

Optical Variability of AGN

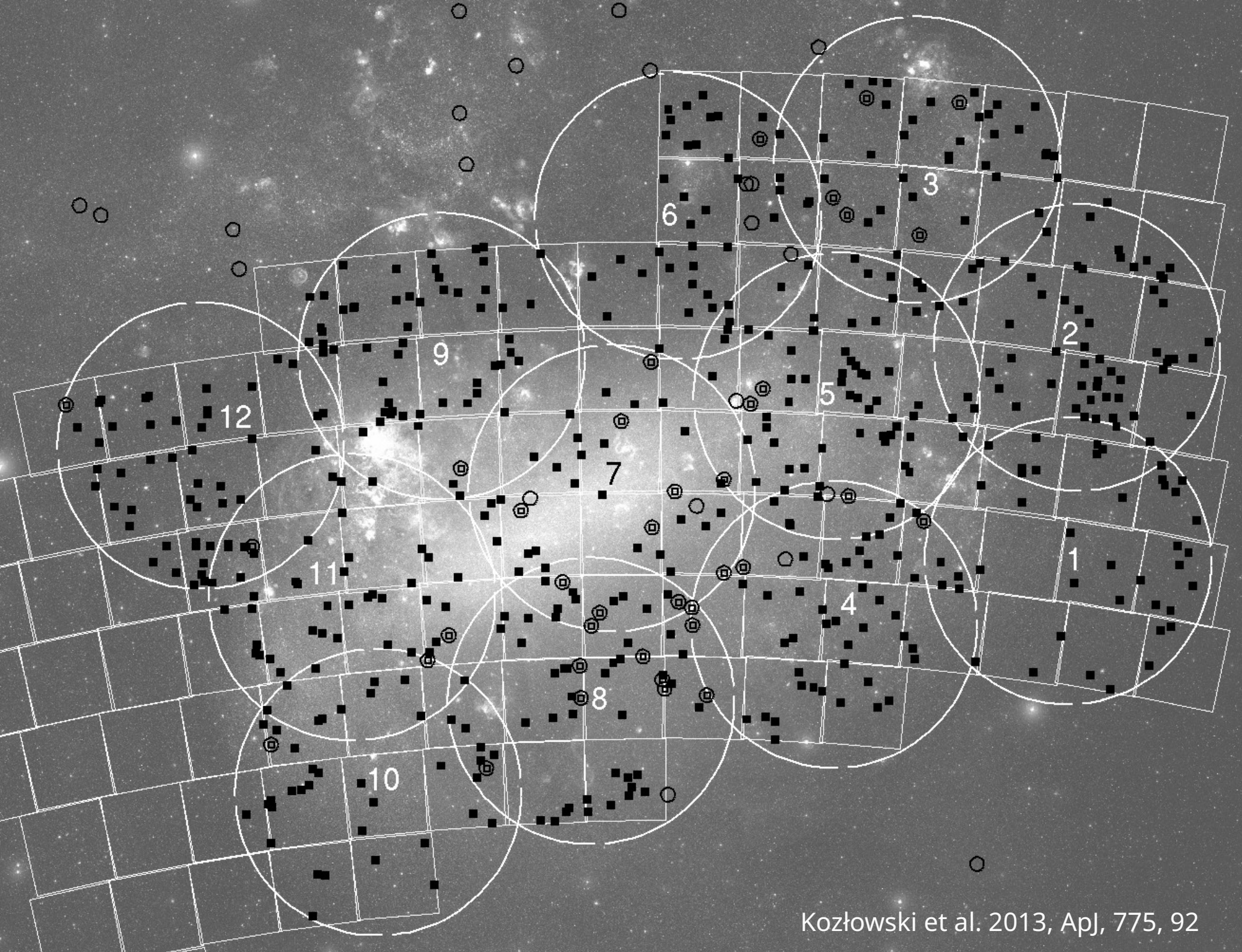
Szymon Kozłowski

The Variable Multi-Messenger Sky
Polish-German WE-Heraeus-Seminar
07-10 November 2022

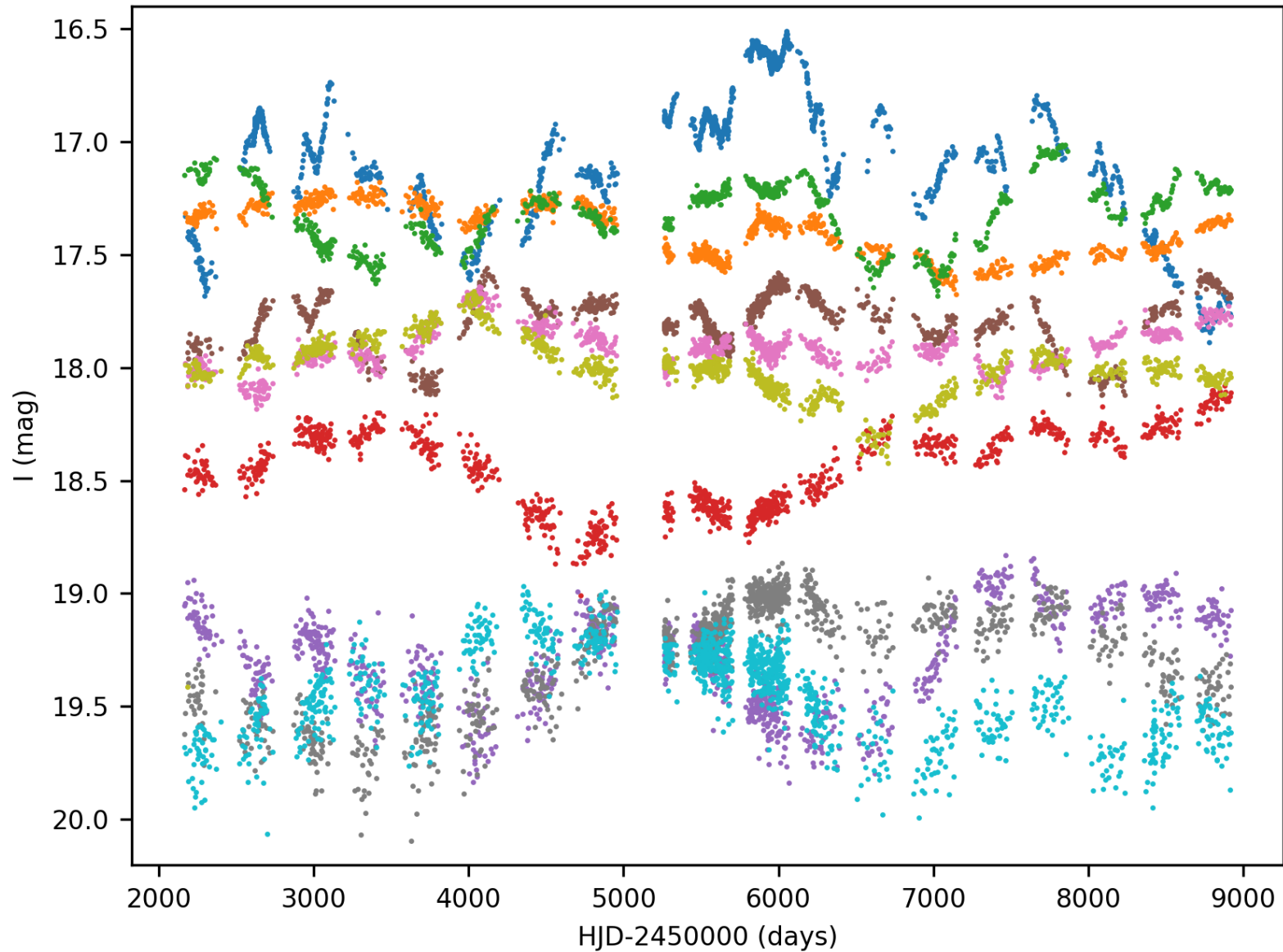
Optical Gravitational Lensing Experiment (OGLE)

Udalski et al. 2015, Acta Astronomica, 65, 1

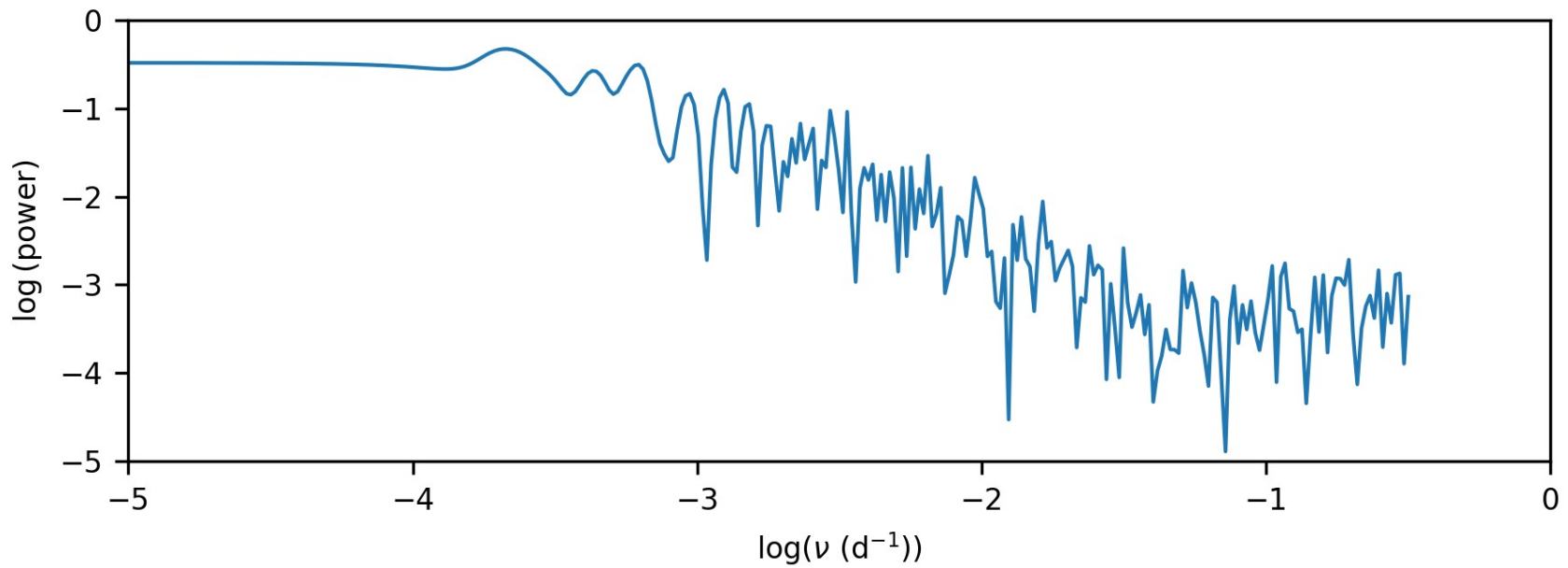
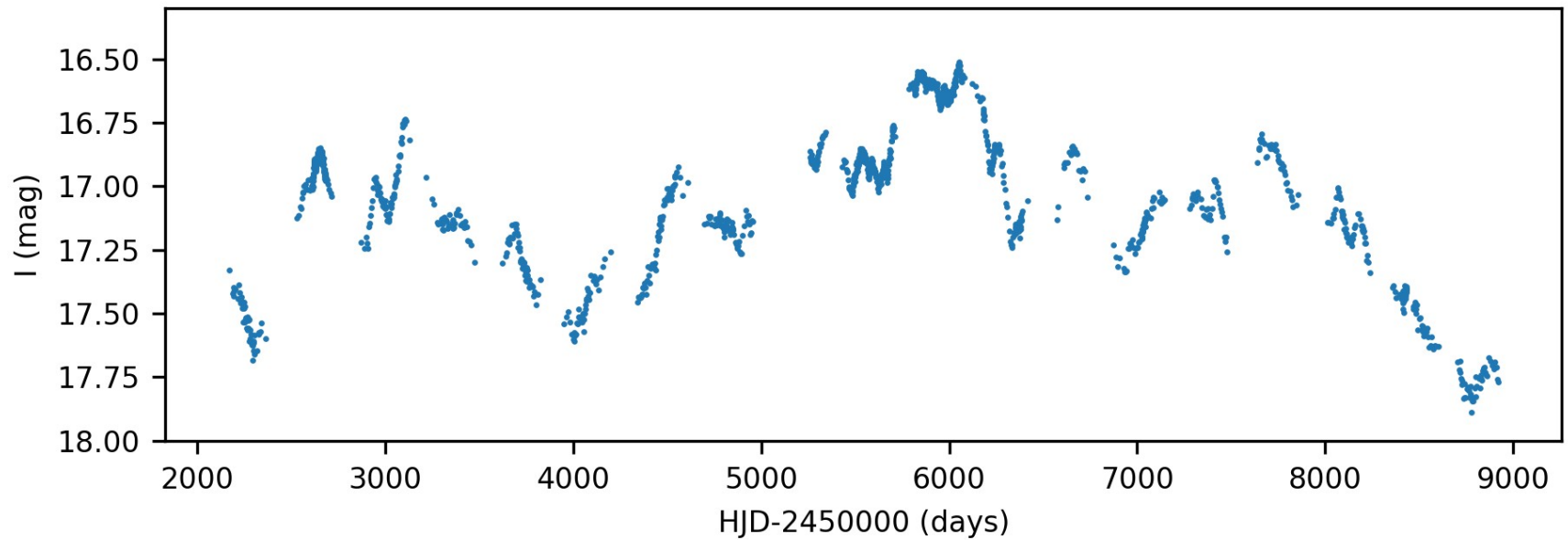




