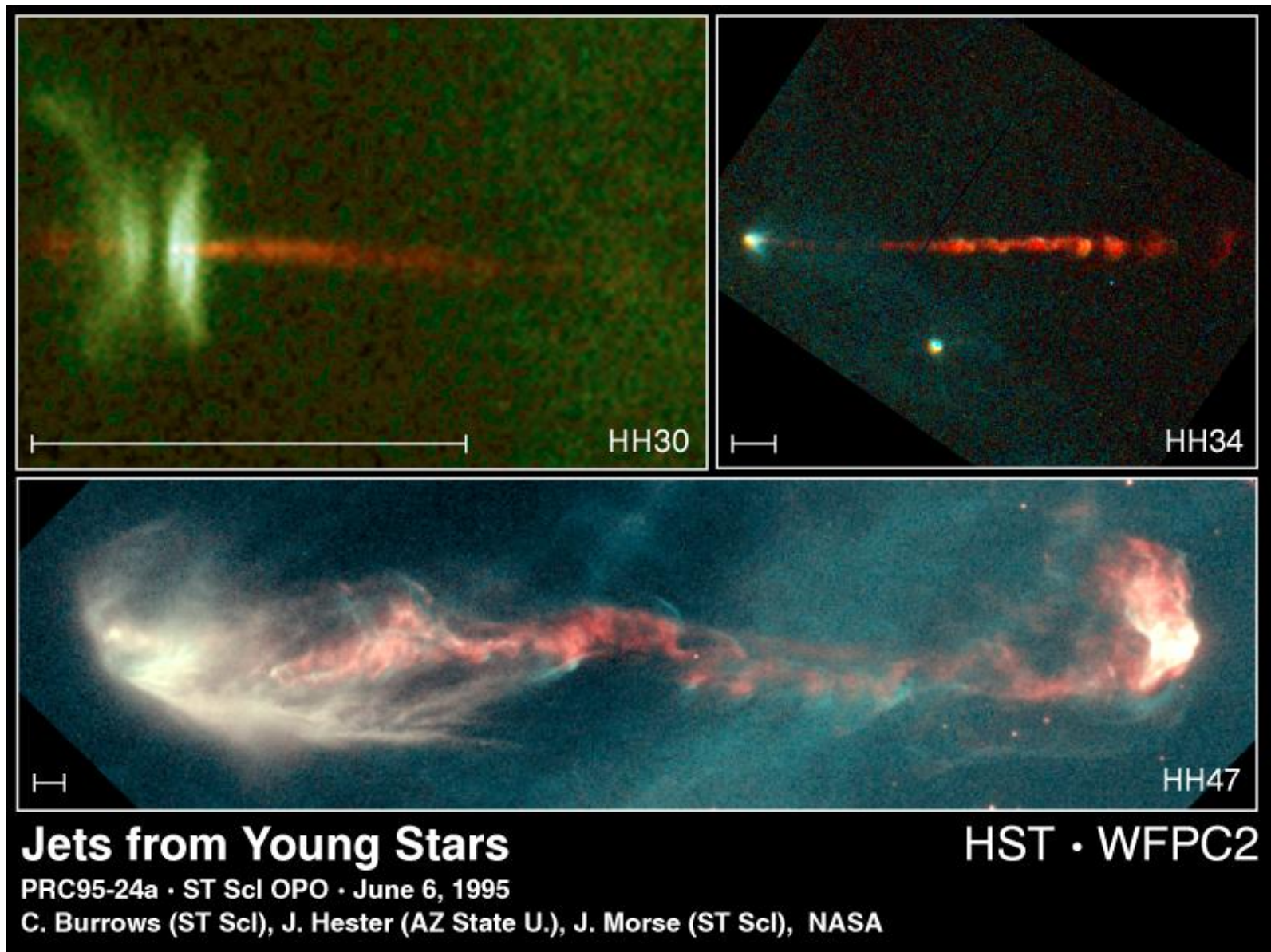


# Jet Driving in GRB Sources

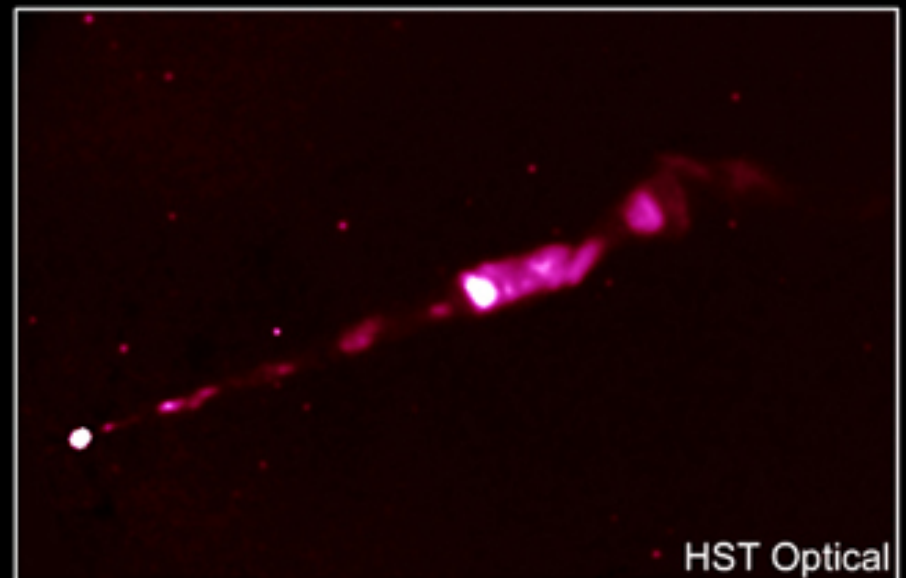
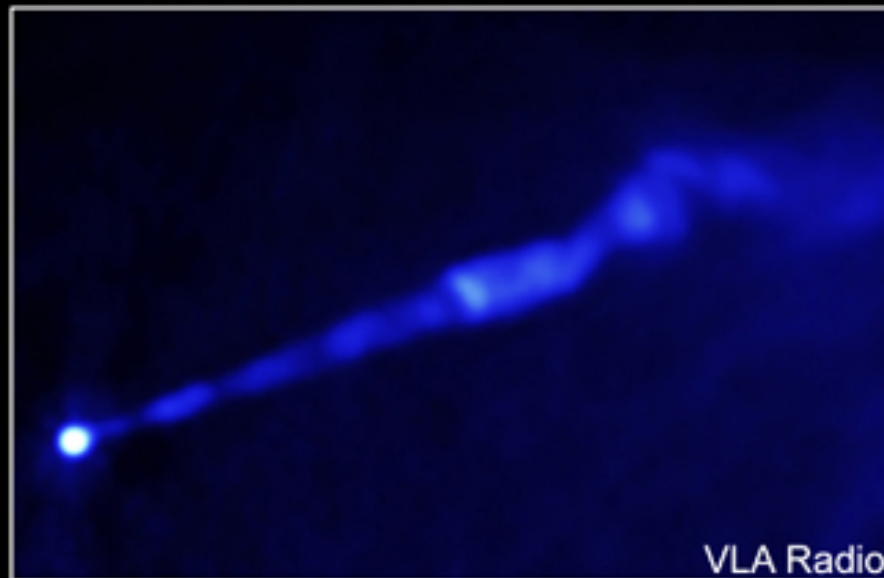
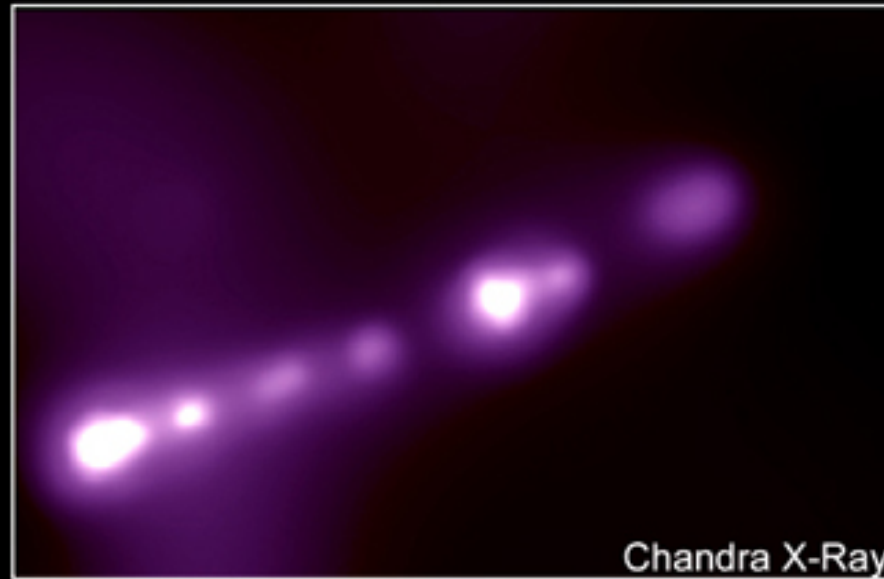
Nektarios Vlahakis  
University of Athens

