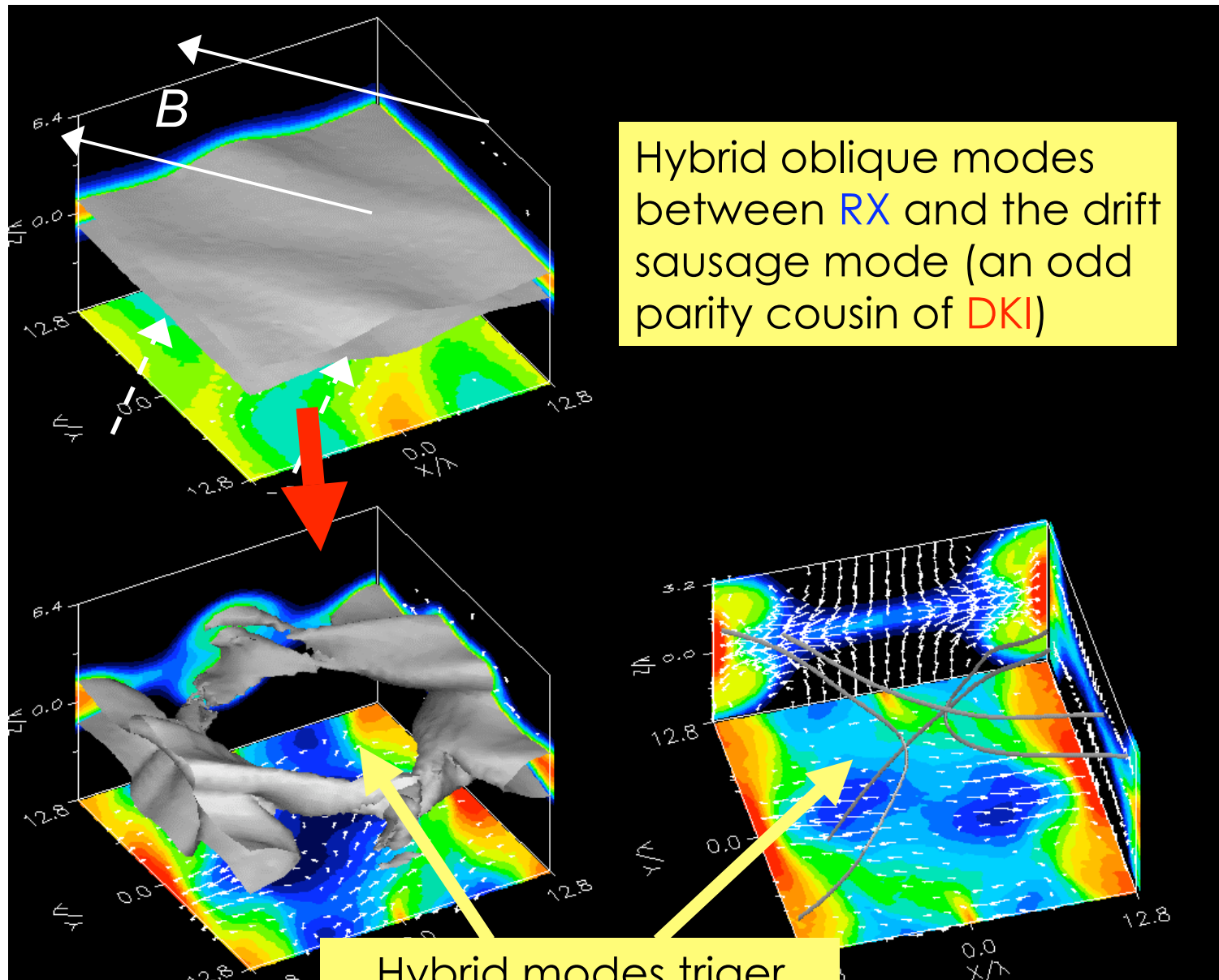
$B \otimes \otimes$

# Growth rate: guide field dependency

- **RX** is insensitive
- **DKI** is stabilized by the magnetic tension
- We expect that **RX** dominates in 3D