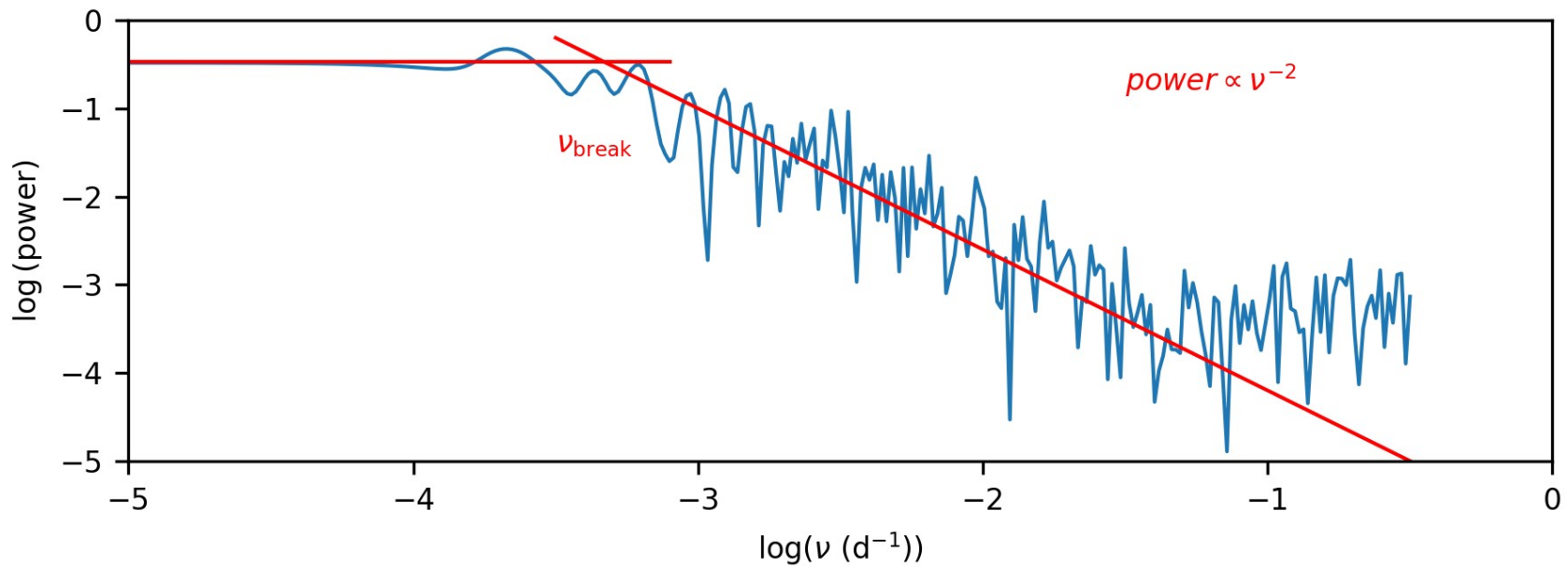
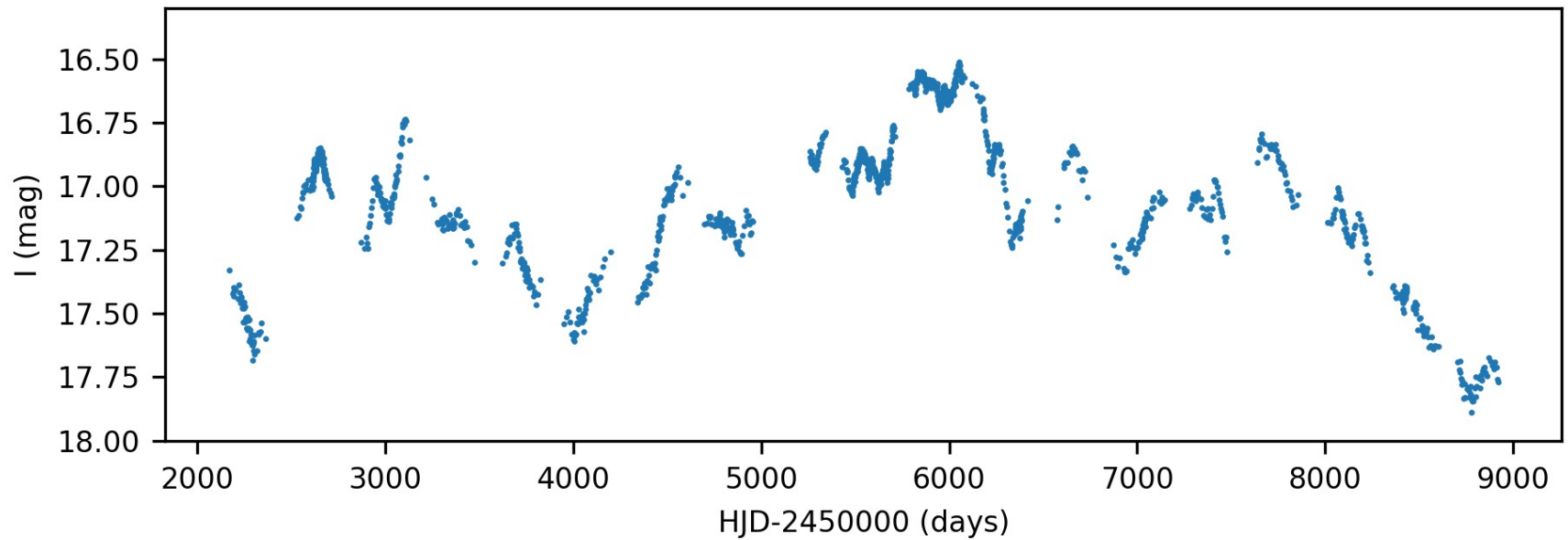
AGN Variability in OGLE



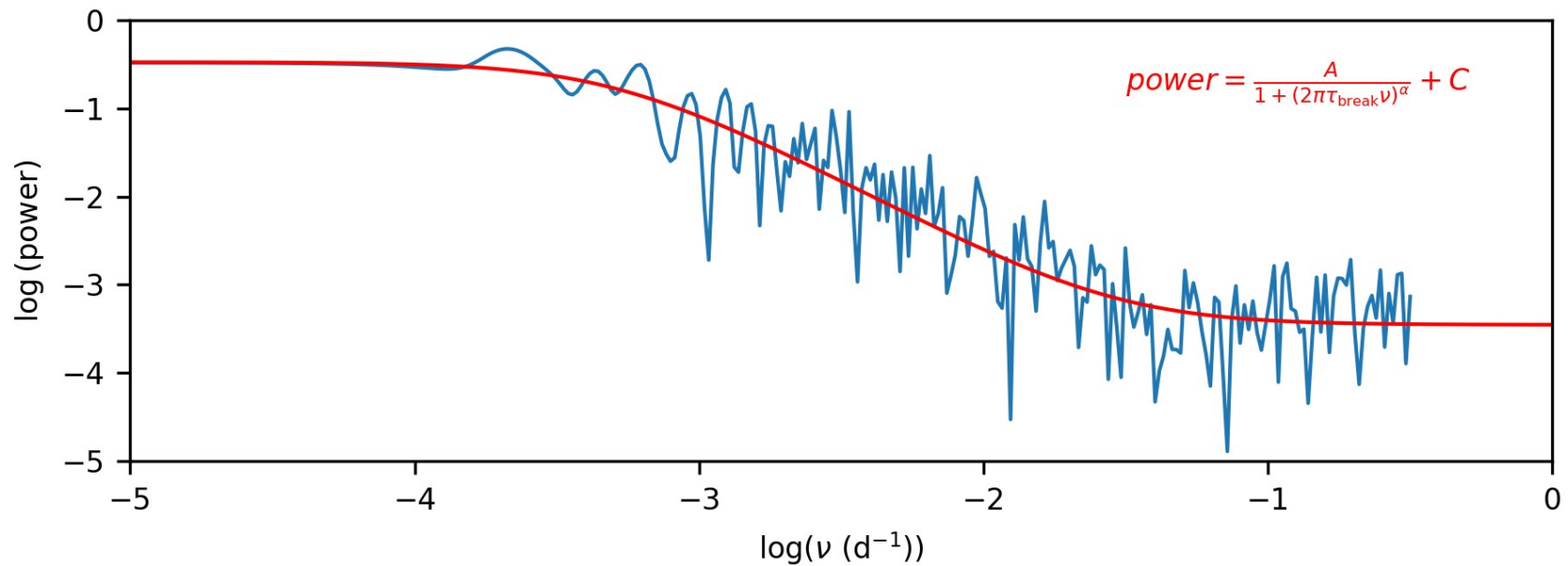
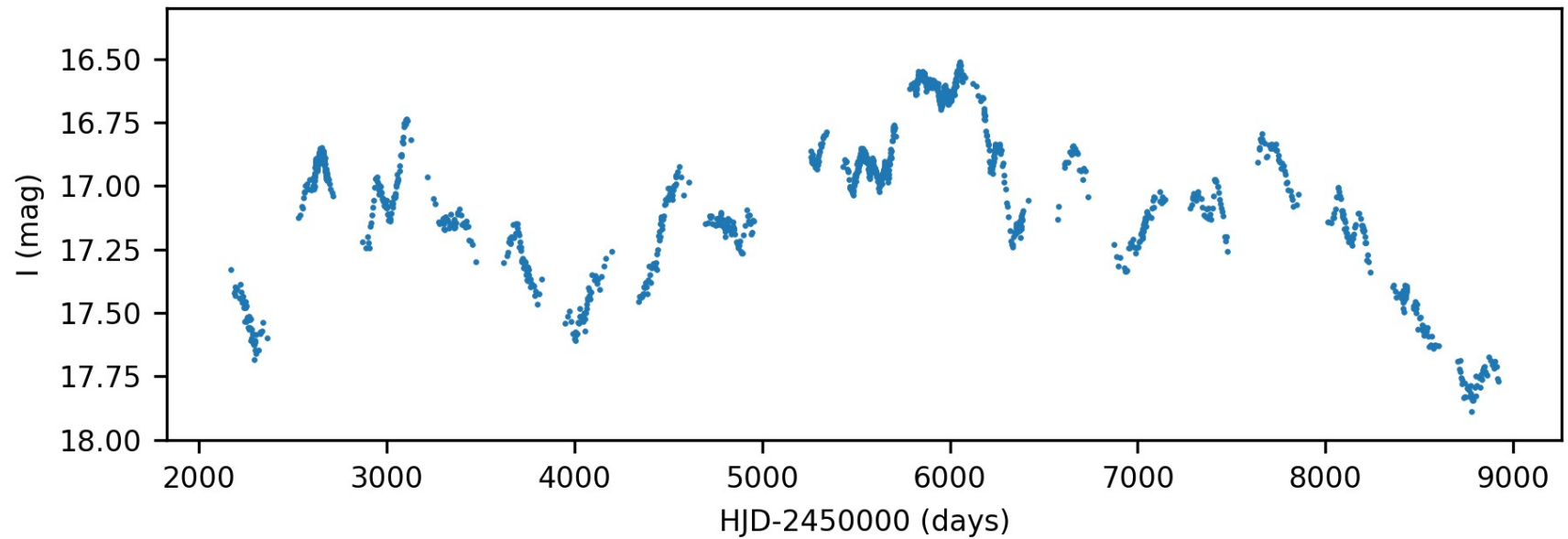
Non-periodic Objects