## outline

- introduction: astrophysical jets
- the MHD description
  - acceleration
  - collimation
- alternatives



(scale = 1000 AU,  $V_{\infty} = \text{a few } 100 \text{ km/s}$ )



collimation at  $\sim 100$  Schwarzschild radii,  $\gamma_\infty \sim 10$

# GRBs

- ★ high Lorentz factors (compactness problem)
- ★ collimated outflows (energy reservoir, achromatic afterglow breaks)

# GRBs

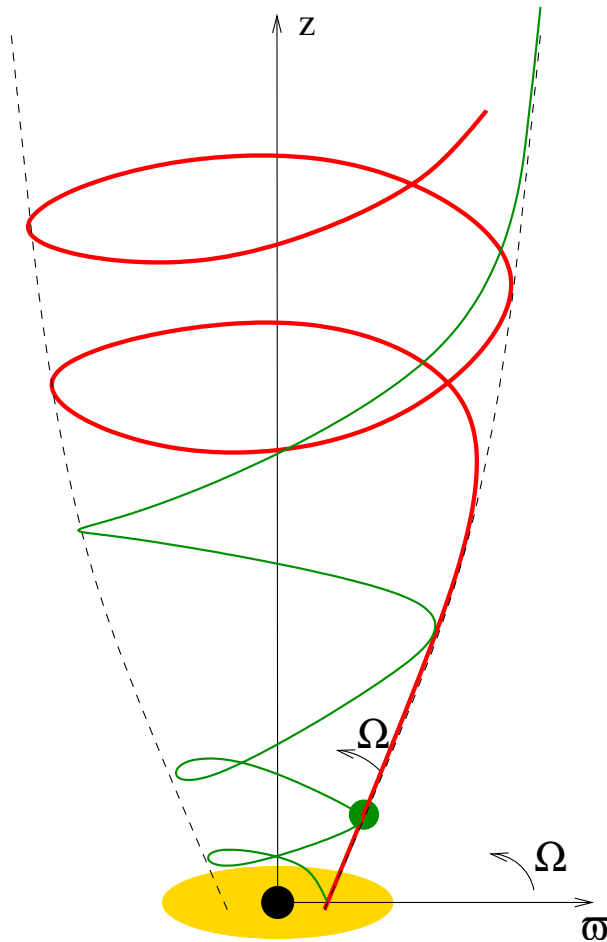
- ★ high Lorentz factors (compactness problem)
  - ★ collimated outflows (energy reservoir, achromatic afterglow breaks)
- 
- ☞ similar characteristics
  - ☞ MHD offers a unified picture

# We need magnetic fields

- ★ to extract energy (Poynting flux)
- ★ to extract angular momentum
- ★ to transfer energy and angular momentum to matter
- ★ to collimate outflows and produce jets
- ★ for synchrotron emission
- ★ to explain polarization maps

# The structure of a magnetized outflow

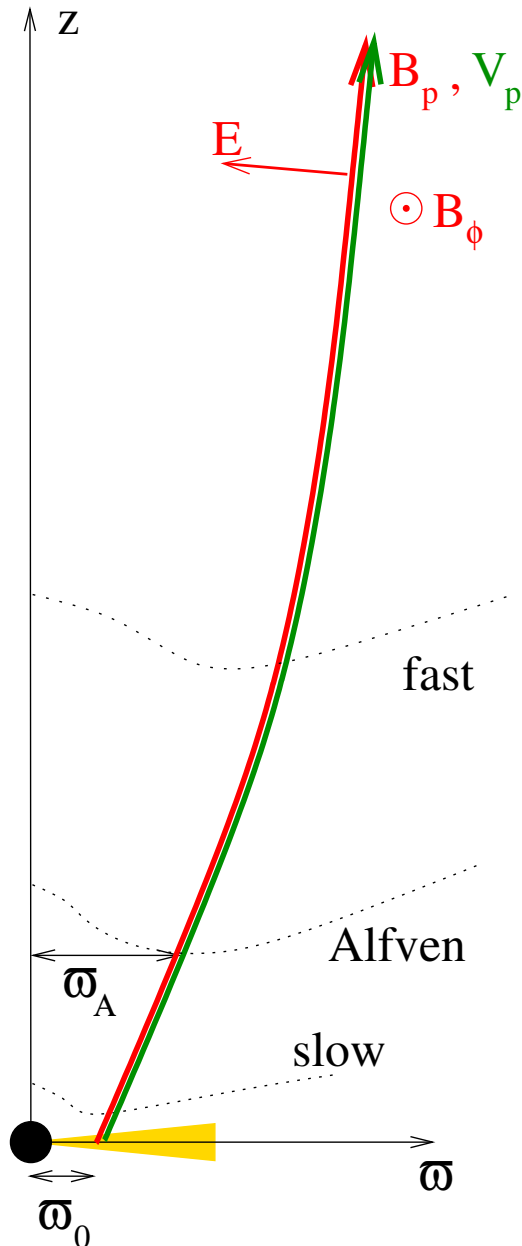
A rotating source (disk or star) creates an **axisymmetric** outflow



Assume **steady-state** and **ideal magnetohydrodynamics (MHD)**:

- Initially  $V_\phi = \varpi\Omega \gg V_p$ ,  $B_p \gtrsim B_\phi$
- Flux freezing: velocity  $\parallel \mathbf{B}$  plus  $\mathbf{E} \times \mathbf{B}$  drift  $\rightarrow \mathbf{V}_p \parallel \mathbf{B}_p$ .
- $B_p \propto 1/\varpi^2$ ,  $B_\phi \propto 1/\varpi$

# Critical surfaces



Regularity conditions:

- slow  $\rightarrow$  mass-loss rate  $\dot{M}_j = \frac{dM}{dt}$
- Alfvén  $\rightarrow$  angular momentum rate  $L\dot{M}_j$   
(for relativistic flows,  
Alfvén = light surface  $\varpi_A = c/\Omega$ )
- fast  $\rightarrow$  acceleration (nontrivial)



# Angular momentum extraction

$$L = \mu \Omega \varpi_A^2 \text{ where } \mu = \frac{\frac{dE}{dSdt}}{\frac{dM}{dSdt} c^2} = \text{maximum Lorentz factor}$$

So rate of angular momentum =  $\mu \Omega \varpi_A^2 \dot{M}_j$  (initially carried by the field and later by the matter).

In the disk, rate =  $\Omega \varpi_0^2 \dot{M}_a$ . If these are equal,  $\frac{\dot{M}_j}{\dot{M}_a} = \frac{\varpi_0^2}{\mu \varpi_A^2}$ .