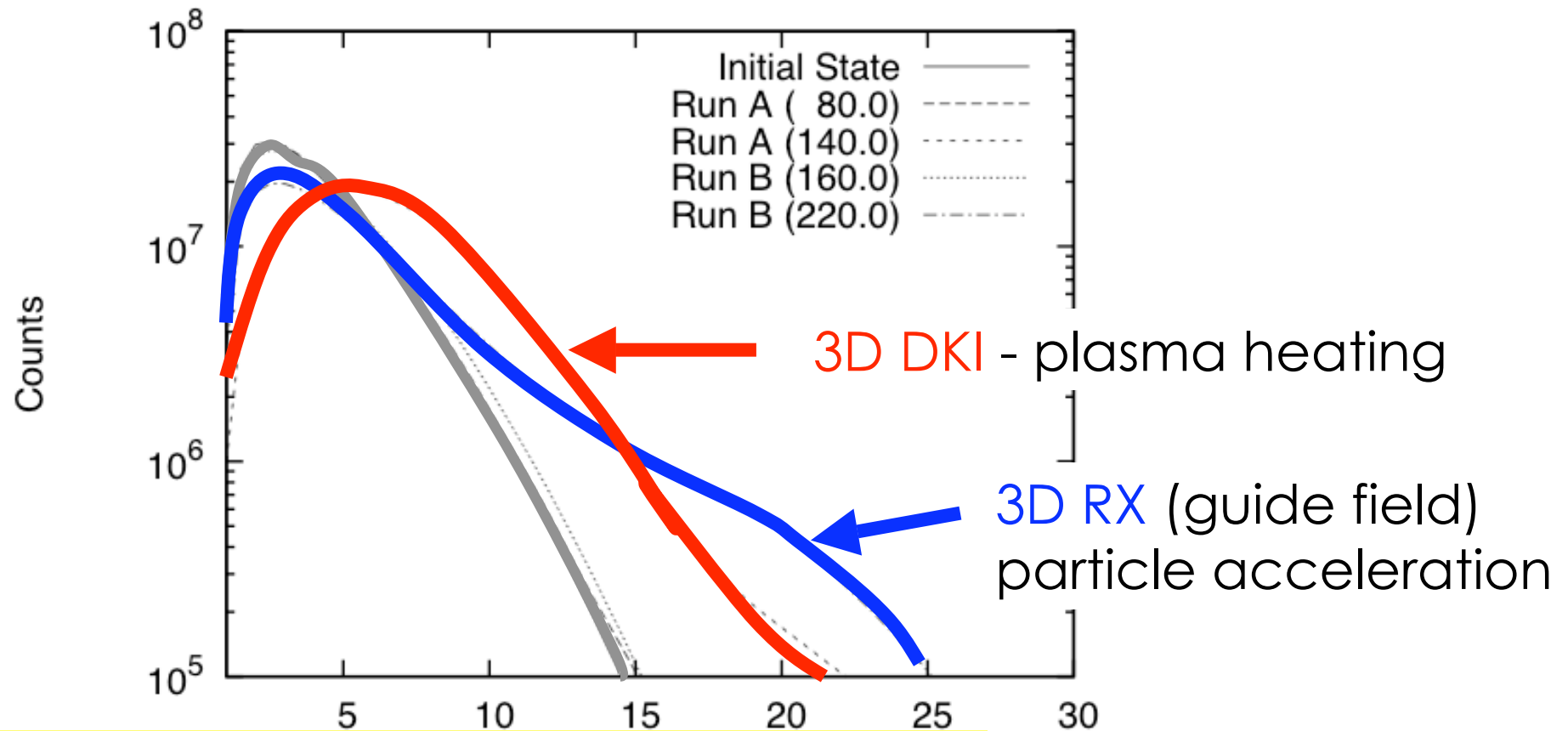
# 3D evolution with guide field



Hybrid oblique modes between RX and the drift sausage mode (an odd parity cousin of DKI)