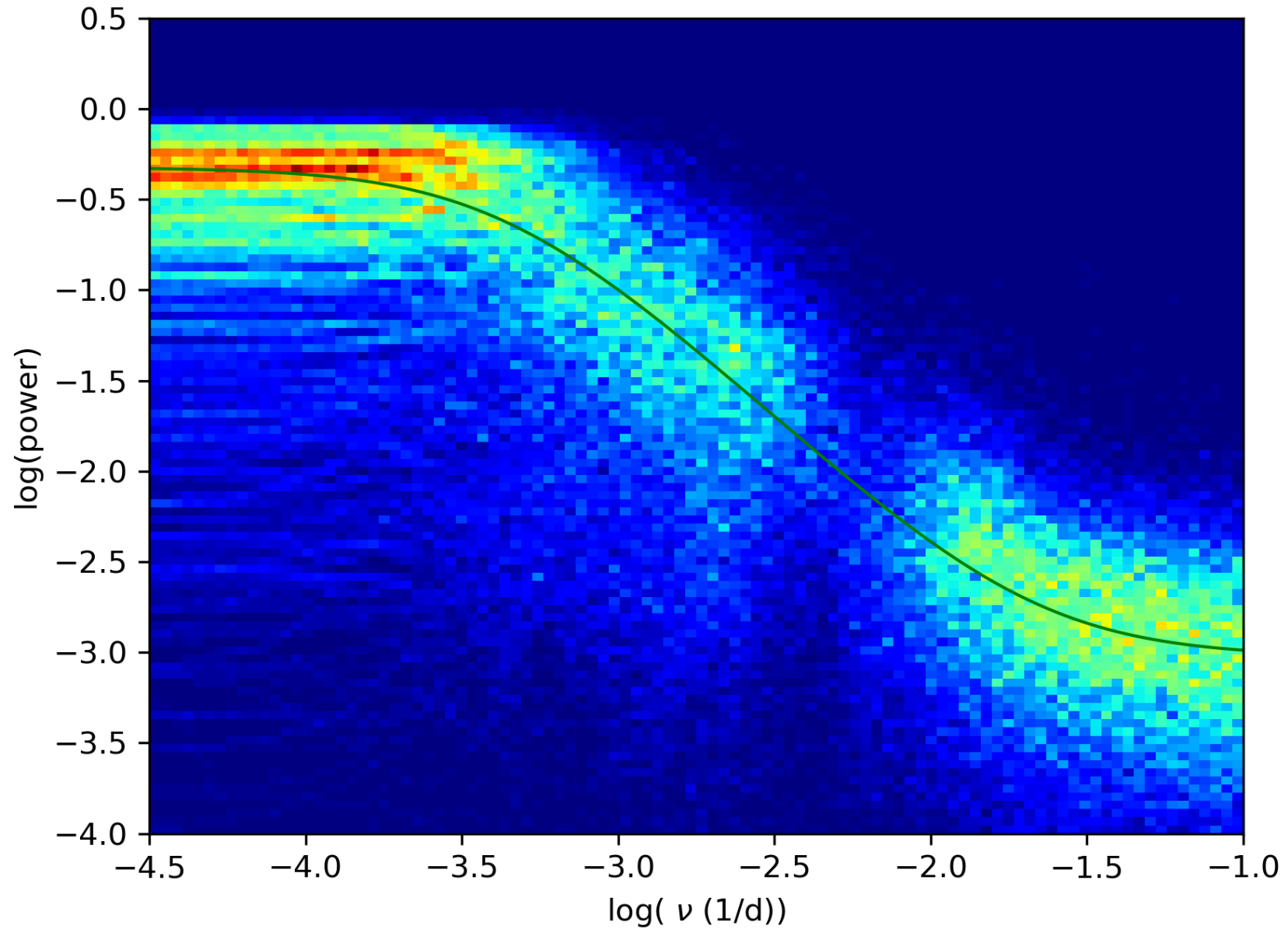
Non-periodic Objects



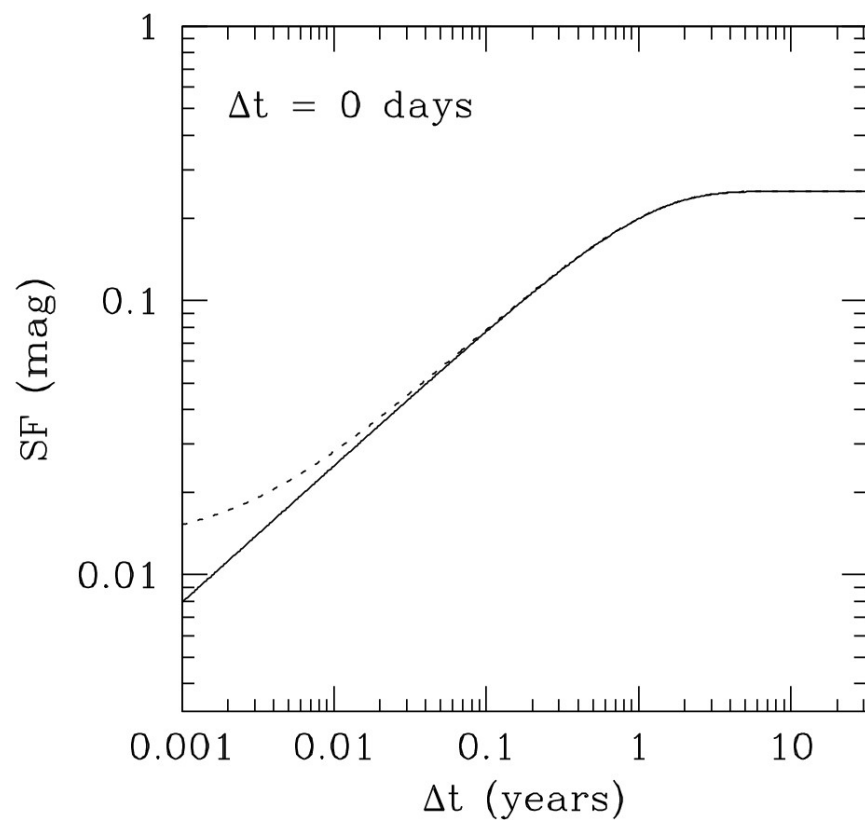
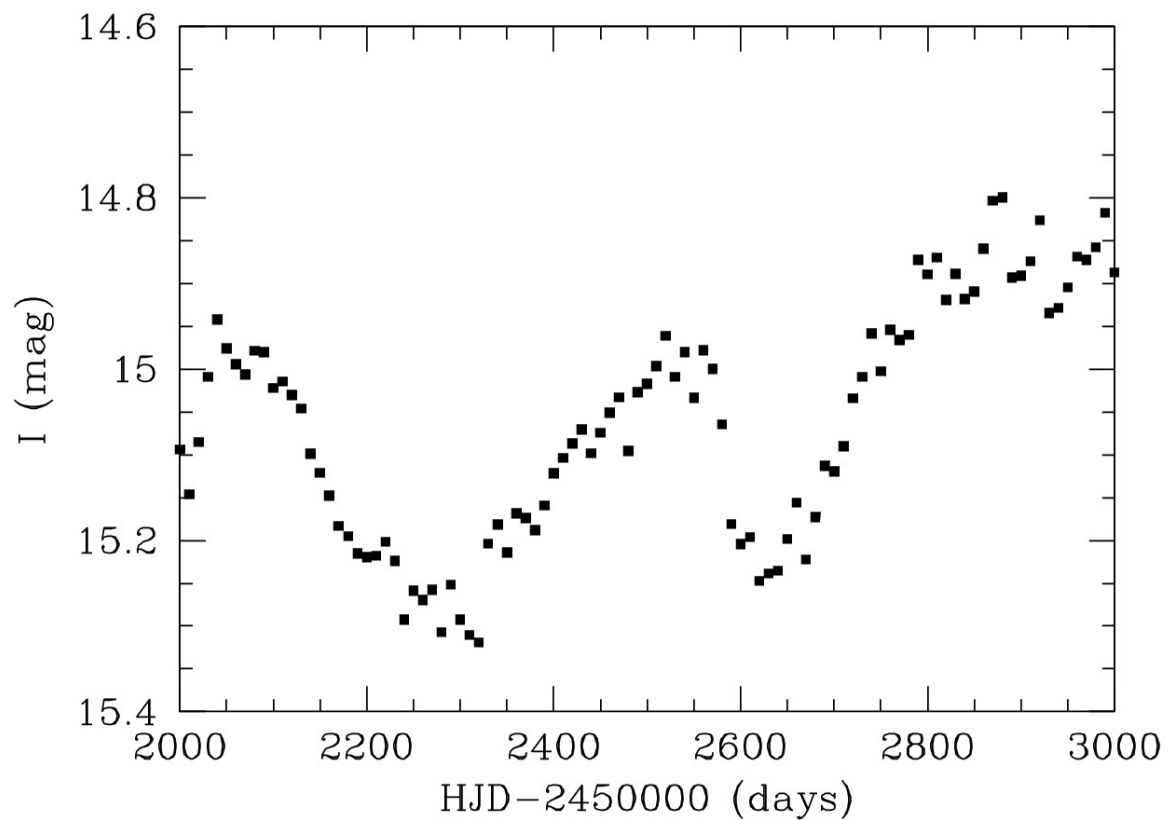
Non-periodic Objects



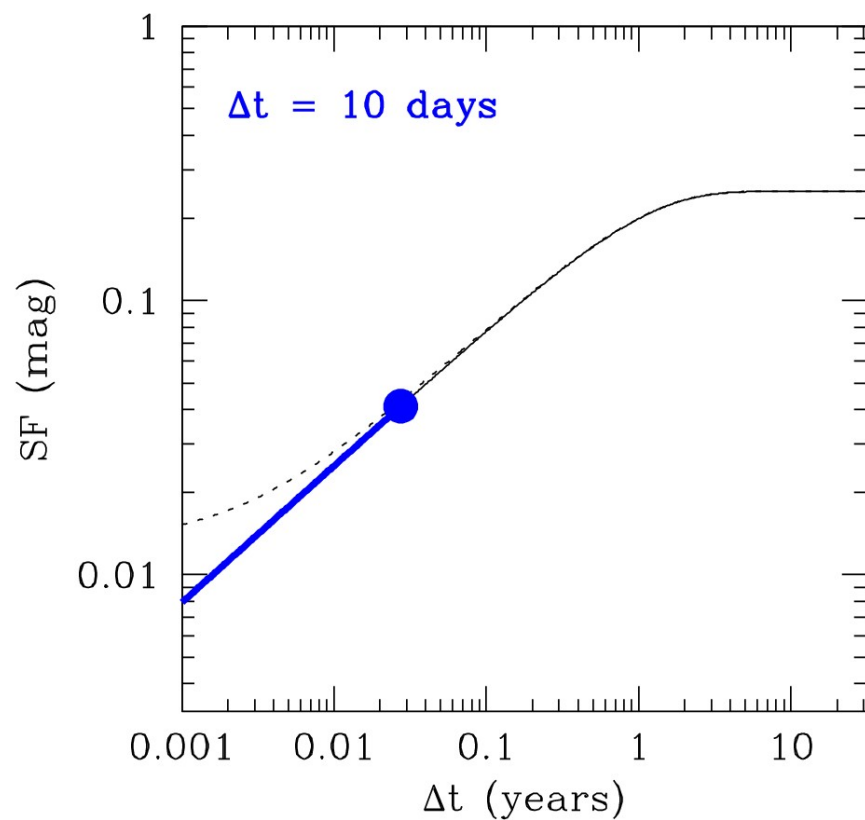
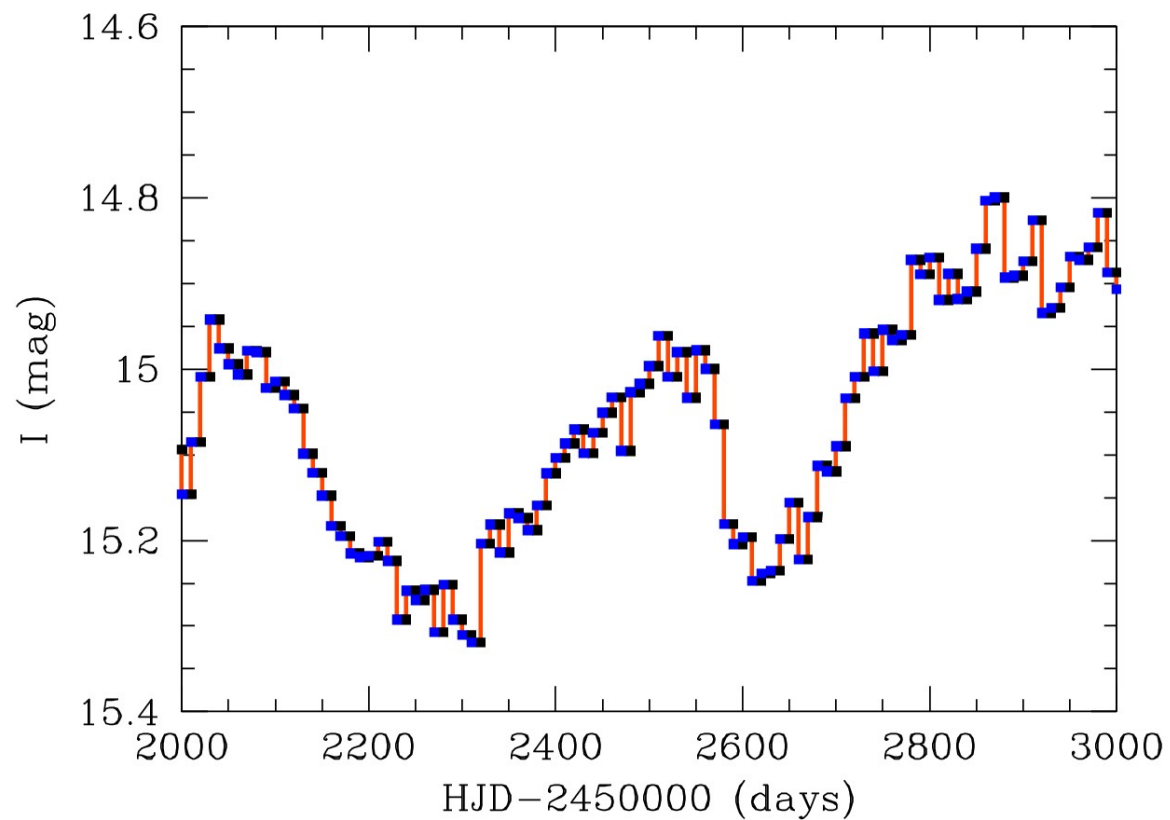
Power spectrum: OGLE-III + OGLE-IV



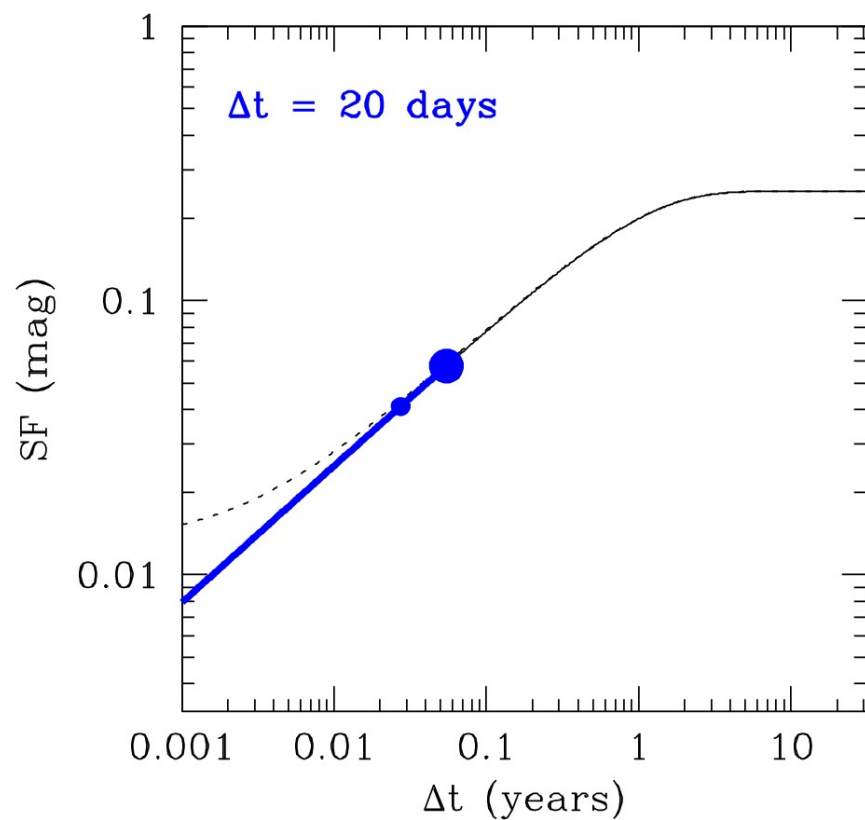
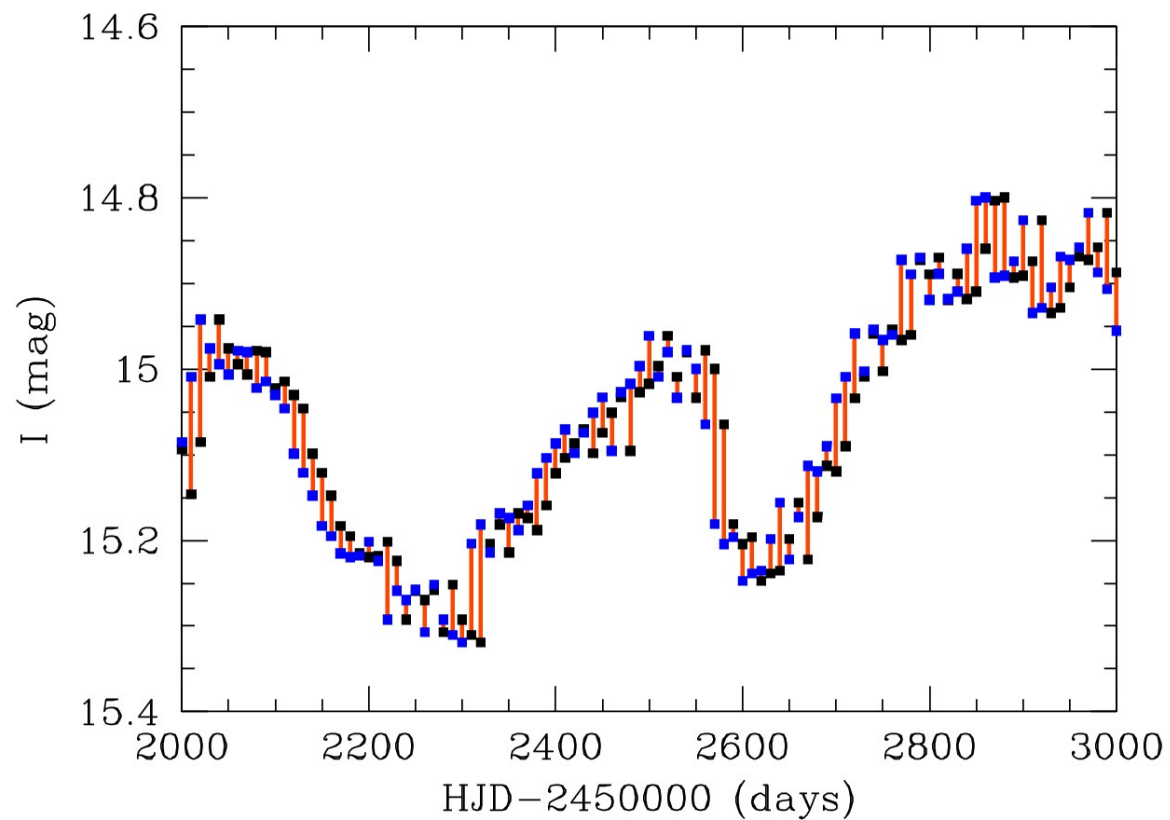
Structure Function