- in YSO confirmed by HST observations! (Woitas et al 2005)

- in GRBs  $\dot{M}_a = 0.01 M_\odot s^{-1} \left( \frac{\dot{M}_j}{10^{-6} M_\odot s^{-1}} \right) \left( \frac{\mu}{400} \right) \left( \frac{\varpi_A / \varpi_0}{5} \right)^2$

(cf Popham et al 1999)

(This is equivalent to  $\frac{dE}{dt} \equiv \mu \dot{M}_j c^2 = \frac{GM \dot{M}_a}{\varpi_0}$ .)

# Acceleration mechanisms

- **thermal** (due to  $\nabla P$ )  $\rightarrow$  velocities up to  $C_s$
- **magnetocentrifugal** (beads on wire - Blandford & Payne)
  - in reality due to magnetic pressure
  - initial half-opening angle  $\vartheta > 30^\circ$
  - the  $\vartheta > 30^\circ$  not necessary for nonnegligible  $P$
  - velocities up to  $\varpi_0 \Omega$
- **relativistic thermal** (thermal fireball) gives  $\gamma \sim \xi_i$ ,  
where  $\xi = \frac{\text{enthalpy}}{\text{mass} \times c^2}$ .
- **magnetic** – up to  $\gamma_\infty = \mu$ ? Not always possible.

All acceleration mechanisms can be seen in the energy conservation equation

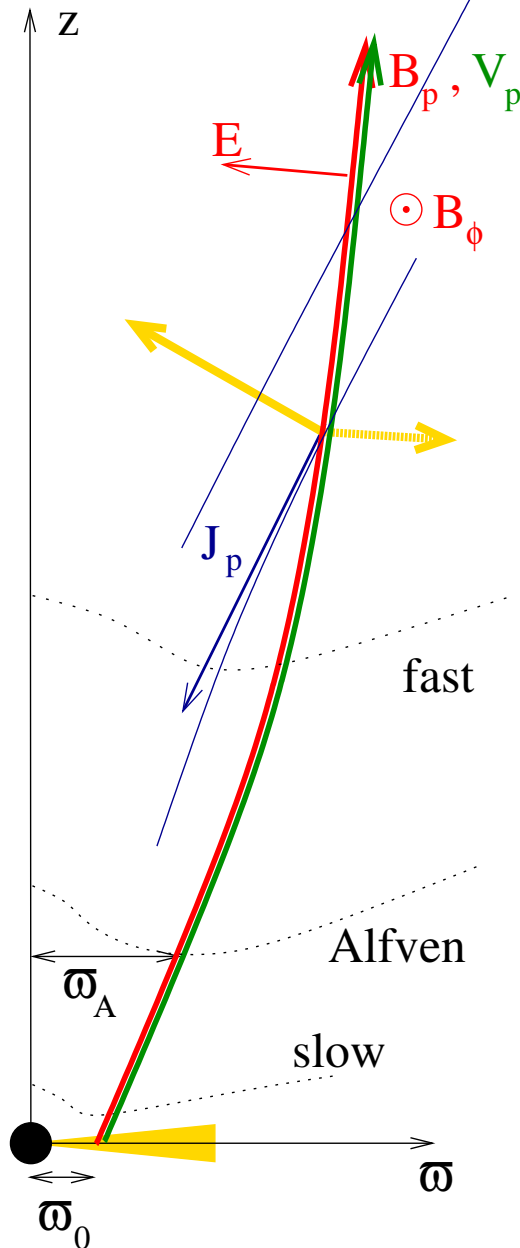
$$\mu = \xi\gamma + \frac{\Omega}{\Psi_A c^2} \varpi B_\phi$$

where  $\mu$ ,  $\Omega$ ,  $\Psi_A$  (=mass-to-magnetic flux ratio) are constants of motion.

So  $\gamma \uparrow$  when  $\xi \downarrow$  (thermal, relativistic thermal), or,  $\varpi B_\phi \downarrow \Leftrightarrow I_p \downarrow$  (magnetocentrifugal, magnetic).

At fast  $\gamma \approx \mu^{1/3} \ll \mu$ . Can we reach  $\gamma_\infty \sim \mu$  in the superfast regime?

# The efficiency of the magnetic acceleration

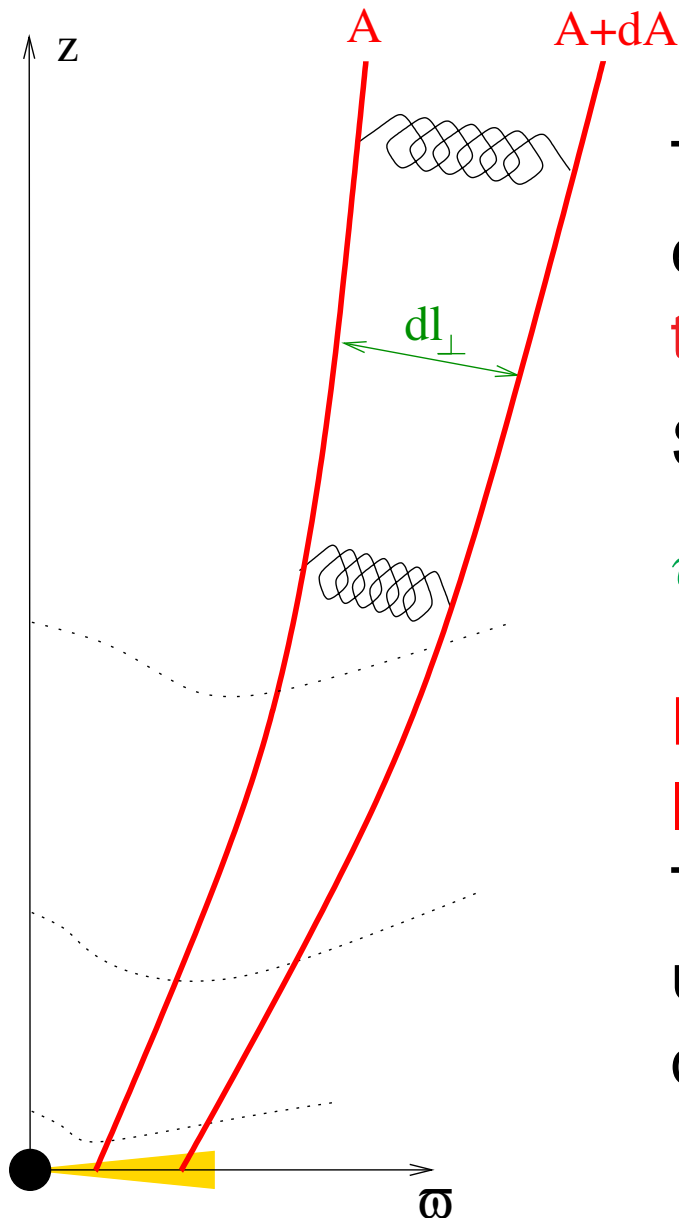


The  $J_p \times B_\phi$  force strongly depends on the angle between field-lines and current-lines.

Are we free to choose these two lines?  
NO! All MHD quantities are related to each other and should be found by solving the full system of equations.

From Ferraro's law,  $\varpi B_\phi \approx \varpi^2 B_p \Omega / V_p$ .