Hybrid modes trigger secondary RX

# Energy distribution

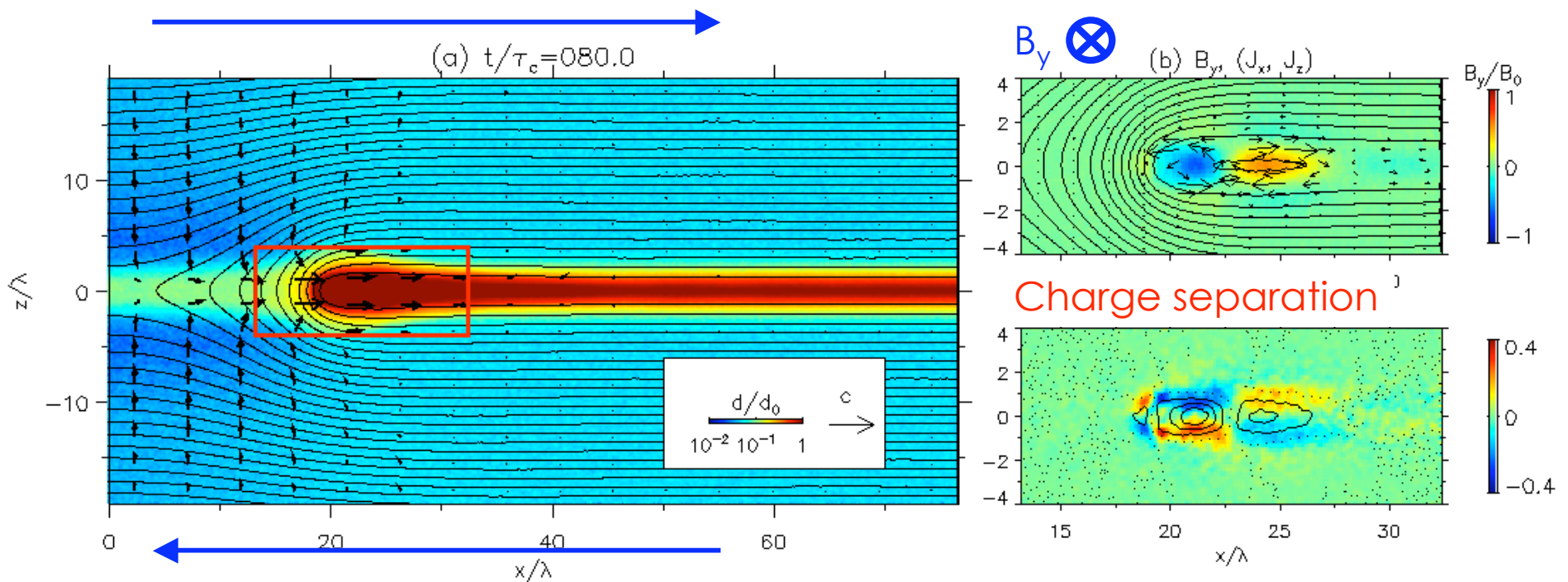


Magnetic topology changes  
the destination of released energy;  
plasma heat or non-thermal energy.