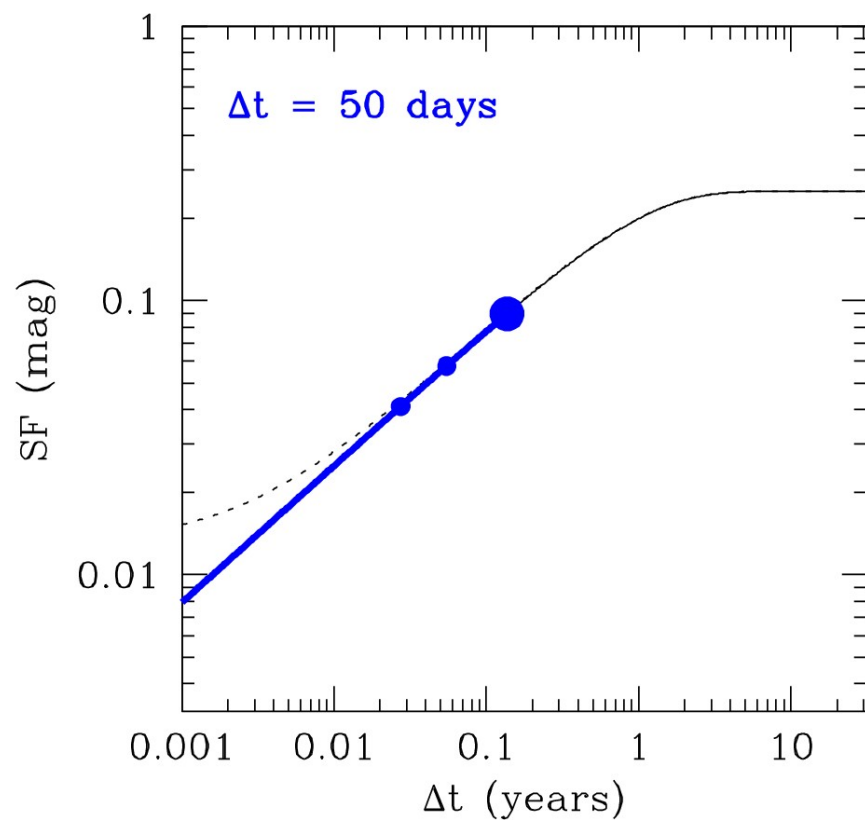
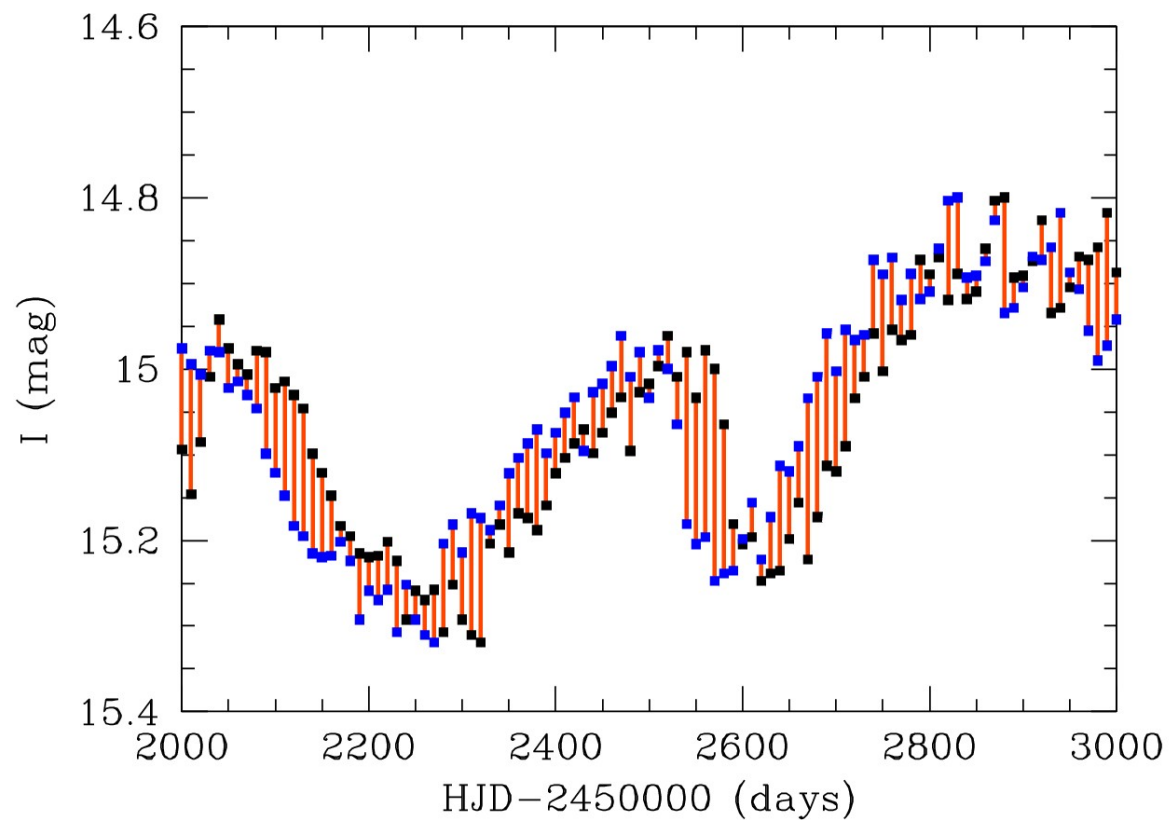
Structure Function



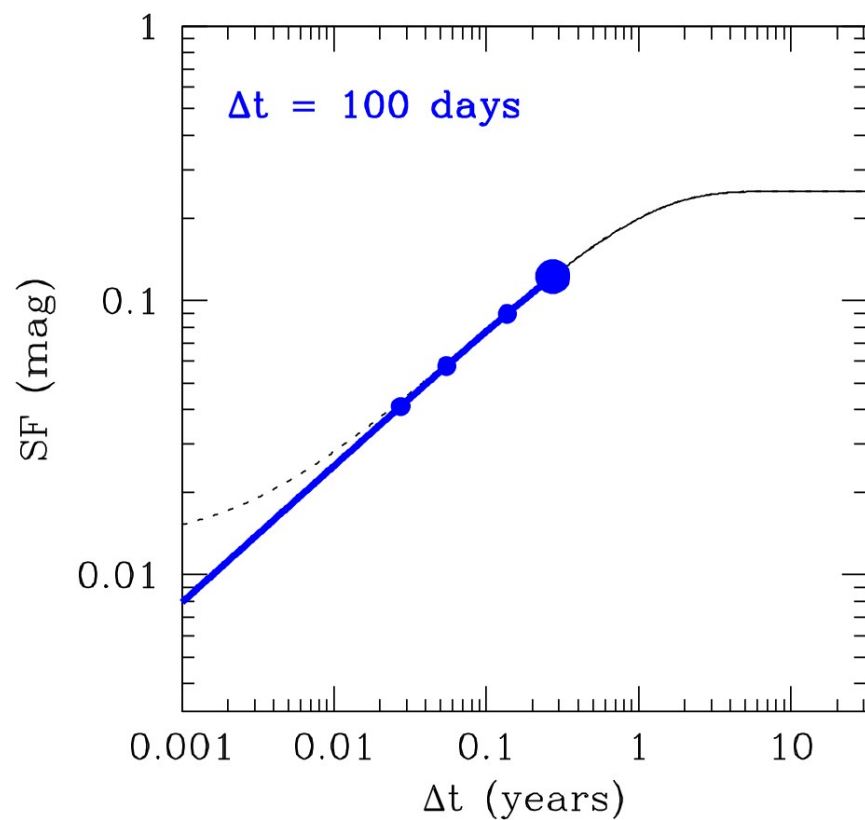
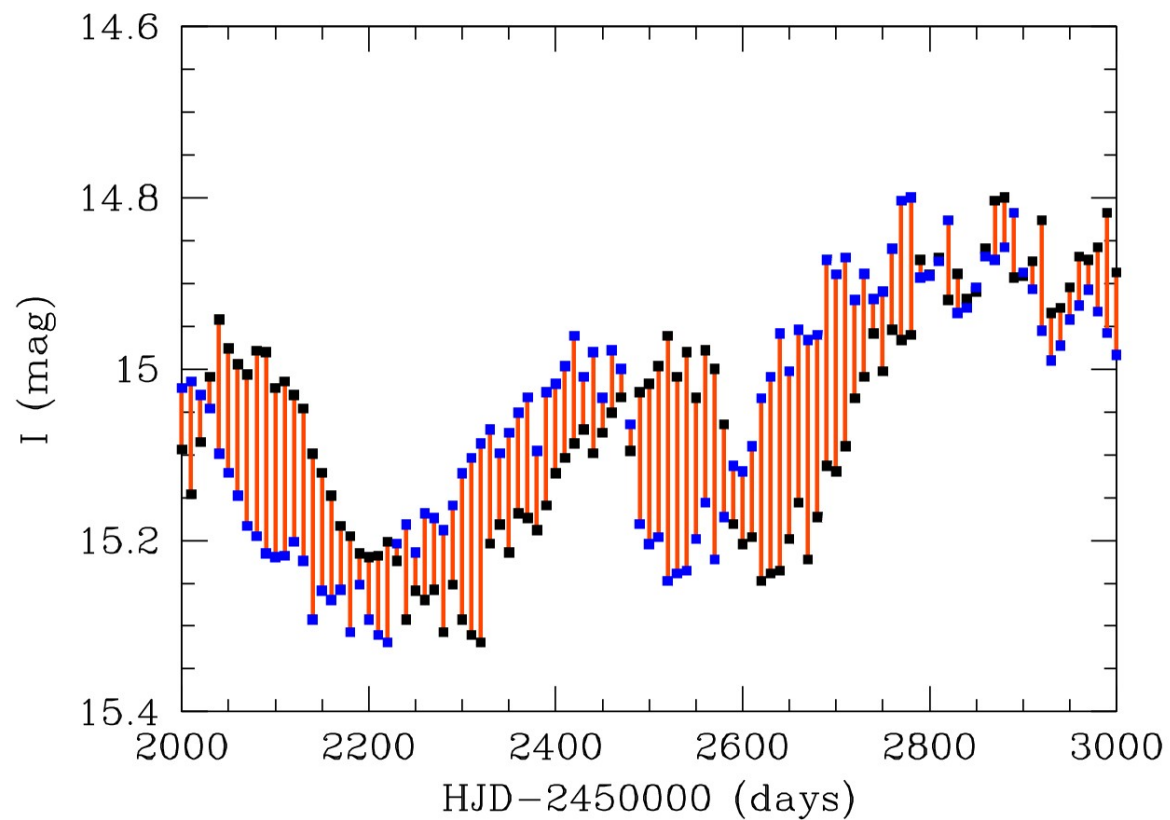
Structure Function