So, **the transfield force-balance determines the acceleration.**



The magnetic field minimizes its energy **under the condition of keeping the magnetic flux constant.**

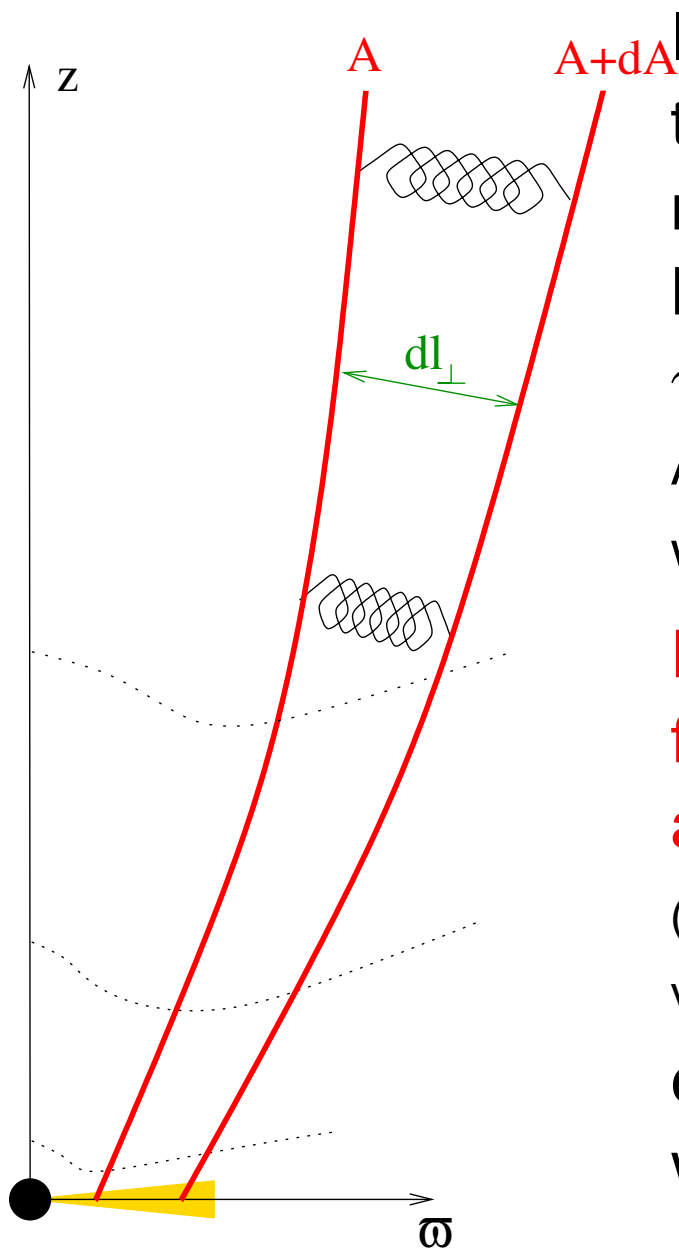
So,  $\varpi B_\phi \downarrow$  for decreasing

$$\varpi^2 B_p = \frac{\varpi^2}{2\pi\varpi dl_\perp} \underbrace{(B_p dS)}_{dA} \propto \frac{\varpi}{dl_\perp}.$$

**Expansion with increasing  $dl_\perp/\varpi$  leads to acceleration** (Vlahakis 2004).

The expansion ends in a more-or-less uniform distribution  $\varpi^2 B_p \approx A$  (in a quasi-monopolar shape).

# Conclusions on the magnetic acceleration



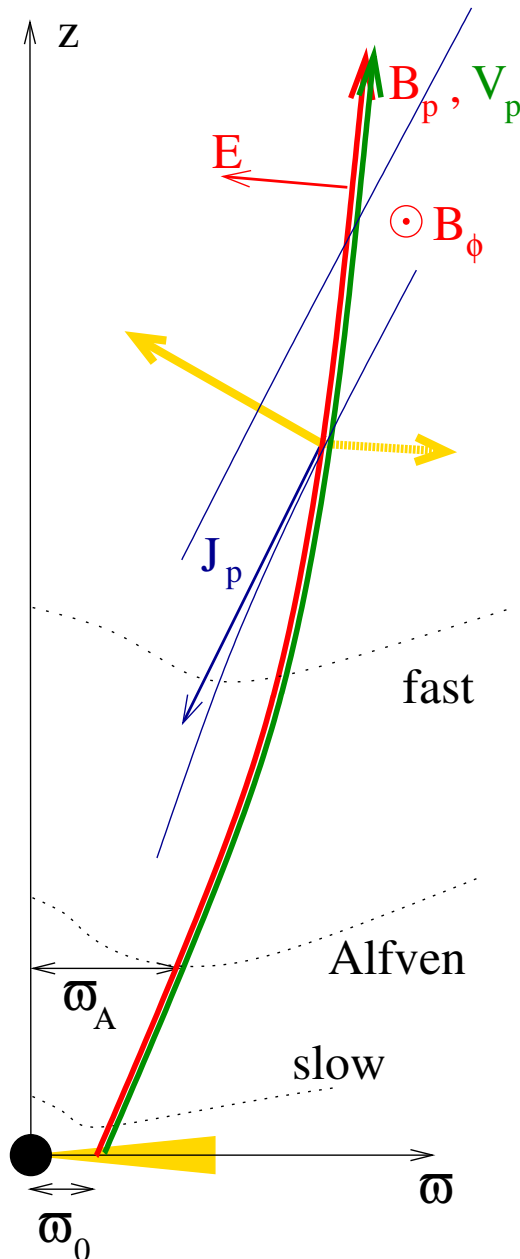
If we start with a uniform distribution the magnetic energy is already minimum  $\rightarrow$  no acceleration. Example: Michel's (1969) solution which gives  $\gamma_\infty \approx \mu^{1/3} \ll \mu$ . Also Beskin et al (1998); Bogovalov (2001) who found quasi-monopolar solutions.

**For any other (more realistic) initial field distribution we have efficient acceleration!**

(details and an analytical estimation of the efficiency in Vlahakis 2004, ApSS 293, 67).

example: if we start with  $\varpi^2 B_p / A = 2$  we have asymptotically  $\varpi^2 B_p / A = 1 \rightarrow 50\%$  efficiency

## On the collimation



The  $J_p \times B_\phi$  force contributes to the collimation (hoop-stress paradigm). In relativistic flows the electric force plays an opposite role (a manifestation of the high inertia of the flow).

- collimation by an external wind (Bogovalov & Tsinganos 2005, for AGN jets)
- surrounding medium may play a role (in the collapsar model)
- self-collimation mainly works at small distances where the velocities are mildly relativistic (Vlahakis & Königl 2003)

For  $\gamma \gg 1$ , curvature radius  $\mathcal{R} \sim \gamma^2 \varpi (\gg \varpi)$ .

Collimation more difficult, but not impossible!

$$\frac{\varpi}{\mathcal{R}} = -\varpi \frac{\partial^2 \varpi}{\partial z^2} \left( \frac{B_z}{B_p} \right)^3 \sim \left( \frac{\varpi}{z} \right)^2$$

Combining the above, we get

$$\gamma \sim \frac{z}{\varpi}$$

The same from

$$(t =) \frac{z}{V_z} = \frac{\varpi}{V_\varpi} \Leftrightarrow \frac{z}{c} = \frac{\varpi}{\sqrt{c^2 - V_z^2}} \approx \frac{\varpi}{c/\gamma}$$