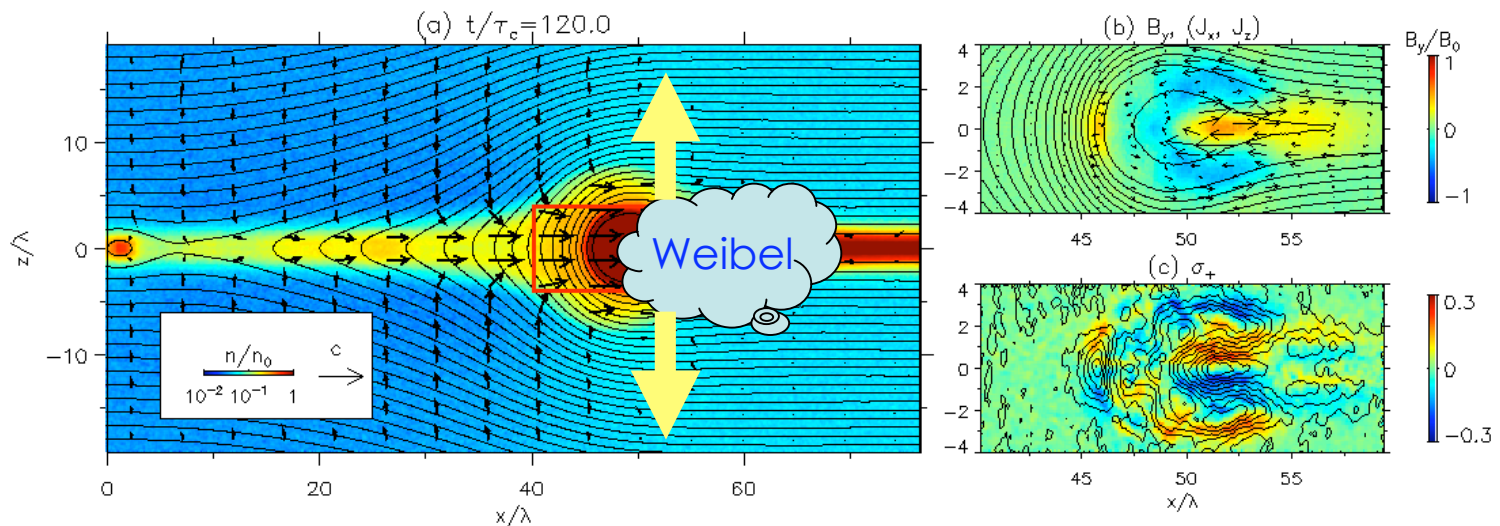
Recent discovery:  
Weibel instability

# Weibel-type instability in reconnection

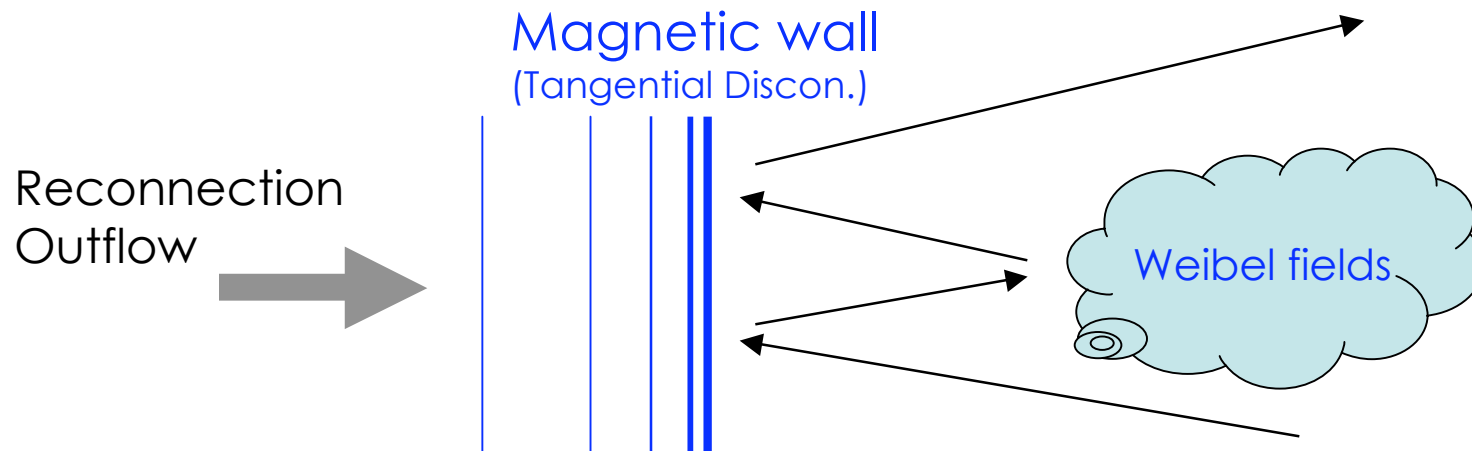
- Anisotropy-driven Weibel instability (WBI) generates out-of-plane magnetic field at the outflow jet front
- Small scale mode of ( $L \sim \gamma^{1/2} c / \omega_p$ )



- The **WBI** quickly widens the magnetic island



- The **WBI** works as a shock-downstream scatterer



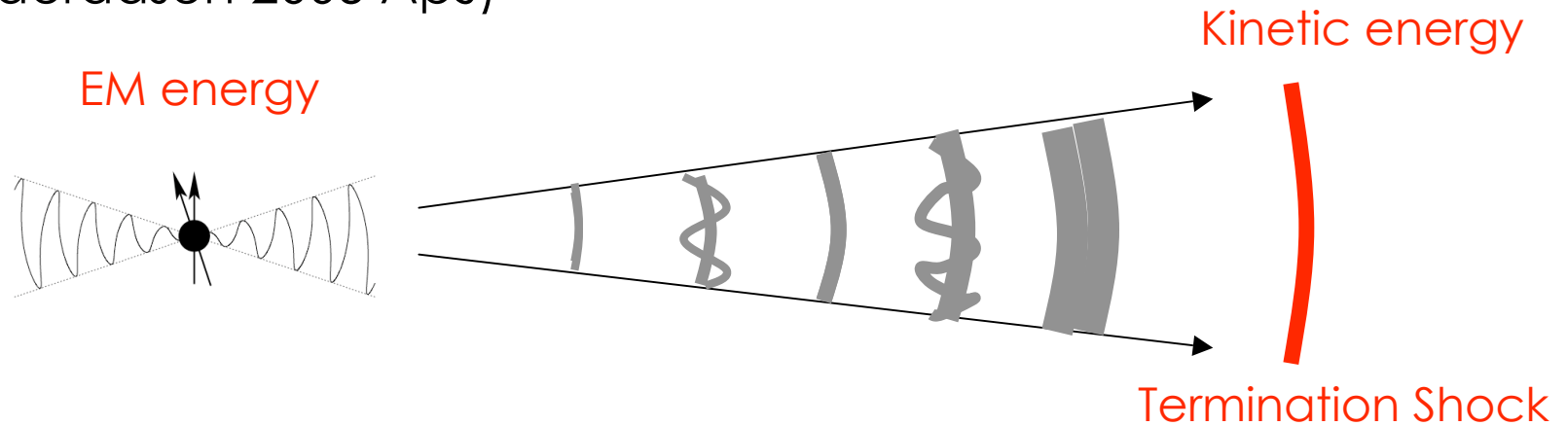
- The **WBI** seems to be universal (Nonrelativistic case; Swisdak's Talk)