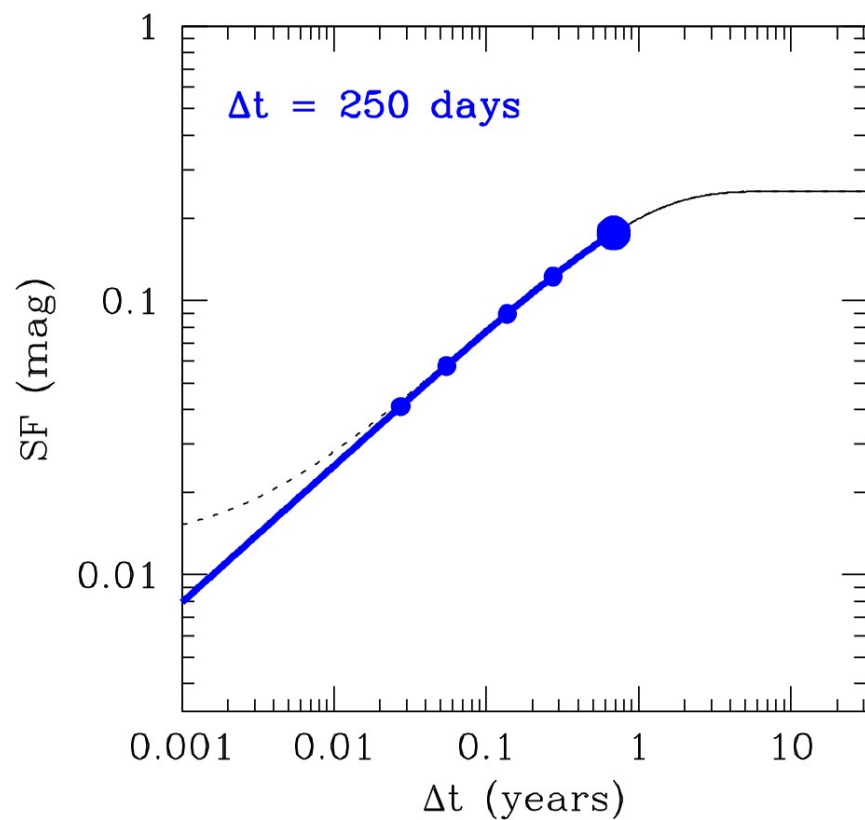
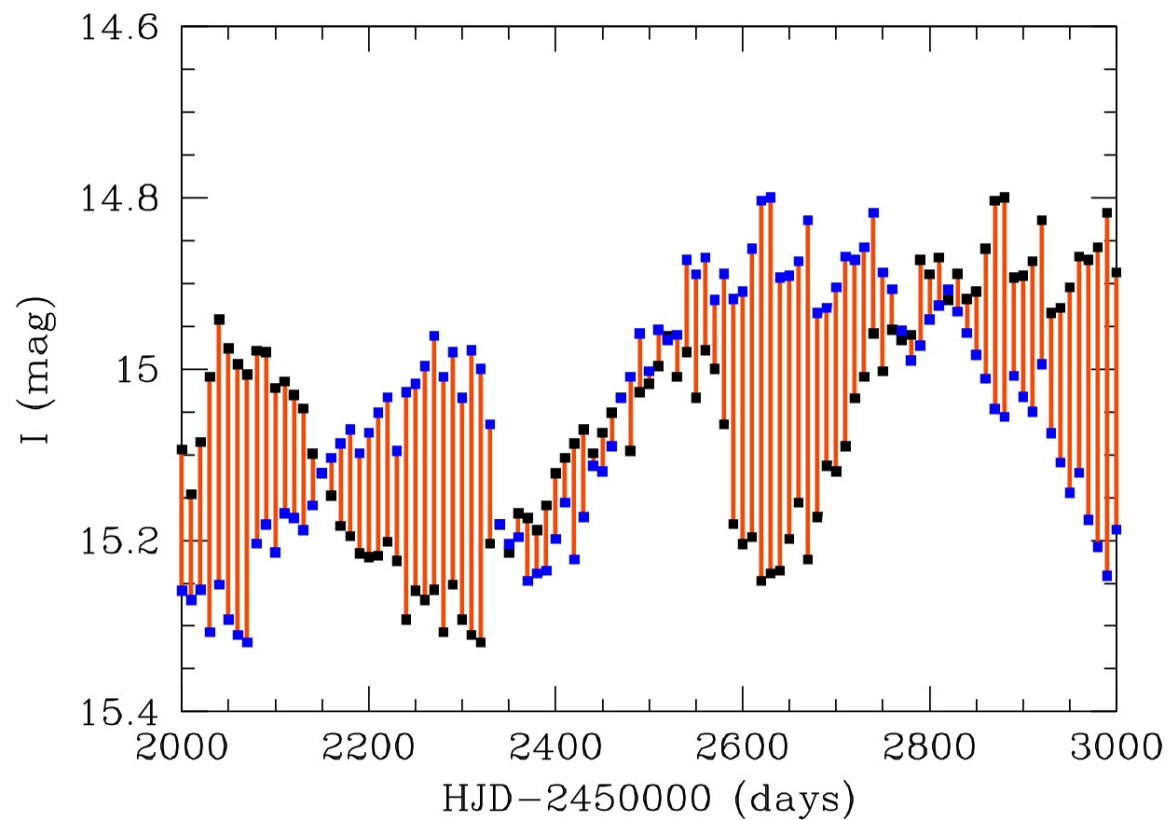
Structure Function



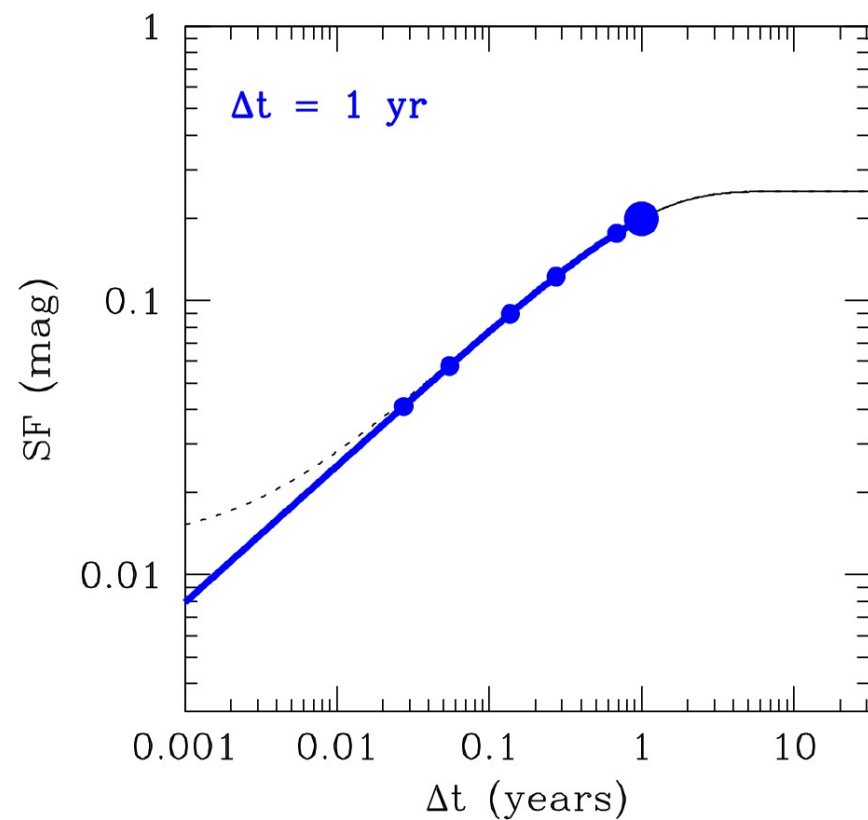
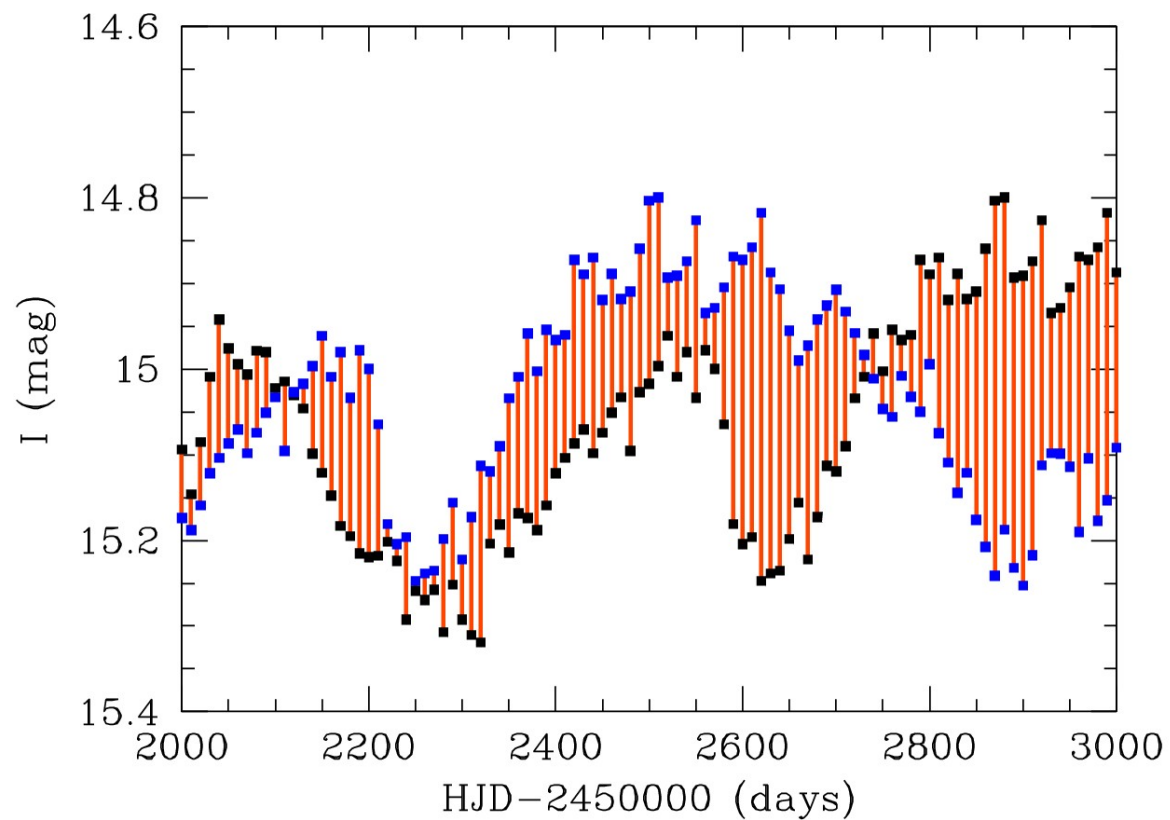
Structure Function



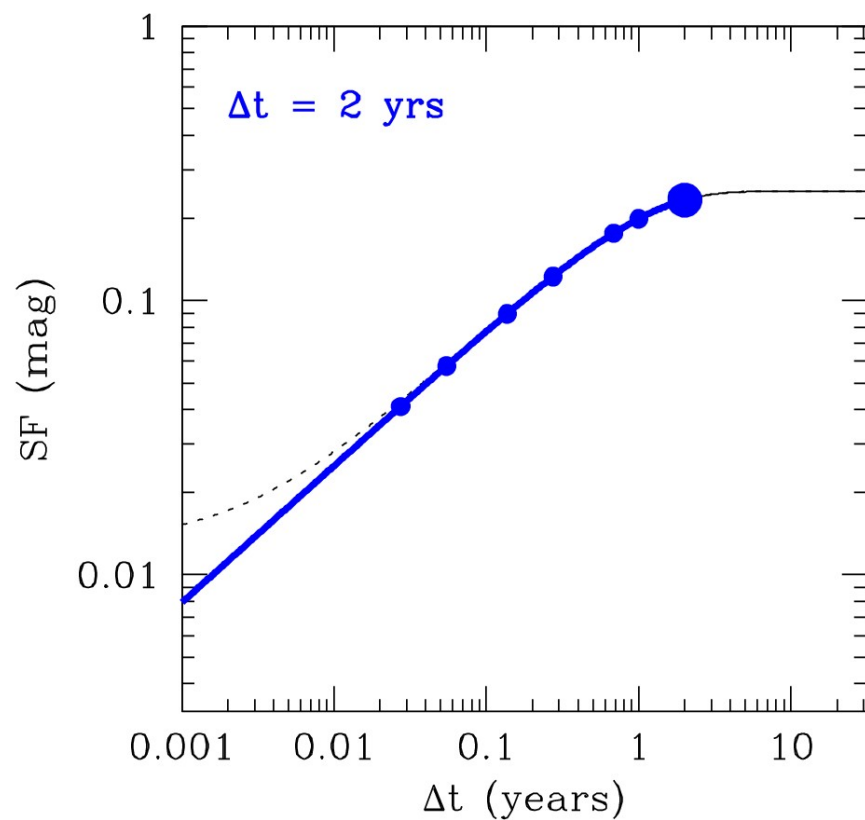
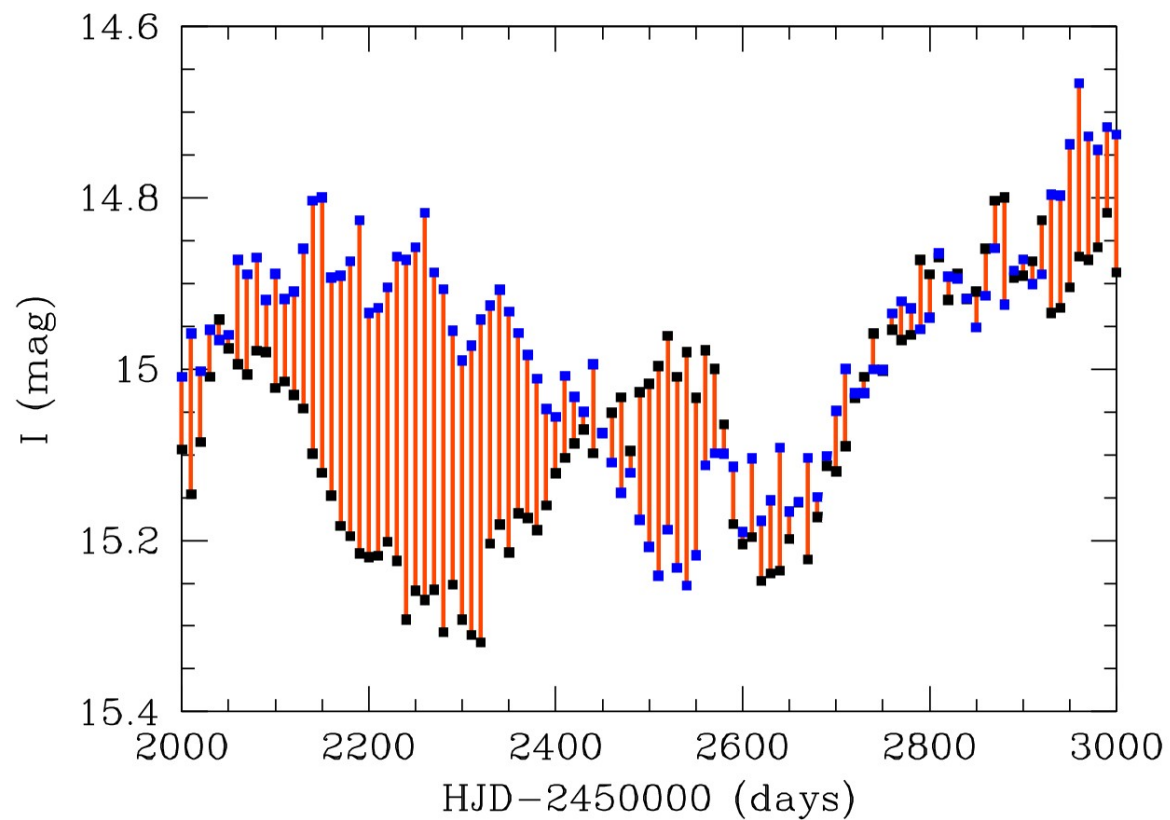
Structure Function