# Application to GRB outflows

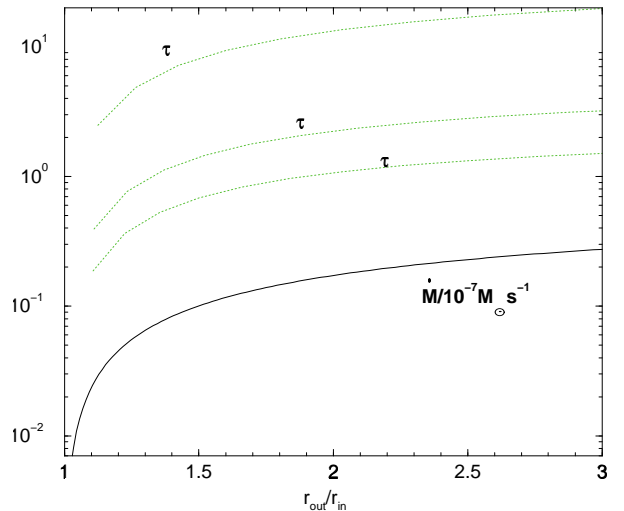
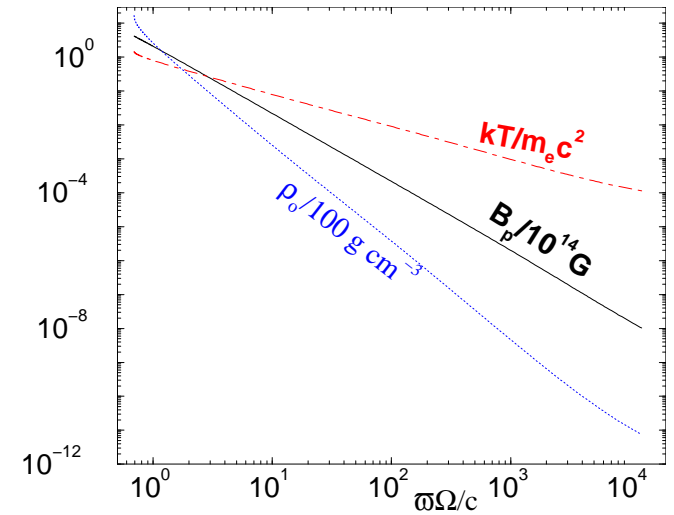
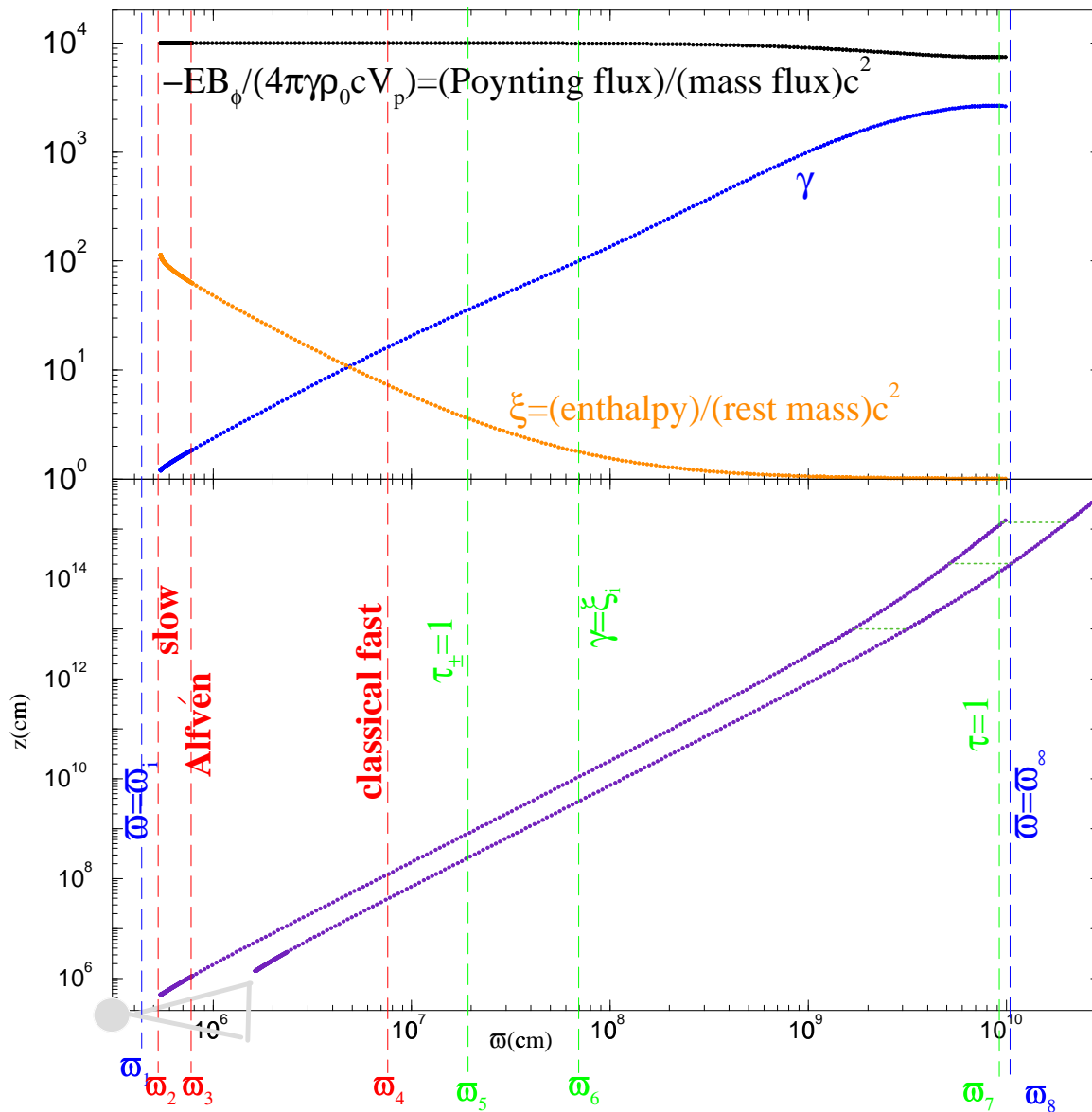
- is steady-state reasonable?
  - $\Omega \sim 10^4 \text{ rad s}^{-1} \Rightarrow$  many rotations during the engine's activity ( $\sim 10\text{s}$ )
  - the outflow is faster than the fastest signals propagating inside the flow  
 $\Rightarrow$  different shells are causally disconnected (frozen pulse)  
 (proof can be found in Vlahakis & Königl 2003, ApJ, 596, 1080)

- $\mathcal{E} = \frac{c}{4\pi} \underbrace{\frac{\varpi\Omega}{c} B_p}_{E} B_\phi \times \text{area} \times \text{duration} \Rightarrow$

$$\frac{B_p B_\phi}{(2 \times 10^{14} \text{G})^2} = \left[ \frac{\mathcal{E}}{5 \times 10^{51} \text{erg}} \right] \left[ \frac{\text{area}}{4\pi \times 10^{12} \text{cm}^2} \right]^{-1} \left[ \frac{\varpi\Omega}{10^{10} \text{cm s}^{-1}} \right]^{-1} \left[ \frac{\text{duration}}{10\text{s}} \right]^{-1}$$