# Discussions



# On the dissipation problem

- Radial 1D flow model (Lyubarsky & Kirk 2001 ApJ, Kirk & Skjaeraasen 2003 ApJ)



- A realistic rate by **RX** (the collisionless tearing mode; Zelenyi & Krasnosel'skikh 1979)

$$\beta_{RTI} = \tau_c \gamma_{RTI} = \beta^{3/2}$$

- The **DKI** will give better dissipation

$$\beta_{RDKI} \sim \beta > \beta_{RTI}$$

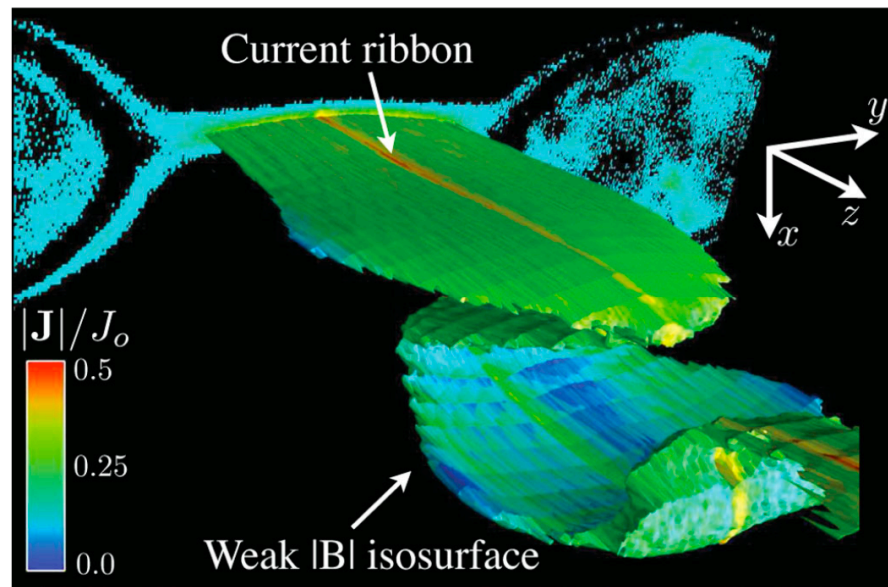
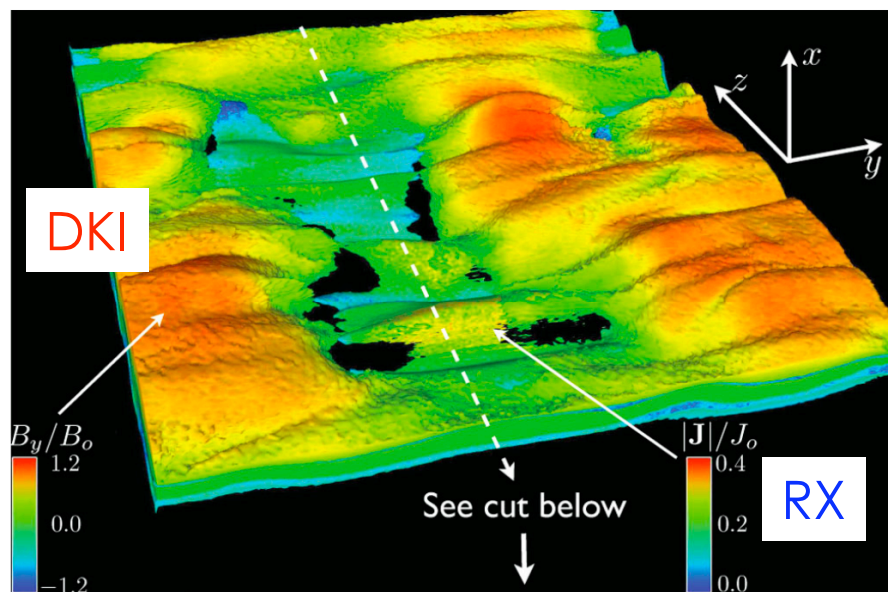
- Dissipation & particle acceleration at the shock

- Lyubarsky 2005 MNRAS, Pétri & Lyubarsky 2007 A&A, Nagata et al. 2008 ApJ

- 2D/3D instabilities would enhance magnetic dissipation - even when  $(r_L/L) \sim O(0.1)$ , 2D instabilities grows fast in such a thin RCS

# Large scale PIC simulation

- 3D evolution in a nonrelativistic pair plasma is more dynamic than expected
- **DKI** saturates, **RX** grows, and again kink-like mode in the thin reconnection CS
- At least the linear physics would be similar



Lin et al 2008 PRL

Large-scale evolution of RCS remains unclear  
It should be checked by large-scale PIC simulation