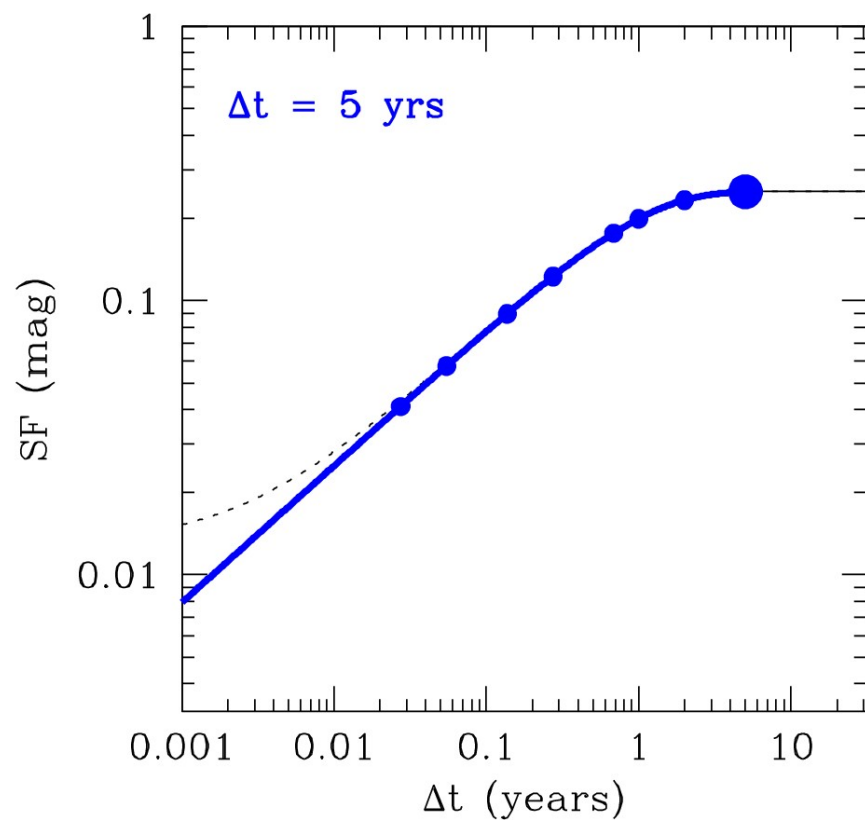
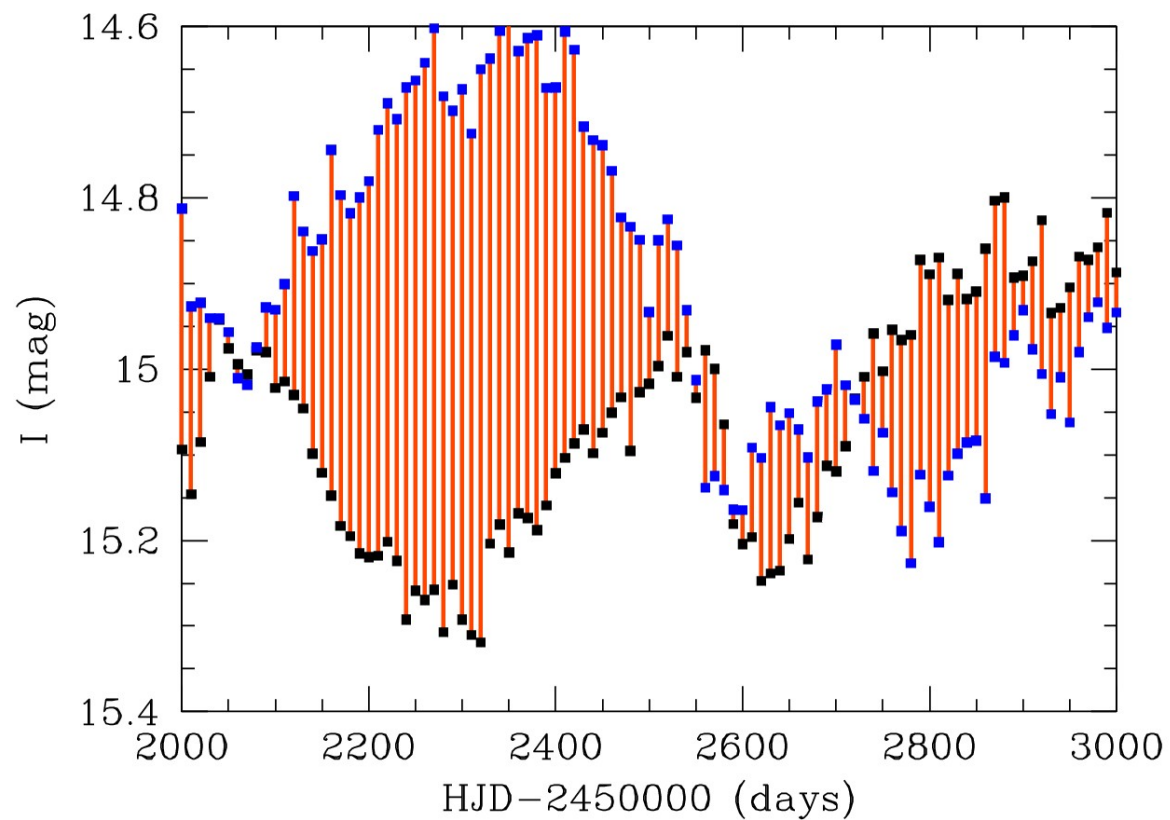
Structure Function



Structure Function



Structure Function



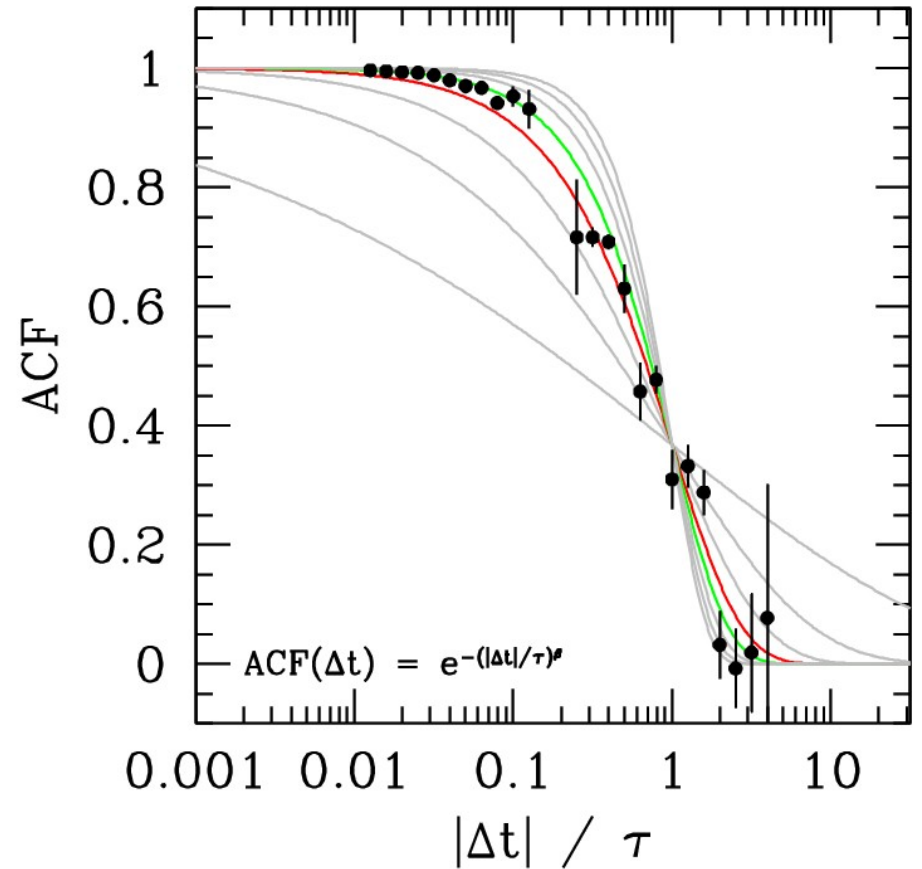
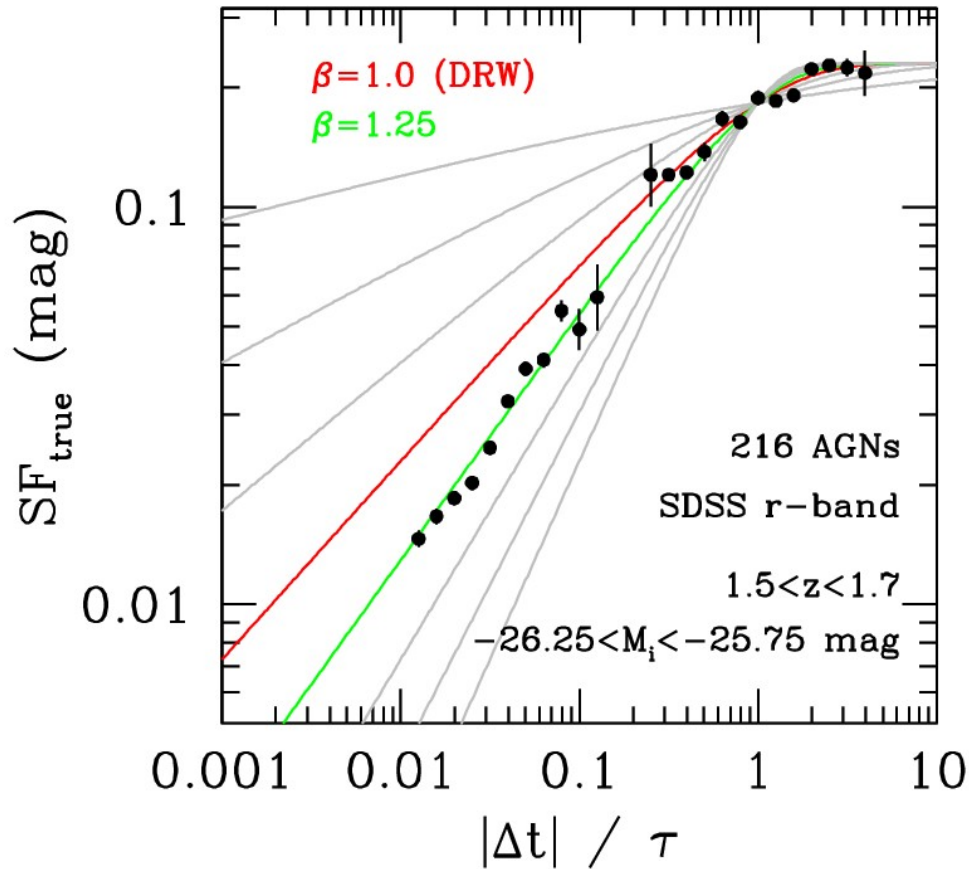
Structure Function