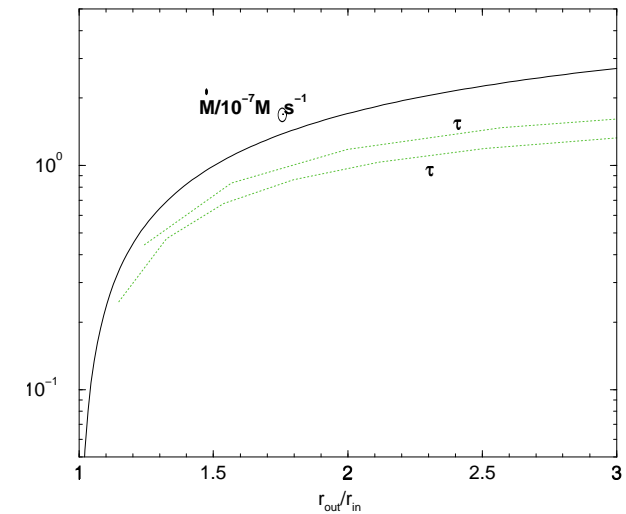
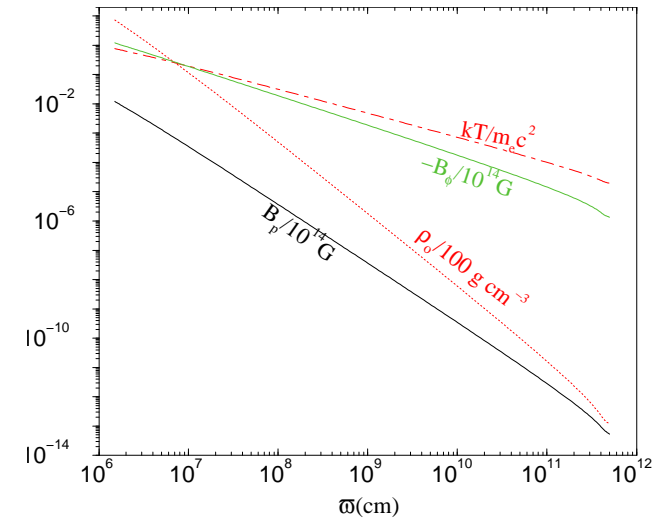
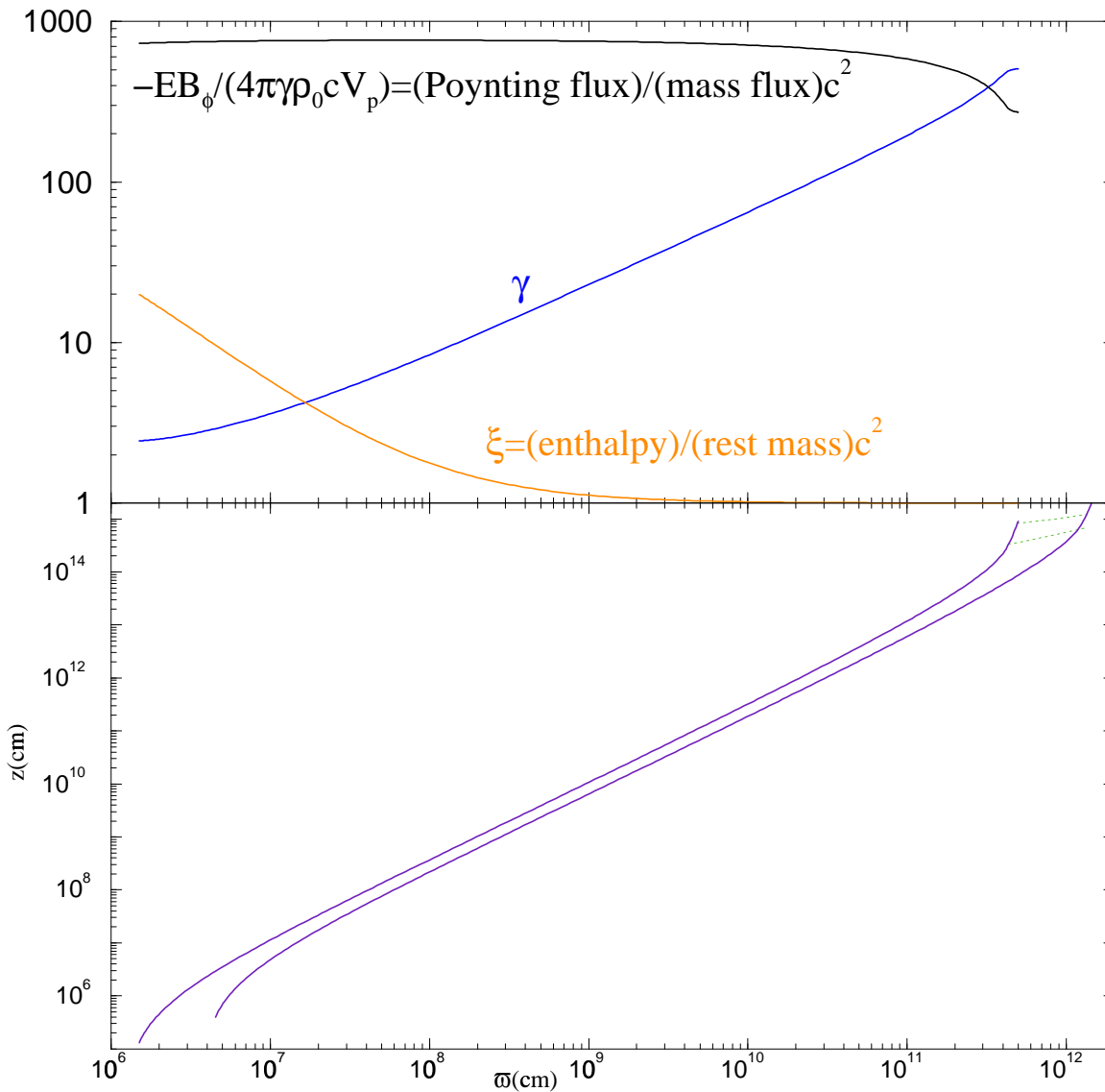
- from the BH:  $B_p \gtrsim 10^{15} \text{G}$  (small  $B_\phi$ , small area)
- from the disk: smaller magnetic field required  $\sim 10^{14} \text{G}$
- If initially  $B_p/B_\phi > 1$ , a **trans-Alfvénic** outflow is produced.
- If initially  $B_p/B_\phi < 1$ , the outflow is **super-Alfvénic** from the start.

# Trans-Alfvénic Jets (NV & Königl 2001, 2003a)



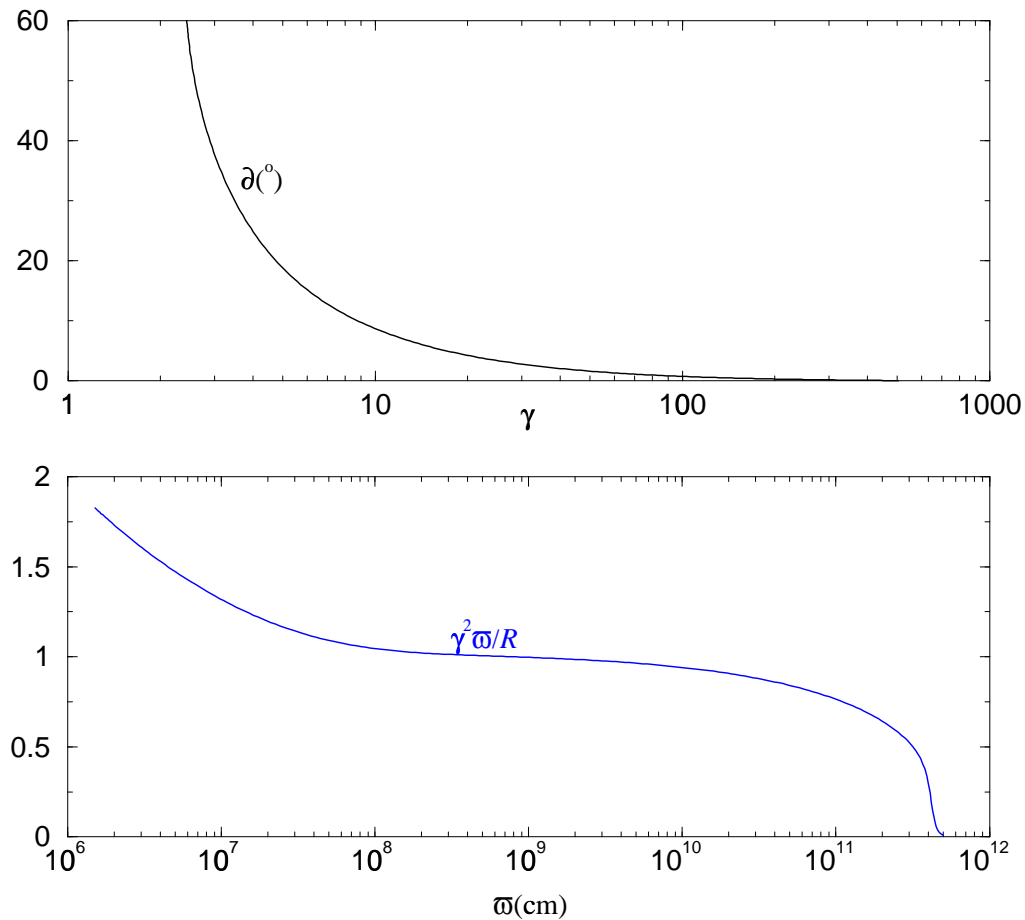
- $\omega_1 < \omega < \omega_6$ : **Thermal acceleration** - force free magnetic field ( $\gamma \propto \omega$ ,  $\rho_0 \propto \omega^{-3}$ ,  $T \propto \omega^{-1}$ ,  $\omega B_\phi = const$ , parabolic shape of fieldlines:  $z \propto \omega^2$ )
- $\omega_6 < \omega < \omega_8$ : **Magnetic acceleration** ( $\gamma \propto \omega$ ,  $\rho_0 \propto \omega^{-3}$ )
- $\omega = \omega_8$ : **cylindrical regime** - equipartition  $\gamma_\infty \approx (-EB_\phi/4\pi\gamma\rho_0 V_p)_\infty$