# Spectral index

- Magnetic reconnection
  - Acceleration region ---  $s \sim 1.x$ 
    - Theory: Romanova & Loverace 1992 A&A, Larrabee et al. 2003 ApJ
    - PIC: Zenitani & Hoshino 2001 ApJ
  - Universal index ---  $s \sim 3$  (2.x)
    - PIC: Jaroschek et al. 2004 Phys. Plasmas, Zenitani & Hoshino 2007, 2008 ApJ, Bessho & Battarachee 2007 Phys. Plasmas, Karlíky 2008 ApJ
    - Moderate guide field may make it harder
  - Further enhanced in pulsar-wind driven configuration
    - Lyubarsky & Liverts 2008 ApJ
- 1D RCS problem
  - Nonadiabatic acceleration in an individual RCS :  $s=2-4$ 
    - Jaroschek et al. 2008 Adv. Space. Res.
  - Shock - RCSs interaction :  $s=4$ 
    - Nagata et al. 2008 ApJ

# Large-scale MHD evolution of RCS

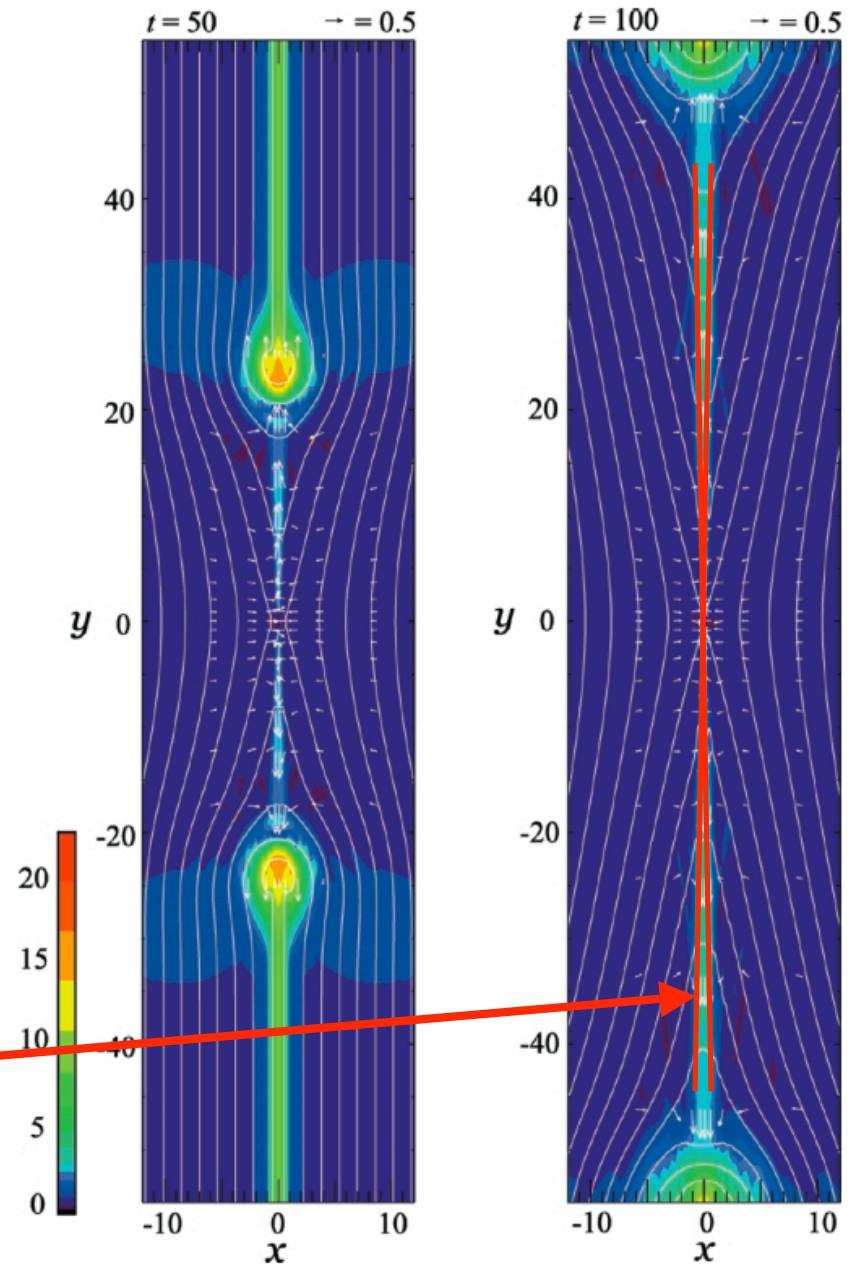
Beyond the kinetic scale ...