$$\text{cov}(y_i, y_j) \equiv \text{var}(y_i) - V(y_i, y_j)$$

$$V(y_i, y_j) = \frac{1}{2} \langle (y_i - y_j)^2 \rangle$$

$$SF = \sqrt{2V}$$

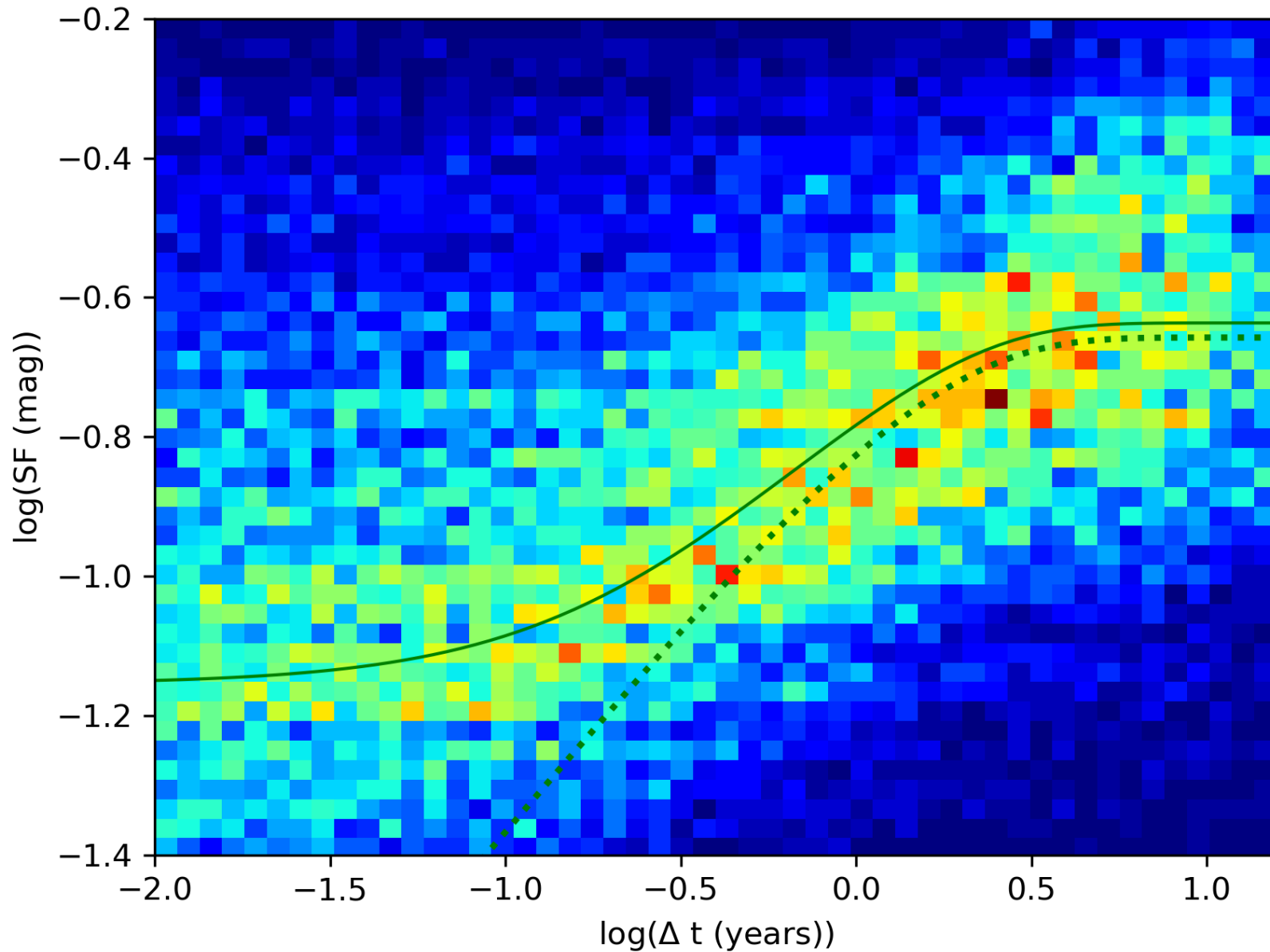
Structure Function and ACF



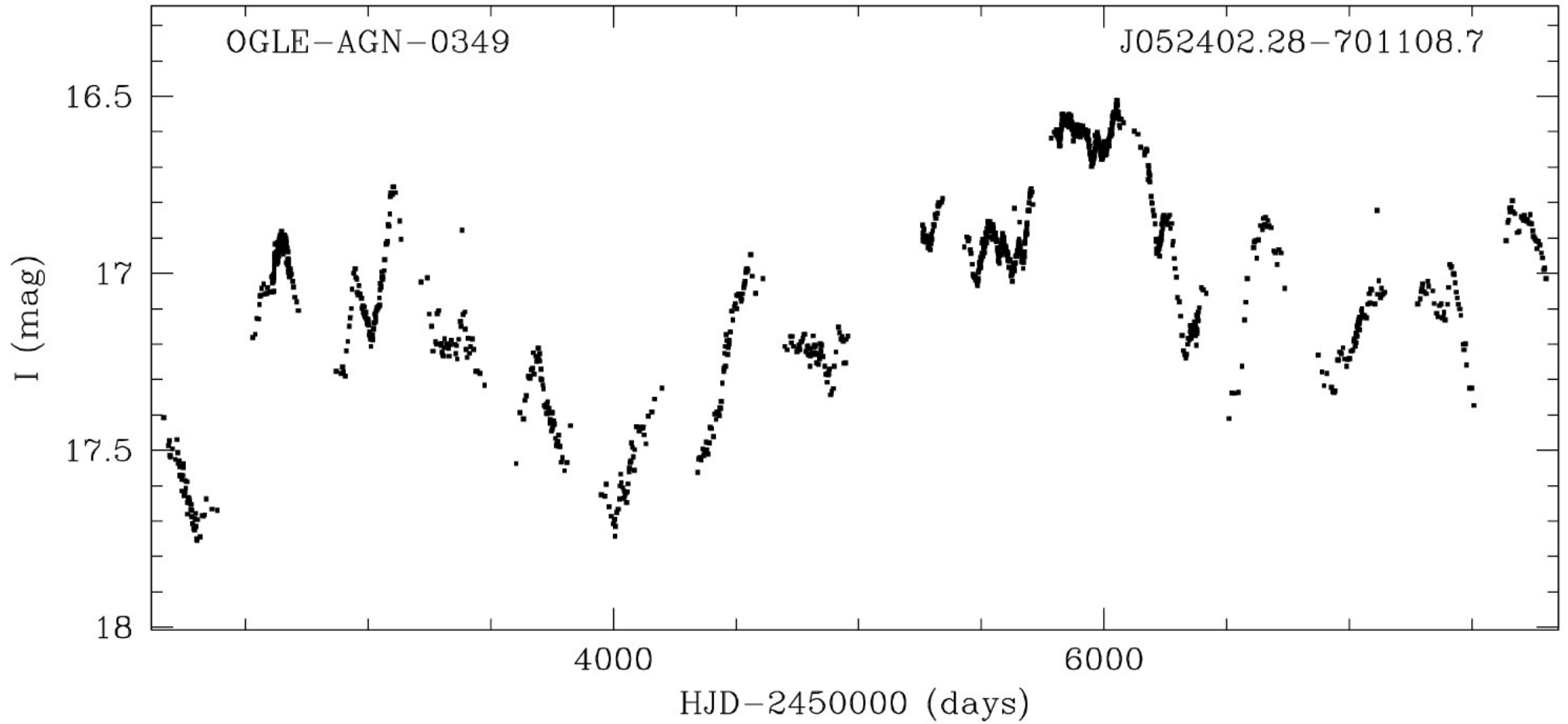
$$SF = \sqrt{SF_\infty^2 (1 - ACF) + 2\sigma_n^2}$$

$$ACF = e^{-\left(\frac{|\Delta t|}{\tau}\right)^\beta}$$

Structure Function: OGLE-III + OGLE-IV



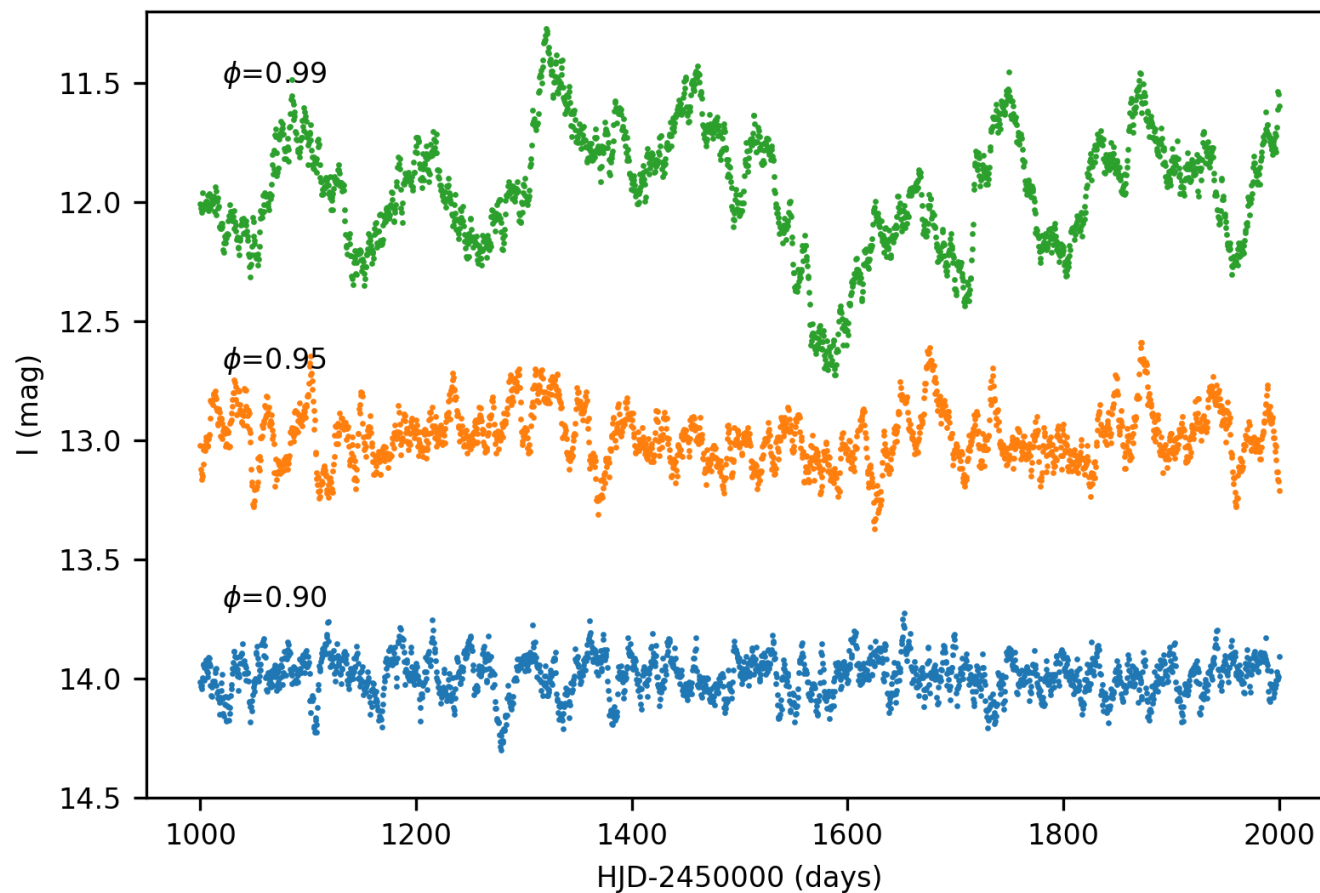
Light Curve Modeling



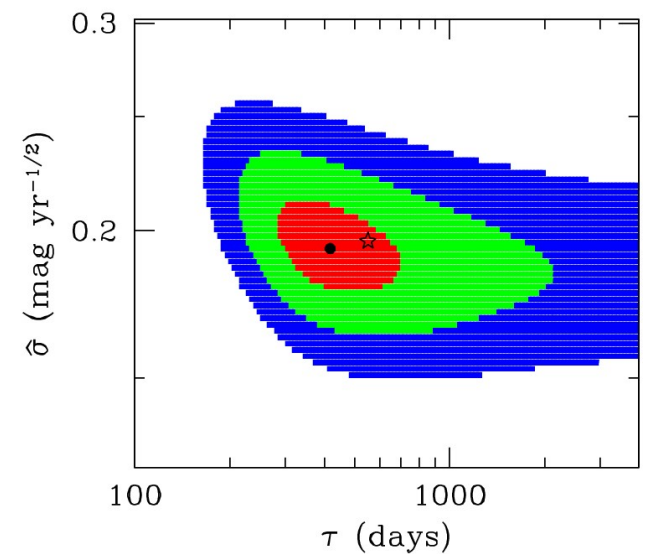
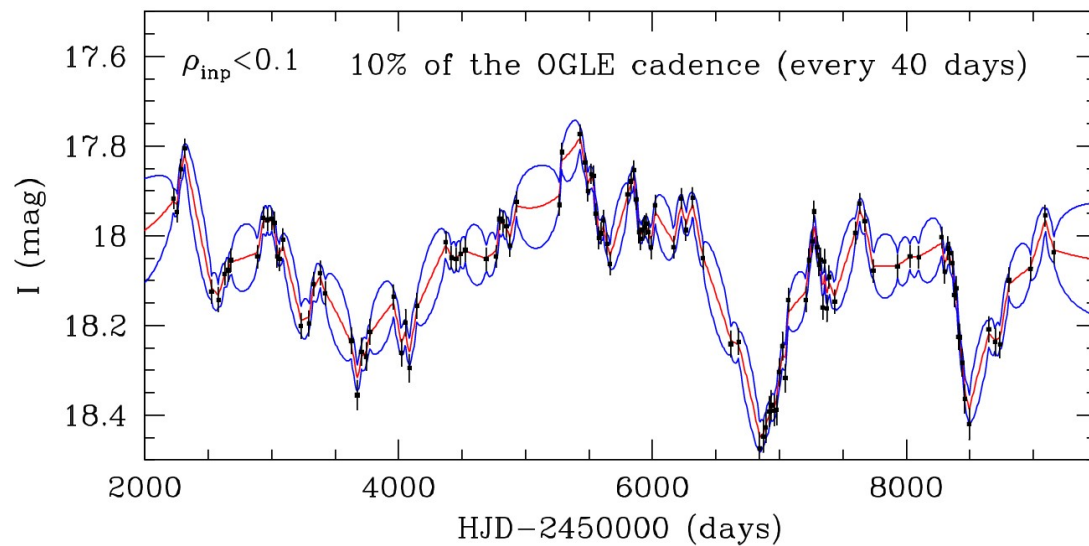
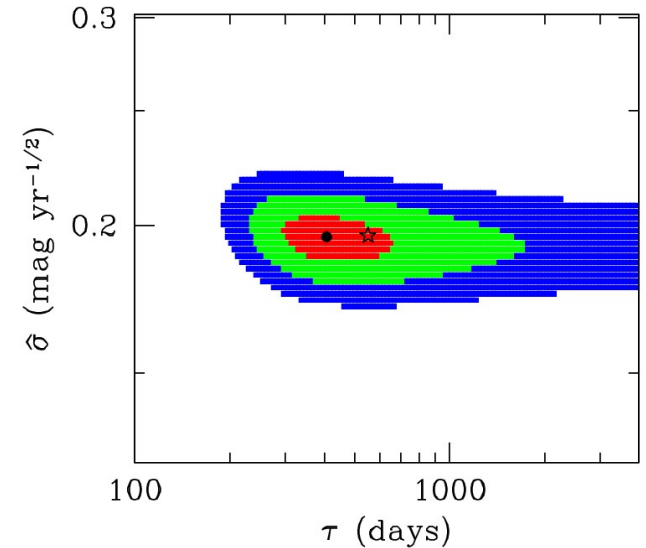
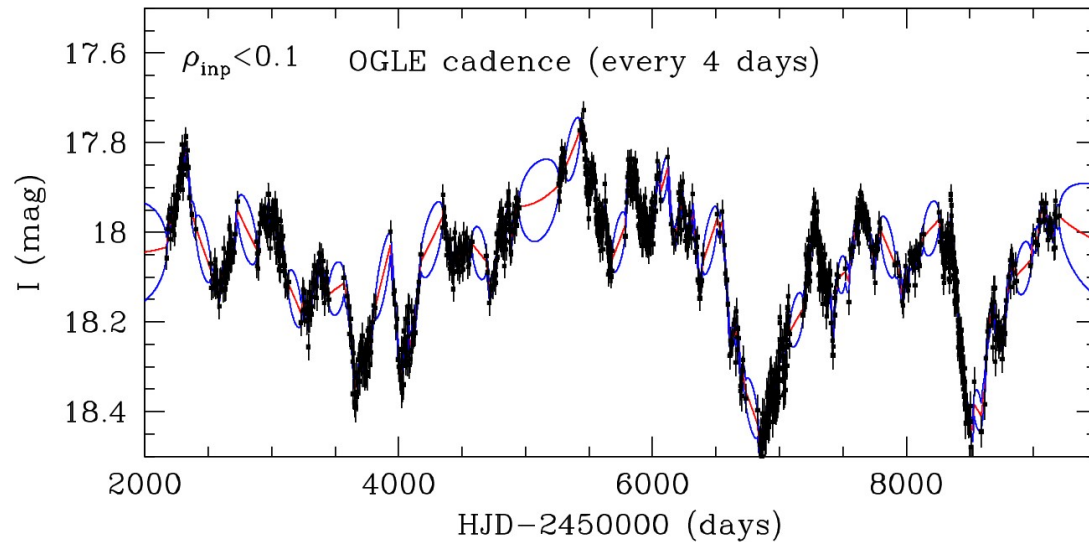
Auto Regressive (AR) models