# Super-Alfvénic Jets (NV & Königl 2003b)



- **Thermal acceleration** ( $\gamma \propto r^{0.44}$ ,  $\rho_0 \propto r^{-2.4}$ ,  $T \propto r^{-0.8}$ ,  $B_\phi \propto r^{-1}$ ,  $z \propto r^{1.5}$ )
- **Magnetic acceleration** ( $\gamma \propto r^{0.44}$ ,  $\rho_0 \propto r^{-2.4}$ )
- **cylindrical regime - equipartition**  $\gamma_\infty \approx (-EB_\phi/4\pi\gamma\rho_0V_p)_\infty$

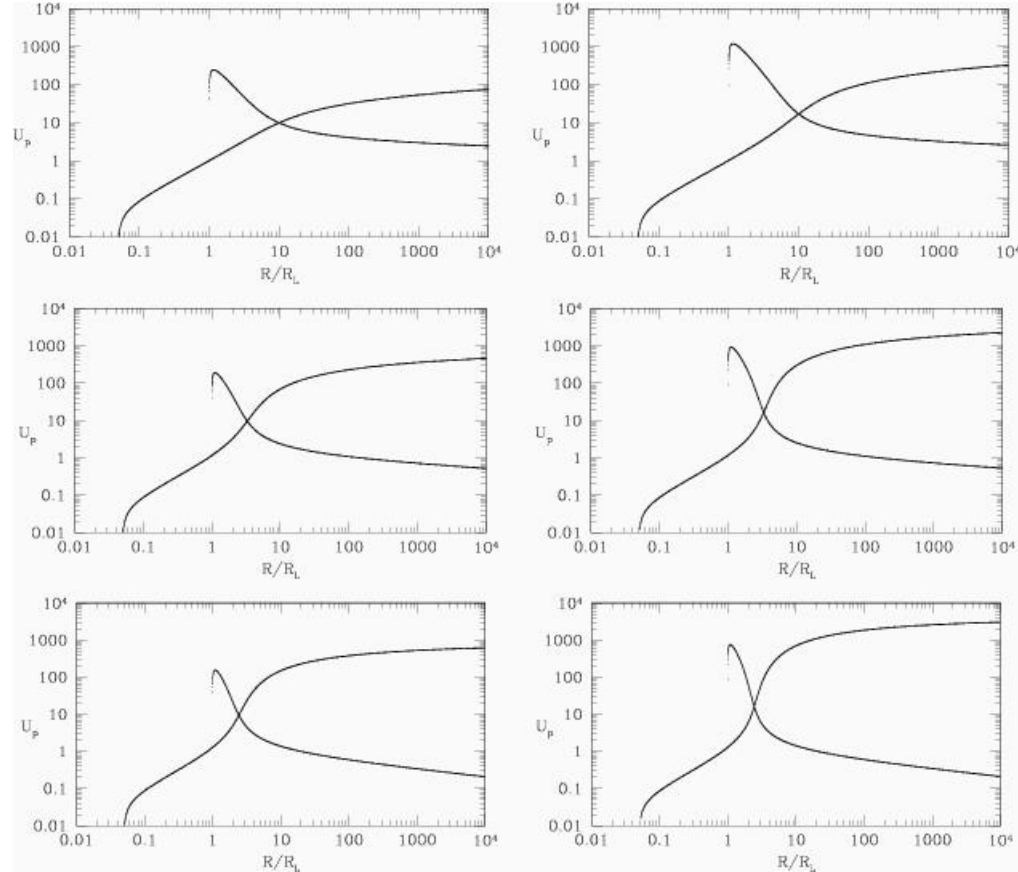
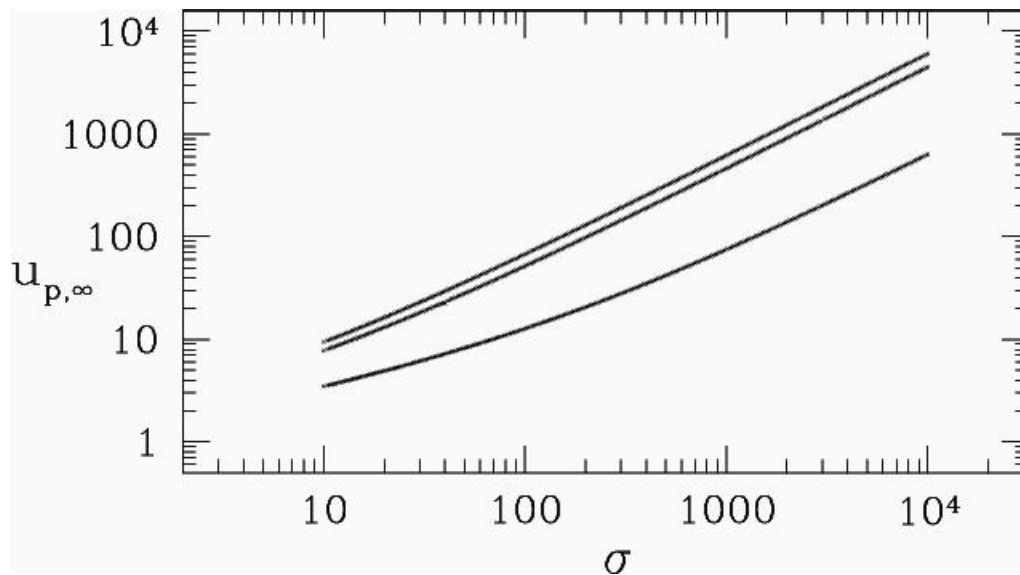
# Collimation



- ★ At  $\varpi = 10^8$  cm – where  $\gamma = 10$  – the opening half-angle is already  $\vartheta = 10^\circ$
- ★ For  $\varpi > 10^8$  cm, collimation continues slowly ( $\mathcal{R} \sim \gamma^2 \varpi$ )