# Resistive RMHD reconnection

- RCS processes dissipate magnetic energy
- Limited number of resistive relativistic MHD (RMHD) studies
- Watanabe & Yokoyama 2006 ApJ
  - Relativistic resistive MHD simulation in weakly magnetized regime
  - Ohm's law: localized resistivity at

$$\gamma \left( \mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right) = \eta \left[ \mathbf{j} + \gamma^2 \left( \mathbf{j} \cdot \frac{\mathbf{v}}{c} - \rho_e c \right) \frac{\mathbf{v}}{c} \right]$$

- Petschek reconnection with a pair of slow shocks



Watanabe & Yokoyama 2006 ApJ

# Two-fluid RMHD reconnection (1)

$$\frac{\partial d_p}{\partial t} = \frac{\partial}{\partial t} \gamma_p n_p = -\nabla \cdot (n_p \mathbf{u}_p) \quad (1)$$

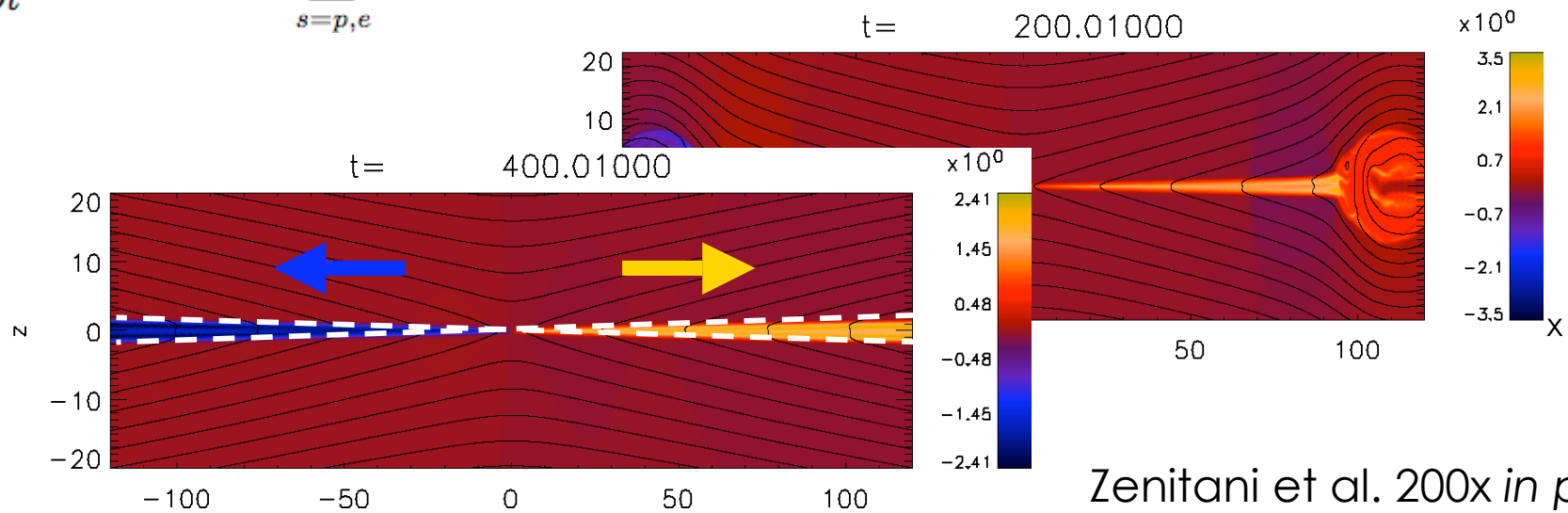
$$\frac{\partial \mathbf{m}_p}{\partial t} = \frac{\partial}{\partial t} \gamma_p w_p \mathbf{u}_p = -\nabla \cdot (w_p \mathbf{u}_p \mathbf{u}_p + \delta_{ij} p_p) + \gamma_p n_p q_p (\mathbf{E} + \mathbf{v}_p \times \mathbf{B}) - \tau_{fr} d_p d_e (\mathbf{v}_p - \mathbf{v}_e) \quad (2)$$

$$\frac{\partial K_p}{\partial t} = \frac{\partial}{\partial t} (\gamma_p^2 w_p - p_p - d_p m c^2) = -\nabla \cdot (\gamma_p w_p \mathbf{u}_p - n_p m c^2 \mathbf{u}_p) + \gamma_p n_p q_p (\mathbf{v}_p \cdot \mathbf{E}) + \eta_{eff} \mathbf{j} \cdot \mathbf{j} \quad (4)$$

$$\frac{\partial \mathbf{B}}{\partial t} = -c \nabla \times \mathbf{E} \quad (5)$$

$$\frac{\partial \mathbf{E}}{\partial t} = c \nabla \times \mathbf{B} - 4\pi \sum_{s=p,e} q_s n_s \mathbf{u}_s \quad (6)$$