$$x_i = \mu + \phi_1 x_{i-1} + \epsilon_i, \quad (1)$$

where ϕ_1 is the auto-regressive or “lag” coefficient that indicates how closely tied future values are to past values and where ϵ_i represents a source of noise.



Damped Random Walk (DRW)



(C)ARMA models

$$x_i = \mu + \phi_1 x_{i-1} + \epsilon_i, \quad (1)$$

where ϕ_1 is the auto-regressive or “lag” coefficient that indicates how closely tied future values are to past values and where ϵ_i represents a source of noise.

The general notation for a p_{th} -order AR process is

$$x_i = \mu + \sum_1^p \phi_p x_{i-p} + \epsilon_i. \quad (2)$$

For example, in an AR($p = 2$) process, the state of the system depends on two lag terms (and thus has two timescales):

$$x_i = \mu + \phi_1 x_{i-1} + \phi_2 x_{i-2} + \epsilon_i. \quad (3)$$

(C)ARMA models

Moving Average (MA) models:

$$x_i = \epsilon_i + \theta_1 \epsilon_{i-1}. \quad (4)$$

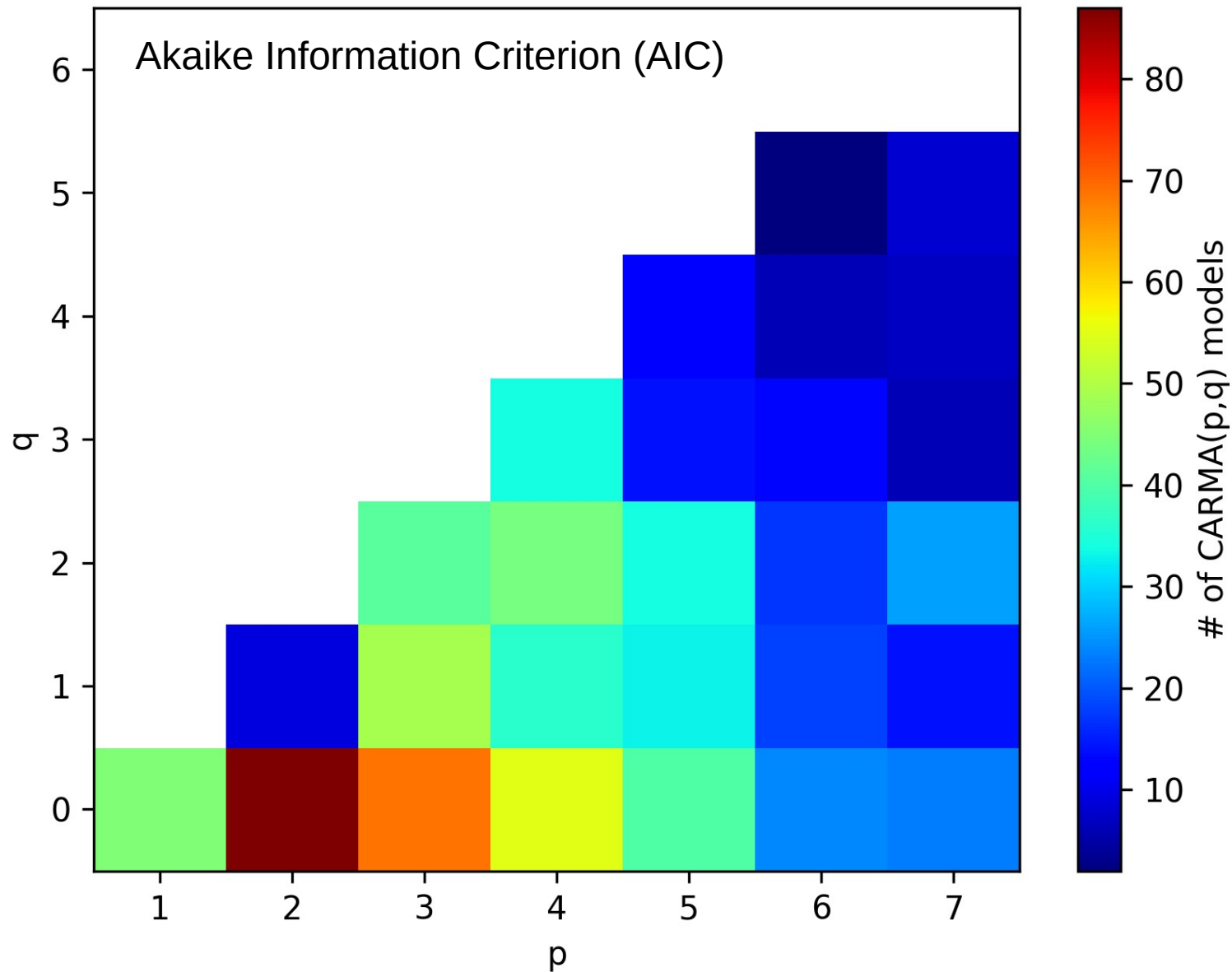
In the simplest MA process (order 1 with $\theta_1 \neq 0$), the system depends not only on the current shock, but also the previous one.

$$x_i = \sum_1^q \theta_q \epsilon_{i-q} + \epsilon_i.$$

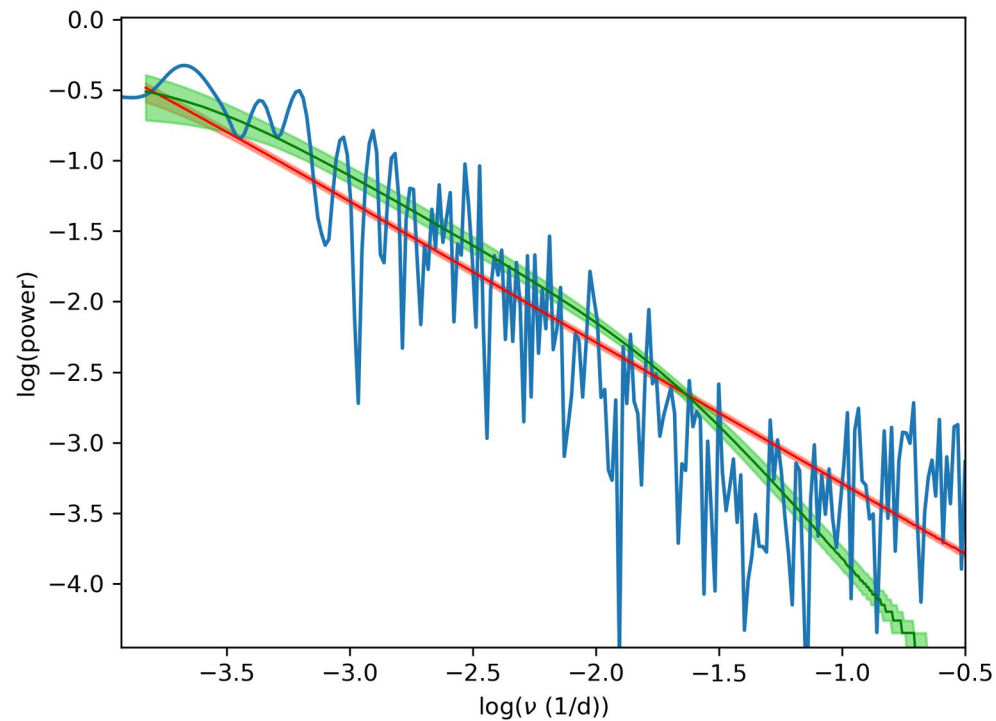
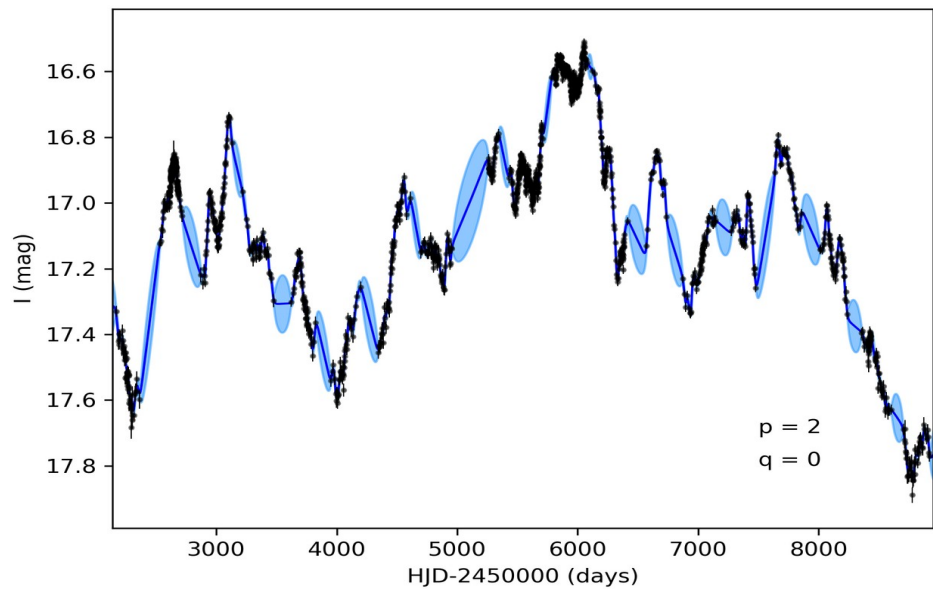
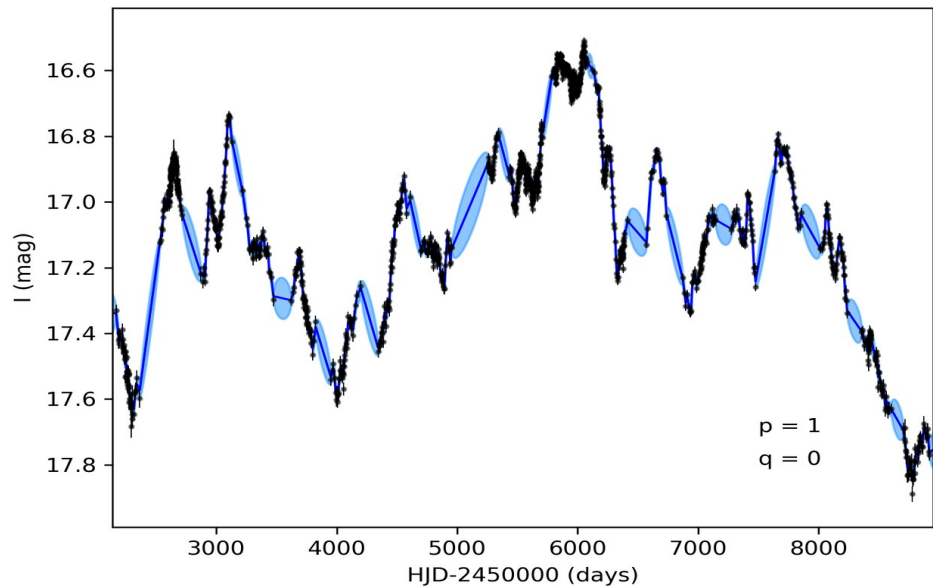
CARMA model: $p+q+1$ parameters and $q < p$

$$x_i = \mu + \sum_1^p \phi_p x_{i-p} + \sum_1^q \theta_q \epsilon_{i-q} + \epsilon_i$$

CARMA: OGLE-III + OGLE-IV



CARMA: OGLE-III + OGLE-IV



Thank you!

Revisiting Stochastic Variability of AGNs with Structure Functions
Kozłowski Szymon, 2016, The Astrophysical Journal, 826, 118

A degeneracy in DRW modelling of AGN light curves
Kozłowski Szymon, 2016, MNRAS, 459, 2787

Limitations on the recovery of the true AGN variability parameters
using damped random walk modeling
Kozłowski Szymon, 2017, A&A, 597, 128

A Method to Measure the Unbiased Decorrelation Timescale
of the AGN Variable Signal from Structure Functions
Kozłowski Szymon, 2017, The Astrophysical Journal, 835, 250

A Survey Length for AGN Variability Studies
Kozłowski Szymon, 2021, Acta Astronomica, 71, 103