## Other solutions

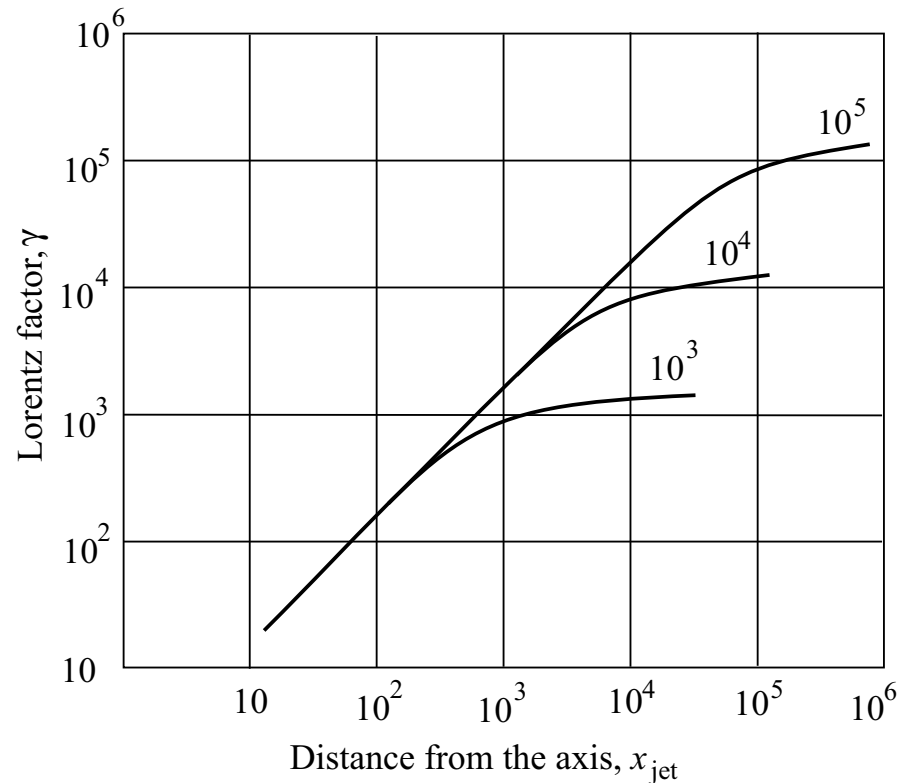
- Fendt & Ouyed (2004):



They used prescribed fieldlines (with  $\varpi^2 B_p/A \propto \varpi^{-q}$ ) and found efficient acceleration with  $\gamma_\infty$  (their  $u_{p,\infty}$ )  $\sim \mu$  (their  $\sigma$ ).

Although the analysis is not complete (the transfield is not solved), the results show the relation between line-shape and efficiency.

- Beskin & Nokhrina (2006):



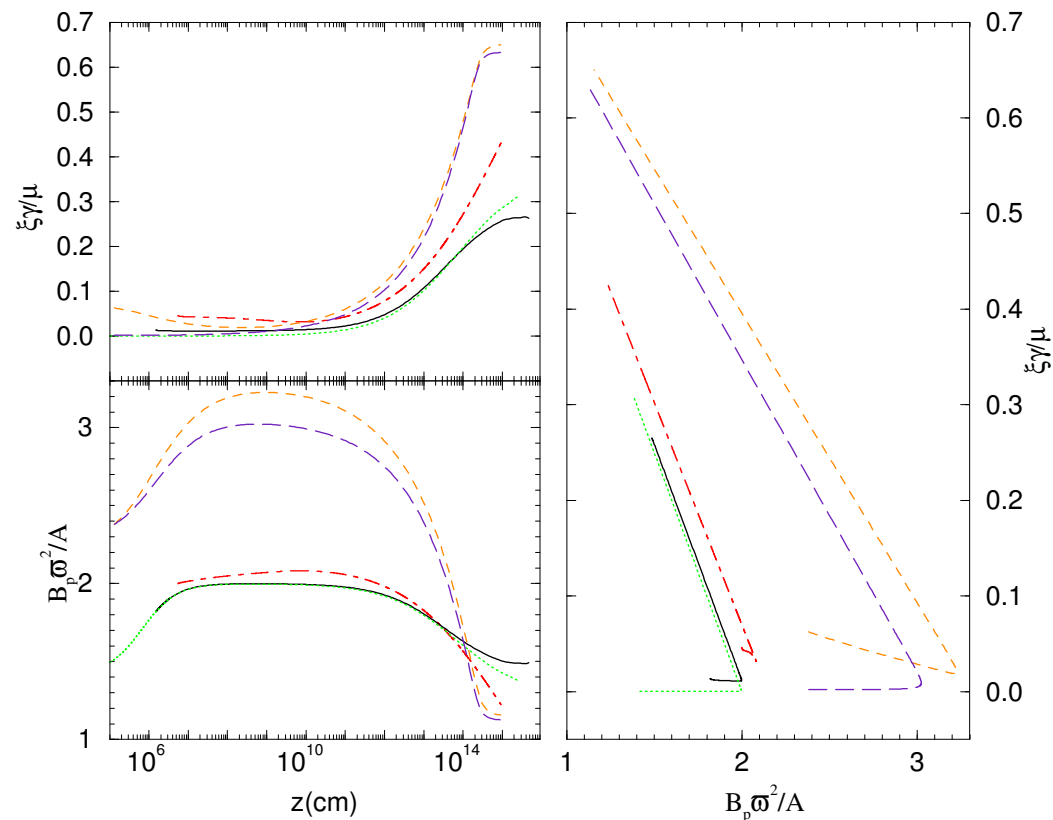
By expanding the equations wrt  $2/\mu$  (their  $1/\sigma$ ) they found a parabolic solution. The acceleration in the superfast regime is efficient, reaching

$$\gamma_{\infty} \sim \mu.$$

The scaling  $\gamma \propto \varpi$  is the same as in Vlahakis & Königl (2003a).

- simulations:  
many nice works (e.g., by De Villiers; Proga; McKinney), but still there are numerical problems to cover all the outflow and high Lorentz factors.

Enough to solve up to the fast point!



# Dissipation processes

- **reconnection** if there exist a small-scale field component (e.g., Drenkahn & Spruit 2002 modified the induction equation by adding a term  $B/\tau$ ). The resulting gradient of  $B^2/8\pi$  accelerates the flow,  $\gamma \propto r^{1/3}$ . The dissipated energy is radiated (above the photosphere). Interesting to combine with MHD (they considered monopolar flow), and to describe the reconnection with a more exact way if possible.
- **kink instability** operates when  $(B_\phi/B_p)_{co} \gg 1$ , or,  $B_\phi/\gamma \gg B_p$ . In the Vlahakis & Königl trans-Alfvénic solutions this never happens, but in the super-Alfvénic solutions it does.  
Giannios & Spruit (2006) modeled the instability by adding a term  $\sim B/\tau$  in the induction equation, with  $\tau \approx \gamma\varpi/c$ . Results similar to Drenkahn & Spruit (2002).  
3D relativistic MHD simulations needed.
- **minimum energy solutions by conserving helicity** (Königl & Choudhuri 1985)



# Alternatives

- thermal driving

- cannot explain the observed angular momentum in YSO jets
- cannot explain pc-scale accelerations in AGN
- GRB photospheric emission would have been detectable (Daigne & Mochkovitch 2002)

- outflow from black-hole vs disk

- no difference if the result is baryonic flow (disk outflow, or, Fick diffusion across fieldlines above a BH – Levinson & Eichler 2003). In both cases we have MHD (although the mechanism that transfers energy to the field is different: Blandford & Znajek vs accretion).
- the field is higher in the BH-case (smaller ejection surface)

- electromagnetic outflows:

- This corresponds to the case (subcase of MHD) where the field distribution is force-free – already at the minimum-energy
- extraction of pure electromagnetic energy (no baryons) – Lyutikov & Blandford astro-ph/0312347
- the flow never becomes superfast
- current-driven instabilities lead to dissipation of magnetic field and subsequent emission

# Conclusions

- ★ MHD could explain the dynamics of GRB jets:
  - acceleration (the flow is initially thermally, and subsequently magnetically accelerated up to Lorentz factors corresponding to rough equipartition between kinetic and Poynting fluxes) –  $\gamma \propto \varpi^\beta$  with  $\beta \approx 1$  in trans-Alfvénic flows and  $\beta < 1$  in super-Alfvénic from the start
  - collimation (parabolic shape  $z \propto \varpi^{\beta+1}$ )
- ★ The paradigm of MHD jets works in a similar way in YSOs, AGN, GRBs!

# Acknowledgments

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