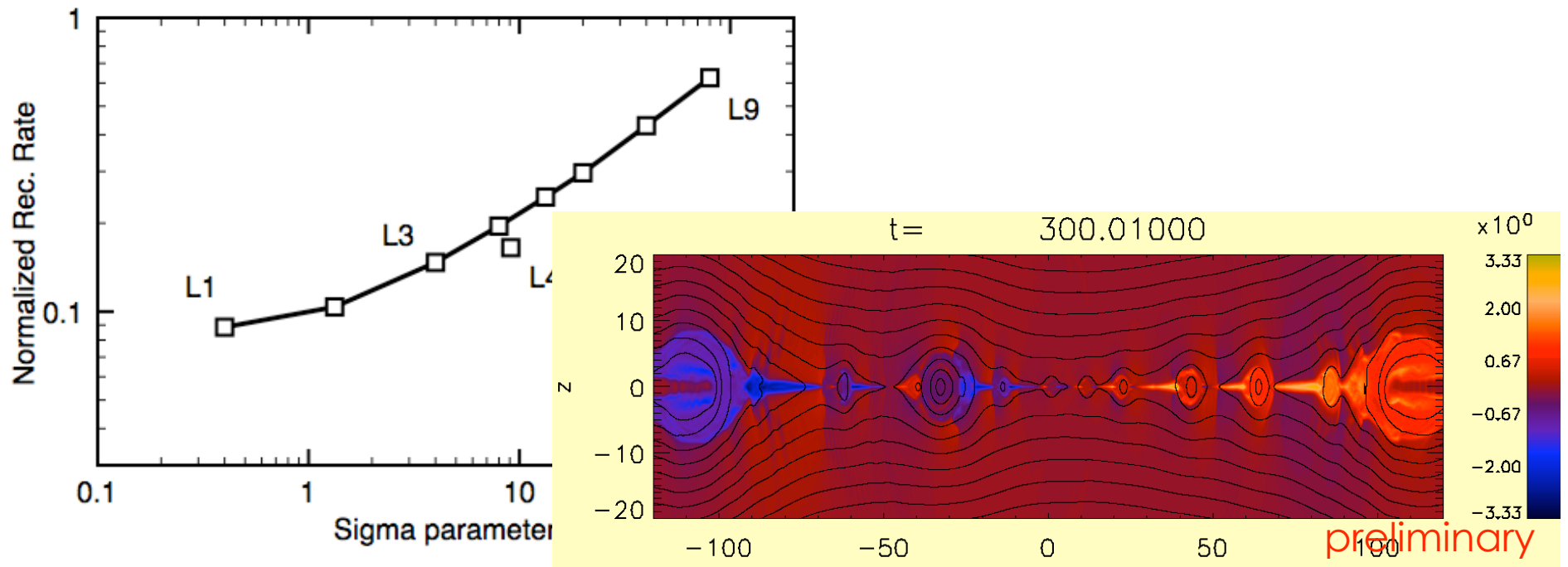
- Independent electron-positron motion
- Resistivity = an inter-species friction force
- Localized resistivity profile



Zenitani et al. 200x in prep

## Two-fluid RMHD reconnection (2)

- When the inflow is more magnetic-dominated, we observe Sweet-Parker-type fast reconnection of the rate  $\sim 1$ .



- The system evolution highly depends on the resistivity profile, which essentially comes from the small-scale kinetic physics.
- RMHD + kinetic joint study required.

# Summary

- Basic instabilities in RCS
  - Magnetic Reconnection (**RX**; nonthermal acceleration)
  - Relativistic Drift Kink Instability (**DKI**; plasma heating)
  - Hybrid oblique modes
  - The Weibel Instability (**WBI**)
- RCS 3D evolution
  - Antiparallel : **RX** < **DKI** (?) → Plasma heating
  - Guide field : **RX** > **DKI** → Nonthermal acceleration
  
  - **DKI** will be the better dissipation mechanism
  - Power Law : universal index of  $s \sim 3$
  - RMHD simulation: important tools to study large-scale astrophysical problems, with PIC
- Open Questions (Next slide)



# Open questions

- Large scale kinetic evolution
- Large scale RMHD evolution, and its consistency with kinetic model
- RX
  - Acceleration rate or power-law index
  - Dependence to the upstream  $\sigma$
  - Origin of the resistivity, and how to scale it?
  - The steady reconnection model and its reconnection rate?
- DKI
  - Saturation mechanism
  - Compressed configuration
- and many more...
  - Radiative effect (→ Jaroschek's Talk)
  - Positron-ion-electron plasma

Dziękuję  
(Thank you!)